# Eclectic CSP 

Bernard Sufrin and Quentin Miller*

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#### Abstract

In this note we introduce the main features of Eclectic CSP - an experimental language, based on the Occam 3 model of communication.


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Warning: The language description herein is subject to change at any time.

## 1 Introduction

In this note we introduce the main features of Eclectic CSP - an experimental specification and programming notation whose semantic features have been borrowed from many sources - including OCCAM [1, 2], CSP [2], Z [3], Polyá, and the Refinement Calculus [4].

The language was originally designed to implement telephone network services within an intelligent Networking server. But we also expected and hoped that the language would be more generally useful in situations where concurrency is of the essence, and where the ideals of predictability and correctness of programs are important.

Our purpose in offering eCSP as an implementation language for telephony services was speculative: we wanted to see whether its support for concurrency would facilitate the construction of new and more imaginative services, and whether service designers would accept eCSP as an adjunct to, if not a replacement of, the notations based on finite state machines that they were then using.

We did not expect the final form of the language to have all the features described here - but language design is a hard process, and the world of computing is littered with attempts to build application-specific languages by starting with an inadequate base and adding features $a d-h o c$. It also seemed to us that concurrency was far too important a feature to be provided without also making it possible to provide some compile time support for a discipline of councurrent programming. So we started by designing a full-featured concurrent language, intending to see what had to be removed.

Happily it turned out that very little needed to be removed, and that our expectation that the language would be more generally useful has proven to be realistic.

The presence of specification constructs in the language means that not every program or system described in it will be directly translateable into code. The process of transforming a pre-program (or specification) into a program is called refinement, and the language has features that make certain aspects of this transformation fairly easy.

All eCSP programs can be implemented straightforwardly by translating them into a language that is powerful enough to support concurrent threads - and we originally implemented it by translating it more or less directly into Java.

Note: In the body of this text we use two forms of the language: the publication form - which uses sophisticated typography including ordinary mathematical symbols and is intended to be easy on the eye, and the machine-oriented form - which is expressed entirely in the ISO-Latin-1 alphabet.

## 2 The Core Language

### 2.1 Types

### 2.1.1 Simple Types and Built-in Type Constructors

The built-in simple types of eCSP are the integers, reals, characters, and booleans - denoted respectively Int, REAL, CHAR, BOOL. The unit type () has a single element, written ().

Note that characters are delimited by single quotes (e.g. 'a'). Escape sequences for denoting unprintable characters are the same as those used in C.
To assert that an expression $E$ has type $T$ we write ( $E: T$ ).
If $T_{1}, \ldots, T_{n}$ are types then $\left(T_{1}, \ldots, T_{n}\right)$ denotes the type of $n$-tuples, which are written $\left(E_{1}, \ldots E_{n}\right)$ (where each expression $E_{i}$ has type $\left.T_{i}\right)$. If $v:\left(T_{1}, \ldots, T_{n}\right)=$ $\left(v_{1}, \ldots v_{n}\right)$, and $i$ is a constant in the range $1 . . n$, then $v . i$ denotes the $i^{t h}$ component of $v$.

If $T$ is a type, then $[T]$ denotes the type of (finite, origin 0 ) vectors of $T$ and $\{T\}$ denotes the type of (finite) sets of elements of $T$. If, in addition, $E$ is a constant integer-valued expression, then $[T] \# E$ denotes the type of (finite, origin 0 , size $E)$ vectors of $T$ : this is a subtype of $[T]$. Moreover $\{T\} \# E$ denotes the type of finite sets of elements of $T$ with at most $E$ elements: this is a subtype of $\{T\}$.
If $v:[T]$ then $\# v$ denotes its size, and $v(i)$ denotes the element with index $i$ (if $i<\# v)$. A variety of additional operations on vectors are provided, including catenation (written + ).

If $v:\{T\}$ then $\# v$ denotes its size. The usual operations on sets are provided, including union (written + ), intersection (written $*$ ), and difference (written $-)$. The membership test and its negation are is written $\in$ and $\notin$ respectively (or in Latin-1, MEM and NOTMEM).

Expressions of the following forms denote sets and vectors respectively

$$
\begin{array}{ll}
\left\{E_{1}, \ldots, E_{n}\right\} & \left(\text { where all } E_{i}: T\right) \\
{\left[E_{1}, \ldots, E_{n}\right]} & \left(\text { where all } E_{i}: T\right)
\end{array}
$$

Notations for set and vector comprehension take the following forms

$$
\left.\left.\left.\begin{array}{l}
\left\{\left(\text { for } v_{1}: T_{1} \text { in } E_{1} \mid B_{1} ;\right.\right.
\end{array} \ldots ; \text { for } v_{n}: T_{n} \text { in } E_{n} \mid B_{n}\right) E\right\}\right\} \text { } \begin{aligned}
& {\left[\left(\text { for } v_{1}: T_{1} \text { in } E_{1} \mid B_{1} ; \ldots ; \text { for } v_{n}: T_{n} \text { in } E_{n} \mid B_{n}\right) E\right]}
\end{aligned}
$$

where the $E$ are expressions representing each element, the $v_{i}$ are variable names, the $T_{i}$ are types, the $E_{i}$ are expressions of type $\left\{T_{i}\right\}$ or $\left[T_{i}\right]$, and the $B_{i}$ are boolean expressions which may be omitted if identically true.

| Operator | Latin-1 Variant | Explanation |
| :---: | :---: | :--- |
| dom | DOM | Domain |
| ran | RAN | Range |
| $\oplus$ | ++ | Relational overriding |
| $\cup$ | + | Relational union |
| $\triangleright$ | $\mid>$ | Range Restriction |
| $\triangleleft$ | $<1$ | Domain Restriction |

Table 1: Relational Operators

The (for...) construct in a comprehension is called a generator. If one of the binary operators,$+ \times, \vee$, or $\wedge$ appears in parentheses in front of a generator and an expression, this operator will be used to combine the generated values into a single value. For example, if $v$ is a vector of integers,

$$
(+)(\text { for } n \text { in } v)(n \times n)
$$

yields the sum of the squares of the values in $v$; and if $s$ is a set of boolean values,

$$
(\vee)(\text { for } b \text { in } s) b
$$

calculates whether at least one of its elements is true.
Contiguous vectors of integers have a special notation
$m . . n$ means the vector of numbers from $m$ to $n$ inclusive
$m \# n$ means the vector of numbers from $m$ to $m+n-1$ inclusive

The type of (finite) mappings from elements of domain type $D$ to elements of range type $R$ is denoted $D \rightarrow R$, and the type of (finite) binary relations between these types is denoted $D \leftrightarrow R$. The type $D \leftrightarrow R$ is a subtype of $D \leftrightarrow R$, which is a synonym for $\{(D, R)\}$. The usual relational operators are available; they are listed in table 1.

### 2.1.2 Type Synonyms

The name $n m$ may be given to type $T$ by a declaration of the form

$$
\text { type } n m=T
$$

For example,

```
type Coord = (INT, INT)
type Polygon = [Coord]
```


### 2.1.3 Free Types

A free data type named $n m$ with constructors $k_{1}, \ldots k_{n}$ over types $T_{1}, \ldots, T_{n}$ is defined by

$$
\text { data TypeName }=k_{1} T_{1}+\ldots+k_{n} T_{n}
$$

The constructors $k_{1}, \ldots$ are functions used to map values of the given types $T_{1}, \ldots$ into the data type TypeName that is being defined.

Recursive types can be specified this way, and the new type name may appear on the right hand side of the definition.

Example 1 Free Type definition: Binary Trees with integer leaves

```
    DATA BT = Leaf Int + Branch (BT, BT)
```

A mutually recursive collection of free types $T_{a}, T_{b}, \ldots$ is defined by

$$
\begin{array}{ll}
\text { data } & T_{a}=k_{a_{1}} T_{a_{1}}+\ldots \\
\text { and } & T_{b}=k_{b_{1}} T_{b_{1}}+\ldots
\end{array}
$$

A constructor may be declared without an associated value field, as in the type of lists of integers declared in example 2.

Example 2 Free Type definition: Lists of integers
DATA IntList $=$ Nil + Cons (INT, IntList)

Example 3 Mutually recursive Free Type Definition

```
    DATA BT = Atom ST + Branch (BT, BT)
```

    AND \(\quad \mathrm{ST}=\) Empty +Vec [BT]
    Note that free data types may not be anonymous - i.e. a type expression of the form

$$
k_{a_{1}} T_{a_{1}}+\ldots+k_{a_{n}} T_{a_{n}}
$$

may be used only in the declaration of a new named type.

### 2.1.4 Record Types

If $T_{1}, \ldots T_{n}$ are types, and $i_{i}, \ldots i_{n}$ are names, then the type expression

$$
\left\{i_{1}: T_{1}, \ldots, i_{n}: T_{n}\right\}
$$

denotes the type of records with fields named $i_{1}, \ldots$ which have types $T_{1}, \ldots$ respectively.
If $E=\left\{\left|i_{1}=E_{1}, \ldots, i_{n}=E_{n}\right|\right\}$ then $E . i_{1}=E_{1}, \ldots, E . i_{n}=E_{n}$.
Example 4 A record type: Account and an instance of that type
TYPE Account =
\{। balance: INT,
overdraft: INT
$1\}$
$\{\mid$ balance $=-50$, overdraft $=50 \mid\}:$ Account

Example 5 Declaration of a record type: Bank
TYPE Bank $=$
\{। account: Person +> Account, balance: INT
$1\}$

### 2.1.5 Free Type Extension and Subtyping

It can be convenient to define a free data type by extending an existing free type. If $n m$ is the name of an existing free type, then the free type ext defined by

$$
\text { data } e x t=\text { data } n m+k_{1} T_{1}+\ldots+k_{n} T_{n}
$$

is an extension of the type $n m$ which has all the constructors of $n m$ together with the additional constructors $k_{1}, \ldots k_{n}$.

