

# Steganalysis using Logistic Regression



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25 January 2011

# Steganalysis using Logistic Regression

## Outline

- Classification in steganalysis
- Logistic regression
- Experimental methodology
- Experimental results

# Classification in steganalysis

Steganalysis is a binary classification problem:

- Innocent cover objects
- vs
- Stego objects.

This is a gross approximation unless

1. the embedding method is known,
2. the payload size is known,
3. the cover source is known.

*For quite practical reasons, steganalysis should probably be multi-class.*

# Classification in steganalysis

A steganalysis method is broadly:

- **Analytical** – some property of covers is distorted in an understood way.  
Spatial-domain bit replacement [Dumitrescu, 2003; Ker, 2005-7]  
LSB replacement in JPEGs [Kodovský, 2010]

*Generally only for flawed embedding.*

- **Empirical** – machine learning algorithms applied to vectors of features.  
Support vector machines and noise features [Farid, 2002]  
Support vector machines and JPEG histograms [Shi, 2006; Pevný, 2007]  
Support vector machines and pixel difference co-occurrence [Pevný, 2010]

*Almost all schemes in the literature use SVMs. Is there an alternative?*

# Logistic regression

Not a classifier! Attempts to model class probabilities.

Predict **log-odds** as linear function of input data. Binary case:

$$P(C_1|x) = \frac{1}{1 + \exp(-(w^T x + b))}$$

with coefficients  $w$ ,  $b$  learned by maximum likelihood.

$$\log L = \sum_{j=1}^n y_j \log P(C_1|x_j) + (1 - y_j) \log(1 - P(C_1|x_j)) - \lambda \|w\|.$$

↑  
*regularization*

*Advantage 1: predicts class probabilities (though often used as a simple classifier).*

Can represent problem in dual space, and use the kernel trick.

# Multinomial logistic regression

Predict log-odds of all classes simultaneously:

$$P(C_i|x) = \frac{\exp(w_i^T x)}{\sum_j \exp(w_j^T x)}$$

with matrix of  $w_j$ 's learned by maximum likelihood.

*Advantage 2:*

- *Time complexity for  $k$  classes is  $O(k)$ ,*
- *Time complexity for SVMs simulating multi-class by all pairs is  $O(k^2)$ .*

# Experimental methodology

Want to compare SVM and LR steganalysis detectors in terms of

- accuracy, and
- speed.

## Extent of comparison

- Images in three sets: 'Camera', 'BOSS', 'BOWS'.
- Spatial-domain, total payload 0.5 bits per pixel:
  - LSB matching,
  - LSB replacement,
  - 2LSB replacement (2 bits per used pixel),
  - Mod-5 matching ( $\log_2 5$  bits per used pixel),plus covers, makes up to 5 classes.
- SPAM features (686 dimensional).

# Experimental methodology

## Implementation

SVM            libSVM (optimized C++)

LR            'minfunc' (MATLAB)

Smooth SVM   'minfunc' (MATLAB)

... with linear or Gaussian kernel.

## Training regime

- Split image set into training & testing.
- Hyperparameter optimization by cross-validation on training set.
- Final training on entire training set.
- Test on testing set.
- Compare performance differences by Student  $t$ -test.



# Results: kernelized classifiers

Image set	Classification Problem	Classification accuracy		Difference
		SVM	Logistic Regression	
Camera	Binary cover v LSBM	96.20%	95.85%	Insignificant ( $p > 0.05$ )
	Binary cover v Mod5	97.55%	97.45%	Insignificant ( $p > 0.05$ )
	Binary cover v LSBR	97.15%	97.45%	Insignificant ( $p > 0.05$ )
	Binary cover v 2LSB	98.25%	98.45%	Insignificant ( $p > 0.05$ )
Camera	5 class	83.01%	80.05%	Insignificant ( $p > 0.05$ )
BOSS	5 class	85.05%	82.30%	Somewhat significant ( $p \approx 0.01$ )
BOWS	5 class	95.95%	96.32%	Insignificant ( $p > 0.05$ )

# Results: kernelized classifiers

Image set	Classification Problem	Classification accuracy		Difference
		Smooth SVM	Logistic Regression	
Camera	Binary cover v LSBM	96.15%	95.85%	Insignificant ( $p > 0.05$ )
	Binary cover v Mod5	97.70%	97.45%	Insignificant ( $p > 0.05$ )
	Binary cover v LSBR	96.90%	97.45%	Insignificant ( $p > 0.05$ )
	Binary cover v 2LSB	98.35%	98.45%	Insignificant ( $p > 0.05$ )
Camera	5 class	80.89%	80.05%	Insignificant ( $p > 0.05$ )
BOSS	5 class	83.81%	82.30%	Insignificant ( $p > 0.05$ )
BOWS	5 class	96.59%	96.32%	Insignificant ( $p > 0.05$ )

# Results: kernelized classifiers

Image set	Classification Problem	Classification accuracy		Final training time	
		Smooth SVM	Logistic Regression	Smooth SVM	Logistic Regression
Camera	Binary cover v LSBM	96.15%	95.85%	106s	145s
	Binary cover v Mod5	97.70%	97.45%	95s	160s
	Binary cover v LSBR	96.90%	97.45%	101s	113s
	Binary cover v 2LSB	98.35%	98.45%	85s	127s
Camera	5 class	80.89%	80.05%	2504s	1394s
BOSS	5 class	83.81%	82.30%	43003s	23446s
BOWS	5 class	96.59%	96.32%	84198s	42311s

# Conclusions

- Logistic regression is a possible alternative to SVMs in steganalysis, with two potential advantages:
  - *well adapted to multinomial case,*
  - *produces class probabilities.*
- The detection accuracy seems to be similar to SVMs.
- For binary classification, the speed is similar to an SVM implemented on the same minimizer.
- For multinomial classification, the speed is superior.
  - *But this excludes the SMO algorithm for SVMs.*
  - *Needs further work to examine SMO-type algorithm for LR.*