The type $n m$ is said to be a subtype of the extended type, and a value of type $n m$ may appear wherever a value of type of ext is required.

Example 6 A free type with two extensions

```
DATA SmallNum = Zero + One + Two
DATA MedNum = DATA SmallNum + Three + Four + Five
DATA Num = DATA MedNum + Big INT
```


### 2.1.6 Record Type Extension and Subtyping

It can be convenient to define a record type by extending an existing record type. If $T_{1}$ and $T_{2}$ are two record types, with disjoint field names then the type $T_{1}+T_{2}$ is a record type which has all the fields of $T_{1}$ and all the fields of $T_{2}$.
$T_{1}+T_{2}$ is an extension of $T_{1}$ and an extension of $T_{2}$. It is a subtype of $T_{1}$, and a value of type $T_{1}+T_{2}$ may appear whenever a value of type $T_{1}$ is expected. For reasons of implementation efficiency, $T_{1}+T_{2}$ is not considered a subtype of $T_{2}$, although the gods of symmetry would no doubt be better pleased if it were.

### 2.1.7 Port Types

If $T$ is a type, then ? $T$ is the type of port from which values of type $T$ can be input, and $!T$ is the type of port to which values of type $T$ can be output. A port of type ? $T$ and a port of type $!T$ may be joined by a channel of type $T$, through which data may be transferred in one direction. Ports are first-class values, in the sense that they can be passed as parameters, delivered as results, and communicated over channels.
A port of type ? $T$ or $!T$ is always implemented by a channel of type $T$ (see 2.2.16). In fact the only reason for distinguishing between ports and channels is that a port embodies an undertaking to use the channel that implements it in only one direction. Both these types are simple port types.
If $P T$ is a port type, then the type $[P T]$ is a port vector type - the type of vectors of ports which all have the specified port type. Such types are composite port types, and their values are implemented by channel vectors (see 2.3.1).
If $P T_{1}, \ldots, P T_{n}$ are port types, then the type $\left\{i_{1}: P T_{1}, i_{n}: P T_{n}\right\}$ is a port record type - the type of records whose fields have the specified port types. Port record types are also composite port types, and their values are implemented by channel records (see 2.3.1).
If $P T_{1}, \ldots, P T_{n}$ are port types, then the type $\left(P T_{1}, \ldots, P T_{n}\right)$ is a port tuple type - the type of tuples whose components have the specified port types. Port tuple types are also composite port types, and their values are implemented by channel tuples (see 2.3.1).

### 2.1.8 Complementary Port Types

If a process communicates using a port of type $P T$, then it is sensible, indeed essential, to run it in parallel with a process that communicates using a port of the complementary port type.
If $P T$ is a port type, then its complementary port type is written as $-P T$. Complementary port types are defined as follows:

| $-? T$ | $=!T$ | for any type $T$ |
| :--- | :--- | :--- |
| $-!T$ | $=? T$ | for any type $T$ |
| $-[P T]$ | $=[-P T]$ | for any port type $P T$ |
| $-\left(P T_{1}, \ldots, P T_{n}\right)$ | $=\left(-P T_{1}, \ldots,-P T_{n}\right)$ | for any port types $P T_{1}, \ldots$ |
| $-\left\{i_{1}: P T_{1}, \ldots, i_{n}: P T_{n}\right\}=$ | $\left.\left\{i_{1}:-P T_{1}, \ldots, i_{n}:-P T_{n}\right\}\right\}$ for any port types $P T_{1}, \ldots$ |  |

### 2.2 Processes

eCSP programs are built from processes, the simplest of which are called actions. An action may be a skip, an exception, an assignment, an output, or a specified action. It will shortly become clear why an input is not simply an action.

### 2.2.1 Skip

A skip, written skip, has no effect on the program. A skip is typically used to convey explicitly a programmer's intention that nothing be done at a particular point in the program. See Example 25 for a typical situation.

### 2.2.2 Assignment

An assignment takes the form

$$
v_{1}, v_{2}, \ldots, v_{n}:=e_{1}, e_{2}, \ldots, e_{n}
$$

where the $v_{i}$ are variables (or, more generally, expressions denoting locations), and the $e_{i}$ are expressions. The expressions must be assignable to the variables, and this is so only if the type of each expression $e_{i}$ is a subtype of the declared type of the corresponding variable $v_{i}$.
The list of expressions is evaluated in parallel, and the resulting values are assigned in parallel to the variables.

Example 7 Rotating three variables in a single assignment
$\mathrm{a}, \mathrm{b}, \mathrm{c}:=\mathrm{b}, \mathrm{c}, \mathrm{a}$

### 2.2.3 Output

An output takes the form

$$
p!e
$$

where $p$ is an output port, and $e$ is an expression. The type of the expression must be a subtype of the type of the port.

The expression is evaluated, and its value transmitted via the port to another process; the action is not complete until that process has input the value.

### 2.2.4 Bracketed Processes

A process $p$ may be enclosed in brackets begin $p$ end without changing its meaning.

### 2.2.5 Composite Processes

The usual forms of sequential process composition are available:

```
Sequential composition \(a_{1} ; a_{2} ; \ldots\)
Alternation \(\quad\) if \(e_{1} \rightarrow a_{1}\) or \(\ldots\) or \(e_{n} \rightarrow a_{n}\) fi
Iteration do \(e_{1} \rightarrow a_{1}\) or \(\ldots\) or \(e_{n} \rightarrow a_{n}\) od
```

In these forms the $e_{i}$ are boolean expressions, called guards, and the $a_{i}$ are processes.
An alternation evaluates each of the guards. If none is true then the program aborts. If any are true, then one of the processes corresponding to a true guard is executed.

An iteration evaluates each of the guards. If none are true then the iteration terminates. If any are true, then one of the processes corresponding to a true guard is executed, and the iteration as a whole is repeated.

If $I$ is the process

$$
\text { do } e_{1} \rightarrow a_{1} \text { or } \ldots \text { or } e_{n} \rightarrow a_{n} \text { od }
$$

then $I$ is equivalent to

$$
\text { if } e_{1} \rightarrow a_{1} ; I \text { or } \ldots \text { or } e_{n} \rightarrow a_{n} ; I \text { or } \neg e_{1} \wedge \ldots \wedge \neg e_{n} \rightarrow \text { skip } \mathbf{f i}
$$

An alternation or iteration may use "else" (everywhere) to separate alternatives instead of "or". In this case the guards are evaluated in sequence, and the process corresponding to the first true guard is executed.

```
Example 8 Two ways to calculate the maximum of m, n
    IF m>n -> max := m
    ELSE TRUE -> max := n
    FI
    IF m>=n -> max := m
    OR m<=n -> max := n
    FI
```

Example 9 Calculate Greatest Common Divisor of mand n
DO $\mathrm{m}>\mathrm{n} \rightarrow \mathrm{m}:=\mathrm{m}-\mathrm{n}$
OR m<n $\rightarrow \mathrm{n}:=\mathrm{n}-\mathrm{m}$
OD

There are also two forms of composition that perform case-analysis by patternmatching:

$$
\begin{array}{ll}
\text { Case alternation } & \text { if } e \text { is } \pi_{1} \rightarrow a_{1} \text { or } \ldots \text { or } \pi_{n} \rightarrow a_{n} \text { fi } \\
\text { Case iteration } & \text { do } e \text { is } \pi_{1} \rightarrow a_{1} \text { or } \ldots \text { or } \pi_{n} \rightarrow a_{n} \text { od }
\end{array}
$$

In these forms the $e$ is an expression, the $\pi_{i}$ are patterns, and the $a_{i}$ are processes.

A pattern is either a variable name ${ }^{1}$, a literal constant, a defined constant, a record or tuple of patterns, a free data constructor applied to a pattern, or the wildcard pattern ".". A pattern that contains literal constants or free data constructors is called a refutable pattern.

A case alternation evaluates the expression $e$, and matches the value against the patterns $\pi_{i}$. If any patterns match, then one of them ( $\pi_{m}$ say) is chosen and the corresponding process $a_{m}$ is executed. If no pattern is matched then the program aborts. Alternates may be separated by "else" rather than "or", in which case the patterns are matched in sequence.

If $I$ is the case iteration

$$
\text { do } e \text { is } \pi_{1} \rightarrow a_{1} \text { or } \ldots \text { or } \pi_{n} \rightarrow a_{n} \text { od }
$$

then $I$ is equivalent to

$$
\text { if } e \text { is } \pi_{1} \rightarrow a_{1} ; I \text { or } \ldots \text { or } \pi_{n} \rightarrow a_{n} ; I \text { or }{ }_{-} \rightarrow \text { skip } \mathrm{fi}
$$

When a case pattern contains variables then a successful match will result in those variables being bound to parts of the structure (value) being matched. The scope of such a binding is the rest of the pattern and the corresponding process.

The pattern [] matches an empty vector, while patterns of the form

$$
\left[\pi_{1}, \ldots, \pi_{n}\right]+\pi
$$

match vectors whose first $n$ elements match $\pi_{1}, \ldots \pi_{n}$, and whose remaining elements match $\pi$. Similarly,

$$
\pi+\left[\pi_{1}, \ldots, \pi_{n}\right]
$$

will match vectors whose last $n$ elements match $\pi_{1}, \ldots \pi_{n}$.
The pattern $\left\}\right.$ matches an empty set, while the patterns $\left\{v_{1}, \ldots, v_{n}\right\}+v s$ and $v s+\left\{v_{1}, \ldots, v_{n}\right\}$ (where the $v_{i}$, and $v s$ are variable names) match a set with at least $n$ elements, making an arbitrary choice of elements from the set to bind to the $v_{i}$ and binding the remaining elements of the set to $v s$.

[^1]```
Example 10 Destructively make a set from a vector
    set := \{\};
    DO vec IS [hd]+vec' -> set,vec := \{hd\}+set,vec' OD
Example 11 Destructively make a vector from a set
    vec := [];
    DO set IS \{hd\}+set' -> vec,set := vec+[hd],set' OD
```

Patterns may be associated with filter expressions - boolean-valued expressions which may contain variables bound in the pattern. Identical patterns may guard different branches of a case composition, providing their filters are distinct. ${ }^{2}$

Example 12 Calculate the number of positive and negative elements in a list

```
ps,ns := 0,0
DO list IS
Cons(hd, tl) | hd>0 -> list,ps := tl,ps+1
OR Cons(hd, tl) | hd<0 -> list,ns := tl,ns+1
OR Cons(hd, tl) | hd=0 -> list := tl
OD
```


### 2.2.6 Guarded Case Iteration

It can sometimes be helpful to terminate a case iteration early. To this end, if $G$ is a boolean expression the form

$$
\text { do } G \& E \text { is } \pi_{1} \rightarrow a_{1} \text { or } \ldots \text { or } \pi_{n} \rightarrow a_{n} \text { od }
$$

is defined to be equivalent to the following (where continue is a fresh variable which does not appear in $G, E$, the $\pi_{i}$ or the $a_{i}$ ):

```
let var continue \(=G\) in
    do continue \(\rightarrow\)
        if \(e\) is
            \(\pi_{1} \rightarrow a_{1} ;\) continue \(:=G\)
            or
            or \(\pi_{n} \rightarrow a_{n}\); continue \(:=G\)
            else \({ }_{-} \rightarrow\) continue \(:=\) false
            fi
        od
end
```

[^2]```
Example 13 Calculate the number of positive and negative elements in a list
    ps,ns := 0,0;
    DO list IS
        Cons(hd, tl) ->
        IF hd>0 -> list,ps := tl,ps+1
        OR hd<0 -> list,ns := tl,ns+1
        OR hd=O -> list := tl
        FI
    OD
```


### 2.2.7 Subtype Matching

A case pattern may consist of a variable annotated with a type, in which case the pattern will only match values of that exact type and its subtypes. This is the means by which a down cast (i.e. a cast from a type to one of its subtypes) is implemented. For example, suppose that the variables $n, m, b$ are respectively declared to be of types Num, MedNum, INT (see example 6), then the following case alternation is well-typed and never aborts. ${ }^{3}$


### 2.2.8 Specified Actions

## Not implemented in Version 1.

A specified action (henceforth spec) is a way of describing what one wishes to achieve without explaining how to achieve it. It takes the form:

$$
\bar{w}:[P, Q]
$$

where $\bar{w}$ is a list of variables, and $P, Q$ are predicates over the program state. This action will change the state of the process so that the predicate $Q$ becomes true, providing that the predicate $P$ is true. If $P$ is not true, then the action may do anything at all. The only variables that change are those named in $\bar{w}$. It is often convenient to be able to name the original values of the variables in the frame $(\bar{w})$. For any such variable $v$, the form ' $v$ (pronounced "original $v ")$ denotes its original value. There is, therefore, an implicit conjunct in the precondition of each spec, namely $\bar{w}={ }^{'} \bar{w}$.

[^3]Example 14 Increase the value of $x$ if it is negative, otherwise do anything.

$$
x:[x<0, x>' x]
$$

A spec is not executable, but it may be replaced by a spec that refines it, ${ }^{4}$ or by executable code that refines it, without changing the meaning of the context in which it appears.

Example 15 Two processes - each of which refines the spec of Example 14 $\mathrm{x}:=0$;
IF $x>=0$-> $x:=x-4$ OR $x<0$-> $x:=0$ FI

The spec $\bar{w}:[P, Q]$ is feasible if $\left(P \wedge \bar{w}={ }^{‘} \bar{w}\right) \Rightarrow \exists \bar{w} @ Q$. Infeasible specs are, of course, unimplementable and no refinement of an infeasible spec can be feasible.

Example 16 A feasible spec: choose an element of a nonempty set

$$
x:[S \neq \emptyset, x \in S]
$$

Feasible because

$$
S \neq \emptyset \wedge x=' x \Rightarrow \exists x @ x \in S
$$

### 2.2.9 Input

An input action takes the form

$$
p ? \pi \rightarrow a
$$

where $p$ is an input port, $\pi$ is a pattern (possibly type-annotated), and $a$ is a process. This action waits until there is input available from the port, then executes the process $a$ providing the input matches the pattern. If the input does not match the pattern, then the program aborts.

Ports are statically typed, and the purpose of a type-annotation in a pattern, if one appears, is to make explicit the type of value carried by the port.

When $\pi$ is a refutable pattern, the input action $p ? \pi \rightarrow a$ is equivalent to

$$
p ? v \rightarrow \text { if } v \text { is } \pi \rightarrow a \mathrm{fi}
$$

where $v$ is a variable which appears neither in $\pi$ nor $a$. So if a value that doesn't match the pattern is input from $p$ then the program will abort.

[^4]Example 17 An infeasible spec: choose an element of a set
$x:[$ true,$x \in S]$
Infeasible because
$x=' x \nRightarrow \exists x @ x \in S$

Example 18 Assign the next value input from the integer port left to v
left?(x:INT) $\rightarrow$ v:=x

### 2.2.10 Input Alternation

A process may wait for input on more than one port at once. An input alternation process takes the form

$$
\begin{aligned}
& \text { if } e_{1} \& p_{1} ? \pi_{1} \rightarrow a_{1} \\
& \text { or } e_{2} \& p_{2} ? \pi_{2} \rightarrow a_{2} \\
& \quad \ldots \\
& \text { or } e_{n} \& p_{n} ? \pi_{n} \rightarrow a_{n} \\
& \text { fi }
\end{aligned}
$$

where the $e_{i}$ are boolean expressions, known as guards, (which may be omitted if identically true), the $p_{i}$ are ports (not necessarily distinct), the $\pi_{i}$ are patterns, and the $a_{i}$ are processes. This process first evaluates all the boolean expressions, then waits until input is available on one of the ports corresponding to the true guards; an input from one such port is then matched against the pattern(s) corresponding to the port, and the processes corresponding to those it matches are considered eligible for execution. If one or more processes are eligible, then one of them is chosen for execution.

Example 20 Merge input from two ports
DO TRUE ->
IF left?x $\rightarrow$ output!x OR right?x $\rightarrow$ output!x FI
OD

Example 19 Abort unless TRUE is read from ack
ack?TRUE -> SKIP

```
Example 21 Interleave input from two ports
    l,r := TRUE,TRUE;
    DO l \/ r ->
    IF l & left?x -> l,r := FALSE,TRUE; output!x
    OR r & right?x -> l,r := TRUE,FALSE; output!x
    FI
    OD
```

A special port called timer has type ?int. This port may be read at any point in a program, and it is always ready to input an integer representing the current time in milliseconds. Such a port can be used with the after $n$ pattern, which will allow input of any integer representing a time later than $n$. For example, we may use the following to limit the time that a process waits for input on channel ichan before going on to do something else.

```
Example 22 Wait 20 seconds for an input, then give up.
    TIMER ? n ->
    IF TIMER ? AFTER n+20000 -> result:=GIVEUP
    OR ichan ? \(\mathrm{x} \quad->\) result:=x
    FI
```

A $p_{i} ? \pi_{i}$ combination may be replaced by a wildcard ("-"). If this is the case, and the corresponding guard yields true, then the wildcard is treated as if it were a ready input port with a matching pattern and the corresponding process is eligible for execution. The process in Example 23 copies an input item to the output if there is input available when it starts, and rushing is false. If rushing is true and no input is available, then NONE is send to the output; if rushing is true and input is available, then one of the outcomes above is chosen.

Example 23 Copy input to output, or send NONE to output
IF input?x $\rightarrow$ output!x
OR rushing \& _ $\quad$ - output! NONE
FI

An input alternation may separate its alternatives with "else" rather than "or". In this case, if more than one port is (or becomes) ready to communicate, then input is taken from the leftmost ready port. The pattern/filter combinations for that port are then matched against the input in the sequence in which they appear: if none succeeds then nothing more happens, otherwise the process corresponding to the first successful match is executed. ${ }^{5}$

```
Example 24 Input from left in preference to right
    IF left?x -> result:=x
    ELSE right?x -> result:=x
    FI
```

Example 25 Absorb all input until a control signal appears
DO absorb ->
IF control?_ -> absorb:=FALSE
ELSE input?x -> SKIP
FI
OD
Example 26 Count the number of odd and even numbers on a port
DO TRUE ->
IF input?x | odd $\mathrm{x} \rightarrow$ odds :=odds +1
OR input?x | even x -> evens:=evens+1
FI
OD

### 2.2.11 Distributed Alternation

If $G(i)$ is an input guard in which the name $i$ appears, $P(i)$ is a process in which the name $i$ appears, and $E$ is a set or vector containing elements $E_{1}, \ldots E_{n}$ then the form

$$
\text { or }(\text { for } i \text { in } E) G(i) \rightarrow P(i)
$$

means

$$
G\left(E_{1}\right) \rightarrow P\left(E_{1}\right) \text { or } \ldots \text { or } G\left(E_{n}\right) \rightarrow P\left(E_{n}\right)
$$

when it appears within an input alternation. Similarly,

$$
\text { else }(\text { for } i \text { in } E) G(i) \rightarrow P(i)
$$

can be used to mean

$$
G\left(E_{1}\right) \rightarrow P\left(E_{1}\right) \text { else } \ldots \text { else } G\left(E_{n}\right) \rightarrow P\left(E_{n}\right)
$$

[^5]```
Example 27 Same as example 26
    DO TRUE ->
        IF input?x -> IF odd \(x\)-> odds :=odds +1
                                OR even \(x\)-> evens:=evens +1
                        FI
        FI
    OD
```

Example 28 Same as example 26
DO TRUE ->
IF input?x -> IF odd $x$-> odds :=odds +1
ELSE TRUE -> evens:=evens+1
FI
FI
OD

### 2.2.12 Iterated Alternation

It is frequently desirable to execute an input alternation repeatedly whilst one of its guards is enabled. The form on the left below provides a convenient syntactic sugar for the common idiom on the right.

$$
\begin{array}{lr}
\text { do } e_{1} \& p_{1} ? \pi_{1} \rightarrow a_{1} & \text { do } e_{1} \vee e_{2} \vee \ldots \vee e_{n} \rightarrow \\
\text { or } e_{2} \& p_{2} ? \pi_{2} \rightarrow a_{2} & \text { if } e_{1} \& p_{1} ? \pi_{1} \rightarrow a_{1} \\
& \ldots \\
\text { or } e_{n} \& p_{n} ? \pi_{n} \rightarrow a_{n} & \ldots p_{2} ? \pi_{2} \rightarrow a_{2} \\
\text { od } & \text { or } e_{n} \& p_{n} ? \pi_{n} \rightarrow a_{n} \\
& \text { od }
\end{array}
$$

Example 29 Merge input(0), ..., input(9)
DO OR (FOR i IN O\#10) input(i)?x -> out!x OD

### 2.2.13 Parallel Composition

The parallel composition of processes $p_{1}, \ldots, p_{n}$ takes the form

$$
p_{1}\left\|p_{2}\right\| \ldots \| p_{n}
$$

The component processes are started at the same time, and the composite process terminates when all its components have terminated.

```
Example 30 Merge input(0), ..., input(9) until control signals Stop
    DO
    go \& control?Stop -> go:=FALSE
    OR
        OR (FOR i IN 0\#10) go \& input(i)?x -> out!x
    OD
```

Example 31 Parallel computation of three function values $a:=f(a)| | b:=f(b)| | c:=f(c)$

A variable (or component of an array) that is assigned to in one of the components of a parallel composition must not appear in any of the other components.

Example 32 An improper use of variables in a parallel composition

$$
x:=2 ;
$$

BEGIN $\mathrm{x}:=3$ || $\mathrm{y}:=\mathrm{x}$ END
-- At this point the value of y may be 2 or 3 !

### 2.2.14 Distributed Parallel Composition

If $P(i)$ is a process in which the name $i$ appears, and $E$ is a set or vector containing elements $E_{1}, \ldots E_{n}$ then the form

$$
\|(\text { for } i \text { in } E) \quad P(i)
$$

means

$$
P\left(E_{1}\right)\|\ldots\| P\left(E_{n}\right)
$$

### 2.2.15 Variable and Constant Declarations

New variables and constants are introduced by declarations at the head of a block that takes the form

$$
\text { let } \Delta_{1} \Delta_{2} \ldots \Delta_{m} \text { in } p \text { end }
$$

Where $p$ is a process - which is known as the body of the block - and each $\Delta_{i}$ takes one of the forms

> var name:Type $=$ Expression
> con name:Type $=$ Expression
> def name:Type $=$ Expression

Example 33 Parallel computation of $n$ then of $2 n$ function values
|| (FOR i IN O\#n) result(i):=f(i);
|| (FOR i IN O\#n) result(i):=f(i)
11
|| (FOR i IN n\#n) result(i):=f(i)

The expression - whose type must be consistent with the declared type ${ }^{6}$ - is evaluated, and in the con or def form is associated directly with the name. The :Type may be omitted, in which case it is taken to be the type of Expression. The expression may be omitted in a variable declaration, in which case the type must be given.

In the var form the value is stored in a memory location that is associated with the name, and subsequent assignments may change the value stored in that location. The special expression any may be used in this form (and this form only) - in which case an unspecified element of the appropriate type is used as the value.

The expression in the con form is evaluated at run-time, when the corresponding block of code is executed. Note that the name will not be treated as a constant in patterns; for example, in example 34 the pattern-matching on the input will always succeed and $n$ will take the input value in $p(n)$. A name that is to be

```
Example 34 Run-time constant declaration
    LET CON n = O IN
        ichan?n -> p(n)
    END
```

used as a constant pattern must be declared as a compile-time constant, using the def form. In example 35 , only a 0 may be input and hence $p(n)$ will always be $p(0)$. The scope of the association between the name and value (or location)

```
Example 35 Compile-time constant declaration
    LET DEF \(\mathrm{n}=0 \mathrm{IN}\)
        ichan?n \(\rightarrow p(n)\)
    END
```

that is established by a declaration is the text of subsequent declarations in the block, and the text of the block's body. The usual scope rules for nested blocks apply: an association for a name $i$ established in an outer block $b$ is superseded by an association for $i$ established in a block nested within $b$.

[^6]Note however that processes which are the operands of (\|) or fork cannot use variables which were declared in an enclosing block - this is to prevent synchronisation problems of shared variables. This hiding is easy to get around by declaring a constant with the same name, and using that within the inner processes.

```
Example 36 Declarations, a legal and an illegal assignment
    LET
        CON thirtyfour: INT = 34 -- Constant declaration
        VAR forty: INT = 40 -- Variable declaration
    IN
        forty := 34; -- This assignment is legal
        thirtyfour := 34 -- This assignment is illegal
    END
```


### 2.2.16 Channels

A channel implements point to point communication between two parallel processes by providing an output port for one of the processes and an input port for the other. A unidirectional channel name suitable for communicating values of type Type is constructed by the declaration

## chan name:Type

Such a channel is used to connect a process that writes to its !Type port to a process that reads from its ?Type port

The composite parallel process in Example 37 implements a one-place buffer, whose producer client writes to it using left!data and whose consumer client reads from it using right?data. The middle channel implements an output port for the left parallel component and an input port for the right component.

Example 37 A one-place buffer process
LET CHAN middle:INT IN DO left?x $->$ middle!x $O D$ || DO middle?y $->$ right!y OD END

A composite channel may be used to connect two composite ports. Because the constituent ports in a composite might not all communicate in the same direction, the declaration of a composite port must indicate this. The declaration

```
channels name:PType
```

where PType is a (possibly composite) port type produces a channel whose two ends have type PType and -PType.

Example 38 shows a simple process farm built by parallel composition. The top process accepts raw data from its left:?RAW port if either of the worker processes are free, then it immediately transmits it to a free worker. It will accept cooked data back from a worker it believes is busy and transmit it to the right:!CKD port.

```
Example 38 Simple process farm using ports left:?RAW, right: !CKD
    LET
        VAR free = (TRUE, TRUE)
        CHANNELS to : (!RAW, !RAW)
        CHANNELS from : (?CKD, ?CKD)
    IN
            DO free.1\/free.2 & left?x -> -- Farmer
                    IF free.1 -> free.1:=FALSE; to.1!x
                    OR free.2 -> free.2:=FALSE; to.2!x
                    FI
                OR ~free.1 & from.1?y -> free.1:=TRUE; right!y
                OR ~free.2 & from.2?y -> free.2:=TRUE; right!y
                OD
        || DO to.1?x -> from.1!cook(x) OD -- Worker 1
        || DO to.2?x -> from.2!cook(x) OD -- Worker 2
    END
```


### 2.3 Procedures and Process Families

The two worker processes in Example 38 have the same structure, but use different input and output ports. This common structure can be made explicit by defining a named family of processes with the same structure, using a declaration of the form

$$
\text { proc } \operatorname{name}\left(\Phi_{1}, \ldots, \Phi_{m}\right) \text { is } p
$$

where $p$ is a process, and each $\Phi_{i}$ is a value parameter declaration of the form name:Type. The type of the resulting process is written

$$
\left(T_{1}, \ldots, T_{n}\right) \rightarrow()
$$

where $T_{i}$ is the type of the $i^{\text {th }}$ parameter. (The () indicates that a call to this procedure yeilds no result value.)

An instance of the family is built (and started) using the notation

$$
\operatorname{name}\left(E_{1}, \ldots, E_{m}\right)
$$

Each $E_{i}$ must be a value of the specified type, or one that implements the specified type. ${ }^{7}$

In Example 39 we present a generalisation of the process farm, with the roles of farmer and workers being played by instances (invocations) of process families. Here Farm, farmer, and worker are families of processes.

```
Example 39 The process farm revisited
    PROC worker (in:?RAW, out:!CKD) IS
        DO in?x -> out!cook(x) OD
    PROC farmer(in:?RAW, to:(!RAW,!RAW), from:(?CKD,?CKD), out:!CKD) IS
        LET
            VAR free \(=(\) TRUE, TRUE)
        IN
            DO free. \(1 \backslash /\) free. 2 \& in?x \(->\) IF free. 1 -> free. \(1:=F A L S E ;\) to. \(1!\mathrm{x}\)
                                    OR free. 2 -> free. \(2:=\) FALSE; to. 2 ! x
                                    FI
            OR ~free. 1 \& from.1?y \(\rightarrow\) free. 1:=TRUE; out!y
            OR ~free. 2 \& from.2?y \(\rightarrow\) free. \(2:=\) TRUE; out!y
            OD
        END
    PROC Farm(in:?RAW, out:!CKD) IS
        LET
            CHANNELS to : (!RAW, !RAW)
            CHANNELS from : (?CKD, ?CKD)
        IN
            farmer (in, to, from, out)
            || worker(to.1, from.1)
            || worker(to.2, from.2)
        END
```

Both the farmer and the worker processes defined in Example 39 can be used in other settings, and it is worthwhile considering whether the Farm process can itself be restructured so as to support re-use. Happily it can, and the result is shown in Example 40.

The type definitions in Example 40 associate names Farmer and Worker with process types. The declaration of GenFarm organizes its parameters systematically into two groups: the left hand group describes its value parameters (in this case they have process types), and the right hand group describes its port parameters. To create a member of such a process family, connect it to its environment and start it, all its parameters must be provided.
For example, a replica of the process farm of Example 38 could be created and started using the notation

[^7]```
Example 40 A generic process farm
    TYPE Farmer = (?RAW, (!RAW,!RAW), (?CKD,?CKD), !CKD) -> ()
    TYPE Worker = (?RAW, !CKD) -> ()
    PROC GenFarm(farmer:Farmer, worker:Worker, in:?RAW, out:!CKD) IS
        LET
            CHANNELS to : (!RAW, !RAW)
            CHANNELS from : (?CKD, ?CKD)
        IN farmer(in, to, from, out)
            || worker(to.1, from.1)
            || worker(to.2, from.2)
        END
```

            GenFarm(Farmer, Worker, left, right)
    To refine (or specialize) a process family it is only necessary to provide an initial subtuple of its parameters. Example 41 shows how to name specialized variants of a process family. Each family defined there takes its input from a port of type ? RAW and sends its output to a port of type !CKD - the families have (respectively) up to twice, four times and eight times the capacity of a single worker.

```
Example 41 Process families defined by specialization
    CON TwoWorkers: Worker = GenFarm(Farmer, Worker)
    CON FourWorkers: Worker = GenFarm(Farmer, TwoWorkers)
    CON EightWorkers: Worker = GenFarm(Farmer, FourWorkers)
```

When the remaining parameters of a refined (or specialized) process family are provided, a member of the family is created and started. For example, on a computer system with enough processors, a farm with (up to) four times the capacity of that in Example 38 can be created and started using the notation

```
EightWorkers(left, right)
```


### 2.3.1 Composite Channel Structures

Examples 42 and 43 show two ways of building a variadic process farm that uses composite channel structures to implement port types.

In Example 42 we define the interface to a worker as a pair of ports. A farmer is given a vector of raw output ports to write to, and a vector of cooked input ports to read from. It is assumed that these vectors are of the same size.

In Example 43 we define the interface to a worker as a port type Window - a worker reads raw material from the raw port of a window, and writes cooked

```
Example 42 A variadic process farm
    TYPE Farmer = (?RAW, [!RAW], [?CKD], !CKD) -> ()
    TYPE Worker = (?RAW, !CKD) -> ()
    PROC GenFarm (size:INT, farmer:Farmer, worker:Worker,
                in:?RAW, out:!CKD) IS
        LET
            CHANNELS raw : [RAW]#size
            CHANNELS ckd : [CKD]#size
        IN
            farmer(in, raw, ckd, out)
            ||
                ||(FOR i IN O#size) worker(raw i, ckd i)
        END
    PROC farmer(in:?RAW, raw:[!RAW], ckd:[?CKD], out:!CKD) IS
        LET VAR free = [(FOR i IN O#size) TRUE]
        IN
            DO
            OR (FOR i IN O#size)
                    ~free(i) & ckd(i)?y -> free(i):=TRUE; out!y
            OR
                    OR (FOR i IN O#size)
                        free(i) & in?x -> free(i):=FALSE; raw(i)!x
            OD
        END
```

material to the ckd port of the same window. A farmer is given a vector of window complements: it writes raw material to their raw ports, and reads cooked material from their ckd ports.

### 2.3.2 Procedures with results

So far we have seen only families of processes that communicate with their environment by means of channels, and which never terminate.

Most ordinary sequential programming languages also provide support for families of sequential processes called procedures, and eCSP is no exception. A procedure is simply a process family whose members are intended to terminate.

Example 44 shows a procedure that calculates the GCD of its two integer arguments, and assigns the result to the variable gcdanswer.

```
Example 43 The variadic process farm revisited
    TYPE Window = \{| raw:?RAW, ckd:!CKD |\}
    TYPE Farmer = (Window, [-Window]) -> ()
    TYPE Worker \(=\) (Window) -> ()
    PROC worker(env: Window) IS
        DO env.raw? -> env.ckd!cook(x) OD
    PROC GenFarm (size:INT, farmer:Farmer, worker:Worker, env:Window) IS
        LET CHANNELS chans : [ \{|raw=CHAN RAW, ckd=CHAN CKD|\}]\#size
        IN
            farmer(env, chans)
            11
                    ||(FOR i IN O\#size) worker(chans(i))
        END
    PROC farmer (env: Window, chans:[-Window]) IS
        LET VAR free = [(FOR i IN O\#chans) TRUE] IN
            DO
                OR (FOR i IN O\#\#chans)
                    free(i) \& chans(i).ckd?y -> free(i):=TRUE; env.ckd!y
            OR
                OR (FOR i IN O\#\#chans)
                        free(i) \& env.raw? \(\quad\)-> free(i):=FALSE; chans(i).raw!x
        OD
        End
```

The effect of the process $\operatorname{gcd}\left(e_{1}, e_{2}\right)$ is the same as the effect of the process

```
LET
    VAR m:INT= }=\mp@subsup{e}{1}{
    VAR n:INT= }\mp@subsup{e}{2}{
IN
    DO m<n -> n:=n-m OR m>n -> m:=m-n OD;
    gcdanswer := m
END
```

In other words, the body of the procedure is executed in an environment in which its formal parameter names are associated with variables which are initialised to the values of its actual parameters.

The experienced reader will no doubt be grumbling that it is not very satisfactory for a procedure to communicate its result by assigning to a global variable in this way. In this she would be in line with our own thinking, for firstly, the relationship between the procedure name and the variable in which the answer is placed is not made explicit at the site of the call, and secondly the definition of recursive procedures is made more complicated.

```
Example 44 A GCD Procedure
    VAR gcdanswer: INT
    PROC gcd(m:INT, n:INT) IS
        BEGIN
        DO m<n -> n:=n-m OR m>n -> m:=m-n OD;
        gcdanswer := m
    END
```

The problem is resolved by a form of procedure definition and invocation in which the variable into which the result will be placed can be named explicitly. In example 45 we present a revised version of the procedure definition, in which a "result parameter" is named explicitly.

```
Example 45 A GCD Procedure with a result parameter
    PROC gcdanswer:INT := gcd(m:INT, n:INT) IS
    BEGIN
        DO m<n -> n:=n-m OR m>n -> m:=m-n OD;
        gcdanswer := m
    END
```

The GCD procedure is invoked using the notation variable $:=\operatorname{gcd}\left(e_{1}, e_{2}\right)$ and the effect of this is the same as the effect of the process

```
LET
    VAR m:INT=e 
    VAR n:INT=e 
    VAR gcdanswer:INT IN
        DO m<n -> n:=n-m OR m>n -> m:=m-n OD;
        gcdanswer := m;
    variable := gcdanswer
END
```

Those familiar with the academic literature on programming languages will recognise that the semantics of this form of parameter passing is that known as "call by result". The definition and invocation notations have the advantage that a simple inspection of the call site demonstrates that a variable can be altered by a procedure call, and a simple inspection of the signature of the procedure demonstrates that it has result parameters as well as value parameters. Furthermore there is no need to introduce words describing the modes in which parameters are passed. ${ }^{8}$

Procedures may have multiple result parameters, as in example 46

[^8]```
Example 46 A Procedure with two result parameters
    PROC min:INT, max:INT := order(left:INT, right:INT) IS
    IF left>=right -> max,min := left,right
        ELSE TRUE \(\quad->\) max,min \(:=\) right,left
        FI
```

The names of one or more value parameters may also appear as result parameters, as in example 47. In such cases, we have the mode of parameter passing known in the literature as "call by value-result".

```
Example 47 A Procedure with two value-result parameters
    PROC left:INT, right:INT := reorder(left:INT, right:INT) IS
    IF left>right -> left,right := right,left
    ELSE TRUE -> SKIP
    FI
```

When a procedure with value-result parameters is invoked, the actual parameters in the corresponding value and result positions must be identical variables. For example, the reorder procedure is invoked using the notation

$$
v_{1}, v_{2}:=\operatorname{reorder}\left(v_{1}, v_{2}\right)
$$

and the effect of this is the same as the effect of the following process - in which left, and right are variables distinct from $v_{1}$ and $v_{2}$.

```
LET
    VAR left: INT = v
    VAR \overline{right}:INT = v
IN
    IF left>right -> left,right := right,left
    ELSE TRUE -> SKIP
    FI;
    v1,v2 := left,right
END
```

We denote the type of this process as

$$
(\text { int }, \text { int }) \rightarrow(\text { int }, \text { int })
$$

where the tuple on the left of the arrow represents the value parameters and the tuple on the right represents the result parameters.

A procedure with a result parameter may be invoked in a context where an expression is expected. In this case the effect is the same as if a new variable had been declared and used as an output parameter before being substituted for the procedure invocation. For example

```
.... print(gcd (39,45)) ....
```

is equivalent to

```
LET VAR v:INT IN
    v := gcd(39,45);
    .... print(v) ....
```

END

If more than one procedure invocation appears in a single expression, then the order in which the procedures are invoked is not specified. For example

```
.... print(gcd (39,45)+gcd (45,98)) ...
```

is equivalent to one of the following

```
LET
    VAR v:INT
    VAR w:INT
IN
    v := gcd(39,45);
    w := gcd(45,98);
    .... print(v+w) ...
END
LET
    VAR v:INT
    VAR w:INT
IN
        w := gcd(45,98);
        v := gcd(39,45);
        .... print(v+w) ....
END
```

Likewise, a procedure with a result parameter may be invoked as part of a variable declaration: for example

```
LET
    VAR v = gcd(39,45)
    VAR w = gcd(45,98)
IN
    .... print(v+w)....
END
```

is equivalent to

```
LET VAR v:INT
IN
    v := gcd(39,45);
    LET VAR w:INT
    IN
        w := gcd(45,98);
        .... print(v+w) ....
    END
END
```

The use of such procedures in constant declarations is also permitted, in which case the effect is the same as if new variables were declared and initialised, then new constants declared with the same values. For example

```
LET
    CON v = gcd(39, 45)
    CON w = gcd(45, 98)
IN
    .... print(v+w) ....
END
```

is equivalent to

```
LET VAR v:INT IN
    v := gcd(39, 45);
    LET VAR w:INT IN
        LET CON v=v, w=wi IN
            w := gcd(45, 98);
            .... print(v+w) ....
        END
    END
END
```


### 2.4 Sharing Resources

### 2.4.1 Static Communication Structures

Many systems are organised along client/server lines - where a server offers a resource to several clients. Whilst it is possible to model this kind of system in the language introduced so far, one of the constraints on such models is that they are static.

For example, in Example 48 we present a system composed of a token-granting server and 42 token-requesting clients. A client can ask for as many tokens as it wishes, and the server hands out a token to a client whenever one is requested. Each client's interface to the token-granting service is described by the port type TokenService, defined as

```
{| ask:!(), answer:?INT |}
```

and the server's interface to each of its clients is described by the complementary port type -TokenService, defined as
\{| ask:?(), answer:!INT |\}

We describe the system as static because the server is equipped in advance with communication channels to and from all its potential clients, and the clients are all started at the same time as the server.

```
Example 48 A Static Client/Server System
    TYPE TokenService = {| ask:!(), answer:?INT |}
    PROC Server(clients: [-TokenService]) IS
        LET VAR counter = 0 IN
            DO
                    OR (FOR i IN O##clients)
                        clients(i).ask?() ->
                        clients(i).answer!counter;
                        counter:=counter+1
            OD
        END
    PROC Client(server: TokenService) IS
        LET VAR token:INT IN
            ...
            server.ask!();
            server.answer?n -> token := n;
            ...
        END
    -- The system
    LET
        CHANNELS chans : [TokenService]#42
    IN
        Server(chans) || ||(FOR i IN 0##chans) Client(chans(i))
    END
```


### 2.4.2 Dynamic Communication Structures

Although there are many inherent strengths in organising a system statically there are a couple of weaknesses. The first weakness is that there are as many
channels as there are potential clients, even though only one client can be serviced at a time. The second weakness is that the server and all its clients must be started simultaneously - there is no way of starting a new client when it becomes necessary to do so, and terminating it when it has served its purpose. The third weakness is that there is an absolute upper bound on the number of clients that can ever be offered service.

We need something a little more flexible than this in order to describe the way in which a server that doesn't know about all its clients in advance can offer services to them. The mechanism that is behind our solution is the shared channel structure. The declaration
shared chan name:Type
creates a shared channel whose port ends have type shared ?Type and shared !Type. These ports may be used by any number of processes - though only one inputting and one outputting process may communicate through the channel at a time. Shared composite channels also may be declared; for example

```
SHARED CHANNELS c: {| ask: SHARED ?(),
    answer: SHARED !INT
    1}
```

constructs a shared channel structure $c$ with a unit channel called ask and an integer channel called answer.

Just as there are two ports associated with every channel (the input port and the output port), there are two interfaces to every shared channel: ${ }^{9}$ the server interface and the client interface. Every time a client needs to use a shared channel for communication with a server it must ensure that no other process is using it as a client by waiting until it can become the owner of the client interface to the channel. Once the communication has finished the client must renounce ownership of the channel. This is accomplished by a process of the form
client $n$ in communications with server end
where $n$ is the name of the shared channel or one of its ports.
Likewise, whenever a server uses a shared channel for communicating with a client it must wait until it can become the exclusive owner of the server interface to the channel, then give up ownership when communication with the client has finished:

$$
\text { server } n \text { in communications with client end }
$$

For example, within the scope of the declarations

```
TYPE SineService = {| input:!REAL, output:?REAL |}
SHARED CHANNELS sine : SineService
```

[^9]the client interface to the shared channel is claimed, used and then renounced by the process

```
CLIENT sine IN
    sine.input!34; sine.output?n -> ...
END
```

It will be delayed until the shared channel structure is free, after which it communicates using the given ports before once again freeing the channel structure for re-use.

Within the scope of the same declarations, the server interface is claimed, used, and then renounced by a granting process

```
SERVER sine IN
    sine.input?n -> sine.output!SINE(n)
END
```

The granting process is synchronised with the claiming process at the point at which the bodies of the processes begin, and the termination of the bodies of the granting and claiming processes is also synchronised.

In example 49 we present a revised version of a server offering the same functionality as example 48 , but which expects to offer its services to clients that it doesn't know about in advance. The body of a corresponding client is shown in example 50. The synchronization between client.ask?() and server.ask! () in example 48 is no longer necessary, since SERVER client in the server and CLIENT server in the client synchronise with each other.

```
Example 49 A Dynamic Server
    TYPE TokenService = ?INT
    PROC Server(client: SHARED -TokenService) IS
        LET VAR counter = O IN
            DO
                    SERVER client IN
                        client!counter;
                    counter:=counter+1
            END
                OD
    END
```

A token service is set up and offered by declaring a shared channel and running the server in parallel with the clients.

```
Example 50 A Client for the Dynamic Server
    PROC Client(server: SHARED TokenService) IS
        LET VAR token: INT IN
            ..
            CLIENT server IN
                server?n -> token:=n
            END
                ...
            END
    LET SHARED CHANNELS tokenservice : TokenService IN
        Server(tokenservice)
        |
            ||(FOR i IN 1..42) Client(tokenservice)
    END
```

Although one might usually expect to find many clients meeting a single server at a shared channel, in fact it can act as a meeting-place for any number of clients and any number of servers, as in example 51.

```
Example 51 Three clients using two servers
    LET SHARED CHANNELS service : Interface IN
        ServerA(service)
        || ServerB(service)
        || ClientX(service)
        || ClientY(service)
        || ClientZ(service)
    END
```


### 2.4.3 Alternation and Iteration of Granting Processes

If $c_{1}, \ldots c_{n}$ are shared port structures, then a process may use them as part of a server alternation or iteration

A server alternation takes the form

```
if e}\mp@subsup{e}{1}{&}\mathrm{ server c}\mp@subsup{c}{1}{}\mathrm{ in }\mp@subsup{a}{1}{}\mathrm{ end
or }\mp@subsup{e}{2}{&}\mathrm{ & server c}\mp@subsup{c}{2}{}\mathrm{ in }\mp@subsup{a}{2}{}\mathrm{ end
or ..
or }\mp@subsup{e}{n}{}& server con in an end
fi
```

where the $e_{i}$ are boolean expressions, known as guards, (which may be omitted if identically true), and the $a_{i}$ are processes. Such a process first evaluates all the guards, then waits until a client claim is made for at least one of the shared channels corresponding to the true guards - at which point one of the claims is granted.

A server iteration takes a similar form

```
do }\mp@subsup{e}{1}{&& server c}\mp@subsup{c}{1}{}\mathrm{ in }\mp@subsup{a}{1}{}\mathrm{ end
or }\mp@subsup{e}{2}{&& server c}\mp@subsup{c}{2}{}\mathrm{ in }\mp@subsup{a}{2}{}\mathrm{ end
or ...
or }\mp@subsup{e}{n}{}& server con in and en
od
```

It is equivalent to

```
do }\mp@subsup{e}{1}{}\vee\mp@subsup{e}{2}{}\vee\cdots\vee\mp@subsup{e}{n}{}
    if e}\mp@subsup{e}{1}{&}\mathrm{ server c}\mp@subsup{c}{1}{}\mathrm{ in }\mp@subsup{a}{1}{}\mathrm{ end
    or }\mp@subsup{e}{2}{&}\mathrm{ & server c}\mp@subsup{c}{2}{}\mathrm{ in }\mp@subsup{a}{2}{}\mathrm{ end
    or...
    or }\mp@subsup{e}{n}{}& server con in and end
    fi
od
```


### 2.4.4 Dynamic Processes

A shortcoming of the arrangement in example 51 is that the processes must be completely specified at compile time. An alternative scheme is to create processes dynamically as they are needed. This is done using the fork construct.
If $p$ is a process of type $t \rightarrow()$ and $(v)$ has type $t$, then fork $p(v)$ invokes $p(v)$ as a separate process (we call this a child process) that runs concurrently with the process that invoked it (the parent process). Note that if the child process dies, the parent will continue to run; but if the parent process dies all its children will also stop running.

Example 52 shows a process farmer which creates a new server process each time a request comes on the req channel from one of the client processes.

### 2.5 Syntactic Sugar

In this section we outline some convenient notational features of eCSP whose meanings are defined in terms of the core language. The term "syntactic sugar"

```
Example 52 Dynamic server creation
    PROC client (req: SHARED !(), service: SHARED Interface) IS
    END;
    PROC server (service: SHARED -Interface) IS
    END;
    PROC farmer (req: SHARED ?(), service: SHARED -Interface) IS
        DO
            SERVER req IN req?() -> FORK server(service) END
        OD
    LET
        SHARED CHANNELS service: Interface;
        SHARED CHANNELS request: ?()
    IN
        client (request, service)
        || client (request, service)
        || farmer (request, service)
    END
```

is due to Christopher Strachey and describes convenient high-level notations whose meanings are defineable in terms of core language features - the idea is that "syntactic sugar" can render "semantic spice" more palatable.

### 2.5.1 Strings

Strings are vectors of characters, and type STRING is a built-in synonym for [CHAR]. Literal strings can be denoted using the usual square bracket notation for vectors, or by delimiting the string with double quotes. The two forms are interchangeable:

$$
\begin{aligned}
\text { "Hello, world!" } & \equiv[' H ', ' e ', ' l ', ' l ', ' o ', ', ', w ', ' o ', ' r ', ' l ', ' d ', '!'] ~ \\
" " ~ & \equiv
\end{aligned}
$$

### 2.5.2 Disjunctive Patterns

When the same action is associated with more than one guard/pattern in an alternation it is a tedious and error-prone task to write out the action repeatedly.
A multiple pattern of the form

$$
G \& \pi_{1} \text { or } \pi_{2} \text { or } \ldots \text { or } \pi_{n} \rightarrow a
$$

may appear in an iteration or alternation. It is equivalent to

$$
G \& \pi_{1} \rightarrow a \text { or } G \& \pi_{2} \rightarrow a \text { or } \ldots \text { or } G \& \pi_{n} \rightarrow a
$$

The patterns in such a construct must not contain variable names, hence they will not bind any new values. They may however contain wildcard (_) patterns.

Similarly,

$$
G \& c ? \pi_{1} \text { or } \pi_{2} \text { or } \ldots \text { or } \pi_{n} \rightarrow a
$$

is equivalent to

$$
G \& c ? \pi_{1} \rightarrow a \text { or } G \& c ? \pi_{2} \rightarrow a \text { or } \ldots \text { or } G \& c ? \pi_{n} \rightarrow a
$$

## Example 53 A disjunctive pattern

IF
input ? Yes OR Maybe -> GoAhead()
OR
input ? No -> Retreat()
FI

### 2.5.3 Bounded Iteration

If $E:[T]$ is a vector, $G$ is a boolean expression (which may be omitted, if identically true, together with the $\&$ ), and $P$ is a process, then the form

$$
\text { do } G \&(\text { for } i \operatorname{in} E) \rightarrow P \text { od }
$$

means "While $G$ is true, execute $P$ with $i$ bound to successive elements of $E$." More formally, it can be translated into the following (where $v^{\prime}, v^{\prime \prime}$ are fresh variables which do not appear in $G, i, P)$ :

$$
\text { let var } v^{\prime}:[T]=E \text { in do } G \& v^{\prime} \text { is }[i]+v^{\prime \prime} \rightarrow P ; v^{\prime}:=v^{\prime \prime} \text { od end }
$$

Similarly if $E:\{T\}$ is a set then the form

$$
\text { do } G \&(\text { for } i \operatorname{in} E) \rightarrow P \text { od }
$$

means "Choosing each element of $E$ at most once, and while $G$ is true, bind $i$ to the chosen element and execute $P$." More formally, it can be translated into

$$
\text { let var } v^{\prime}:\{T\}=E \text { in do } G \& v^{\prime} \text { is }\{i\}+v^{\prime \prime} \rightarrow P ; v^{\prime}:=v^{\prime \prime} \text { od end }
$$

### 2.5.4 "Bidirectional" Ports and Channels

## Not implemented in Version 1.

When a process communicates with a peer process via an input and an output port, it can be useful to give both ports the same name, rather than having to invent two names.

If $T_{1}, T_{2}$ are types, then $? T_{1}!T_{2}$ denotes the port tuple type $\left(? T_{1},!T_{2}\right)$, and $!T_{1} ? T_{2}$ denotes its complement tuple type $\left(!T_{1}, ? T_{2}\right)$. If $c: ? T_{1}!T_{2}$ then the action $c .1 ? x \rightarrow a$ may be abbreviated to $c ? x \rightarrow a$, and the action $c .2!v$ may be abbreviated to $c!v$; likewise if $c:!T_{1} ? T_{2}$ then $c .1!v$ is abbreviated to $c!v$ and $c .2 ? x \rightarrow a$ to $c ? x \rightarrow a$. The pair of channels that implement the requisite ports and their connections may be created by either of the delcarations channels $n: ? T_{1}!T_{2}$, channels $n:!T_{1} ? T_{2}$.

### 2.5.5 Remote Procedure Call

## Not implemented in Version 1.

The shared channel machinery is a relatively low-level mechanism. Typically it will be used for providing a service to any of a number of client processes. With this in mind we introduce a slightly more memorable notation.

The shared channel is declared as a remote procedure - perhaps with some result parameters.

$$
\text { shared proc } R T_{1}, \ldots, R T_{n}:=\operatorname{name}\left(V T_{1}, \ldots, V T_{m}\right)
$$

This means

$$
\text { shared channels name }:\left(?\left(R T_{1}, \ldots, R T_{n}\right),!\left(V T_{1}, \ldots, V T_{m}\right)\right)
$$

A server process grants the channel with a server process:

$$
\begin{aligned}
& \text { server } r_{1}: R T_{1}, \ldots r_{n}: R T_{n}:=\operatorname{name}\left(v_{1}: T_{1}, \ldots v_{m}: T_{m}\right) \text { in } \\
& \quad \text { body } \\
& \text { end }
\end{aligned}
$$

This means
server name in

$$
\text { name. } 2 ?\left(v_{1}, \ldots, v_{m}\right) \rightarrow
$$

let var $r_{1}: R T_{1}, \ldots, r_{m}: R T_{n}$ in body name.1! $\left(r_{1}, \ldots, r_{n}\right)$
end
end

The channel is claimed using a syntax that is no different from that of an ordinary procedure call:

$$
a r_{1}, \ldots, a r_{n}:=\operatorname{name}\left(e_{1}, \ldots, e_{m}\right)
$$

In the given context, this means

```
client name in
    name.2! \(\left(e_{1}, \ldots, e_{m}\right)\);
    name.1? \(\left(v_{1}, \ldots v_{n}\right) \rightarrow a r_{1}:=v_{1} ; \ldots ; a r_{n}:=v_{n}\)
end
```

In example 58 (on page 42) we present part of an alternative implementation of the sine computation service presented earlier.

## 3 The Module Language

### 3.1 Modules and Interfaces

The simplest forms of module provide a way of packaging a data structure with a particular behaviour whilst hiding its implementation. The declaration in example 54 declares a module type, known as Tokens, which exports the type Token, the constant limit, and the procedures newToken and freeToken, while forbidding any process using these procedures to take advantage of the knowledge that Token is implemented as INT.

```
Example 54 A module that hides its implementation
    MODULE Tokens IMPLEMENTS
        TYPE Token
        CON limit: INT
        PROC Token := newToken()
        PROC freeToken(Token)
    WITH
        TYPE Token = INT
        CON limit \(=42\)
        VAR unused : [BOOL] \(=\) [(FOR i IN O\#limit) TRUE]
        PROC tok:Token := newToken() IS
            LET VAR search = TRUE IN
                DO search \& (FOR i IN O\#limit) ->
                IF unused(i) -> unused(i), tok, search := FALSE,i,FALSE FI
            OD
            END
        PROC freeToken(tok:Token) IS
            unused(tok) := TRUE
    END
```

The set of exported types and values is called the module's interface. It can be declared independently of the module declaration, thus allowing more than one module to implement an interface. Example 55 shows the same interface as before, but with different implementations based on different Token types.
In some cases it is advantageous to parameterise modules or interfaces by types and/or values. In example 56 we define a parameterised interface Atom describing modules that administer collections of atoms, and a parameterised module which implements the interface by administering a set of atoms which are supplied in advance.

To create an instance of this module we use an InStance declaration, e.g.

```
INSTANCE x:AtomInterface <INT> IS Atoms <INT> ({(FOR i IN O#42) i})
```

```
Example 55 Two modules implementing the same interface
    INTERFACE TokenInterface IS
        TYPE Token
        CON limit: INT
        PROC Token := newToken()
        PROC freeToken(Token)
    END;
    MODULE IntTokens IMPLEMENTS TokenInterface WITH
        TYPE Token = INT;
    END;
    MODULE StringTokens IMPLEMENTS TokenInterface WITH
        TYPE Token = STRING;
    END
```

This instance of the module is called x , and it exports the type x .Atom (which in this case will be INT), the constant x.limit ( 42 in this instance), and the procedures $x . n e w A t o m$ and $x . f r e e A t o m$.

We can create any number of instances of a parameterised module, and the specification of the interface in an instance declaration (e.g. ":AtomInterface<INT>") is optional.

Example 57 shows another implementation of TokenInterface. It introduces a parameterised module, called RemoteTokens, which can be instantiated by a declaration of the form

## INSTANCE tokeninstance IS RemoteTokens(sharedchannel)

where sharedchannel is a shared channel to a remote token server. The initially process gets run when tokeninstance comes into existence - it is analogous to the initialising expression of an ordinary constant or variable. The FInALLY process gets run after termination of the body of the block in which tokeninstance is declared.

In example 58 we present another parameterised module which, when instantiated, offers a sine-computation service.

```
Example 56 Parameterised interface and module
    INTERFACE AtomInterface <Atom> IS
        CON limit: INT
        PROC Atom := newAtom()
        PROC freeAtom(Atom)
    END
    MODULE Atoms <Atom> (original: {Atom})
    IMPLEMENTS AtomInterface <Atom>
    WITH
        VAR unused : {Atom} = original
        CON limit = #original
        PROC tok:Atom := newAtom() IS
        IF
            unused IS {sometok}+rest -> tok,unused := sometok,rest
        FI
        PROC freeAtom(tok:Atom) IS
            unused := unused + {tok}
    END
```

```
Example 57 An Implementation Description
    TYPE TokenDatabasePort =
        {| begin: ?INT;
                newtoken: !()?INT;
                freetoken: !INT;
                end: !()
        1}
    MODULE RemoteTokens(db: SHARED TokenDatabasePort)
    IMPLEMENTS TokenInterface
    WITH
        TYPE Token = INT
        CON limit:INT = 42
        PROC tok: Token := newToken() IS
            BEGIN
                            db.newtoken ! ();
                            db.newtoken ? n -> tok:=n
                END
        PROC freeToken(tok: Token) IS
                db.freetoken!tok
        INITIALLY
            db.begin ? n -> limit:=n
        FINALLY
            db.end ! ()
    END
```

```
Example 58 A sine server type with usage reporting
    MODULE SineService(report: !INT) IMPLEMENTS
        SHARED PROC REAL := sine(REAL)
    WITH
        VAR usage: INT = 0
        PROC result:REAL = SINE(value: REAL) IS ....
        INITIALLY
            DO
            SERVER output:REAL := sine(input: REAL) IN
                    output := SINE(input);
                    usage := usage + 1
                END
            OD
        FINALLY
            report!usage
    END
```


## 4 Services

## Note that Version 1 implements the Core and Module languages of eCSP; but not the Service language described here.

### 4.1 Introduction

The conceptual architecture behind the provision of services is rather simple. A service (for example: number translation), will in general have several aspects (for example: client customisation, call handling, statistics reporting). Each invocation of every aspect of every service is handled in the INS by spawning an aspect-specific process in response to the initial call.

This handler process oversees the entire life of the invocation. It may call on facilities provided by other processes - either other evanescent handlers or long-lived utilities provided as part of the INS infrastructure such as databases and network adapters. Note that the distribution of messages from the network amongst currently-active processes, and the multiplexing of messages intended for the network will be implemented by a network adapter layer.

### 4.2 Example: A "Follow Me" Service

We begin with an example of a simple service in which calls to the subscriber's number are rerouted to another number. When the subscriber rings a dedicated number, he is prompted for information for a new routing. Thus, as the subscriber makes his way from office to customer to restaurant and back to office, he rings the special number upon his arrival at each place so that he can receive his calls on that phone. (Of course a full version of such a service would need more features to make it really useful, but this will suffice to show how a service is implemented.)

At the topmost level of description, we note that there are two aspects to this service: the routing of calls to the subscriber, and the changing of routing target. Although these aspects are processes that are run independently of each other, they may share some common resources - in particular they will need to refer to the same mapping from the subscriber's ordinary number to his new number.

The overall structure of the service is as follows:

```
SERVICE FollowMe IS
    VAR translate : Number +> Number
    ASPECT Route (caller:Number, callee:Number; sw:Switch) IS
    END
    ASPECT Edit (caller:Number, callee:Number; sw:Switch) IS
    END
END
```

The translate function is a finite mapping from Number (i.e. a telephone number) to Number, which implements the current routing for all subscribers to this service. Although it will be implemented using database access, the service description uses it only at this abstract level. This has important implications for efficiency which we discuss below.

Route and Edit are processes, instances of which are created dynamically when the appropriate trigger is detected. For Route this will be the dialling of a subscriber's number; for Edit it will be the dialling of the dedicated number for changing the routing. Triggers are set when these service aspects are installed; they are not part of the description of aspects.

The parameter list of a service aspect implements the interface between an instance of the aspect and the environment that created it and with which it interacts. In this example, each aspect is provided with the dialling number, the dialled number, and a port through which it communicates with the network. In practice this will be a process that provides the aspect with a simple and standardised view of network interaction.

First let us look at the body of the Route aspect:

```
ASPECT Route (caller:Number, callee:Number; sw:Switch) IS
    LET VAR callee':Number
    IN
        IF callee MEM DOM translate -> callee' := translate(callee)
        ELSE TRUE -> callee' := callee
        FI;
        sw!Connect (caller,callee')
    END
```

If the called function is in the domain of translate - i.e. translate includes a mapping from that number - we use translate to find the new destination; otherwise we use the number originally dialled. An instruction is then sent to the switch asking for the connection to be made; this instruction will not require a reply, as there is no special action to be taken on a successful or
unsuccesful connexion. There is nothing further for the aspect instance to do, so it terminates.

Now consider the Edit aspect:

```
ASPECT Edit (caller:Number, callee:Number; sw:Switch) IS
    sw!GetSubNumber
    IF
        sw?Number sub
            -> sw!GetDestNumber;
                        IF sw?Number dest -> translate(sub) := dest
                        ELSE sw?_ -> SKIP
                        FI
    ELSE
        sw?_ -> SKIP
    FI
END
```

The switch is instructed to perform whatever actions are required to obtain the subscriber number and the destination number from the caller. (Note that the caller and callee numbers are not actually used in this process.) If numbers are yielded as a result of both these requests, the translate mapping is updated accordingly; otherwise no action is performed.

### 4.3 Database access optimisation

Consider a slightly more elaborate routing service than that described above, where routing can depend upon such things as the day of the week or the caller's area code, and may yield a sequence of alternative numbers to try. The abstract interface to the database used by such a service would, of course, be described by a more elaborate translation mapping - perhaps

$$
\text { translate }: \text { Number } \rightarrow(\text { UserData } \rightarrow[\text { Number }])
$$

It is important that the underlying database accesses are performed as efficiently as possible, so we almost certainly want to avoid generating multiple database accesses to retrieve the number sequence.

The problem may seem like one whose solution demands that the service designer deal with database access at a lower level. We wish to avoid this solution because not only does it make the programmer's task more difficult, it also makes the result less portable because it depends on the relative efficiencies of basic actions, and these may vary from machine to machine, from library to library, or from one version of a library to the next.

We choose instead to leave the optimisation to the compiler. While this would allow a programmer to inadvertently implement a service with unnecessarily expensive database access, the compiler would be able to detect this (it knows
what patterns of access it can generate efficient code for) and warn the programmer at compile time. Should the set of desirable patterns change, perhaps owing to a library re-implementation, the compiler can identify any existing service programs whose database requirements will need to be restructured if they are to remain efficient.

It is, desirable, of course that the compiler be highly configurable with respect to the database access library, so a notation will have to be designed that can be used to describe that library succinctly. It seems unnecessary to burden service designers with the task of learning and using the configuration notation - we expect this to be the province of a database specialist.

## References

[1] INMOS Ltd., occam ${ }^{\text {TM }} 2$ Reference Manual, Series in Computer Science, Prentice-Hall International (1988).
[2] G. Jones \& M. Goldsmith, Programming in occam ${ }^{\text {R }}$ 2, Series in Computer Science, Prentice-Hall International (1988).
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[3] J.M. Spivey, The Z Notation: A reference manual, Series in Computer Science, Prentice-Hall International (1992).
[4] C. Morgan, Programming from Specifications (2nd edn.), Series in Computer Science, Prentice-Hall International (1994).


[^0]:    *Programming Research Group, Oxford University Computing Laboratory, OX1 3QD, UK.

[^1]:    ${ }^{1}$ Which should not, in this context, be the same as that of any nullary free data constructor or defined constant.

[^2]:    ${ }^{2}$ Distinctness is not a statically decideable property, and a simplistic compiler may not be able to warn of overlapping filters.

[^3]:    ${ }^{3}$ The type of the variable n is still Num, even though its value has type MedNum, so replacing the assignment $\mathrm{m}:=\mathrm{v}$ with $\mathrm{m}:=\mathrm{n}$ would result in an ill-typed program.

[^4]:    ${ }^{4}$ In the sense of the Morgan/Back refinement calculus [4].

[^5]:    ${ }^{5}$ More discrimination can be exercised here by factoring a combined input/match/filter alternation into a nest of input, then match, then filter alternations.

[^6]:    ${ }^{6}$ i.e. of the same type or a subtype

[^7]:    ${ }^{7}$ Recall that a channel of type $T$ implements ports of type $? T$ and $!T$.

[^8]:    ${ }^{8}$ These notations for procedure definition and invocation were first used by Bernard Sufrin in his 1971 implementation of a dialect of John Reynolds's experimental language Gedanken.

[^9]:    ${ }^{9}$ Here and subsequently we abbreviate "shared channel structure" to "shared channel".

