

Imperative Programming 2: Abstract members

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```
class A1 {  
  def sort(a: Array[Int], less: (Int,Int) => Boolean) = { ... }  
}  
  
abstract class A2 {  
  def less(x1: Int, x2: Int): Boolean  
  def sort(a: Array[Int]) = { ... }  
}
```

- When would you use A1? What about A2?

```
class A1 {  
  def sort(a: Array[Int], less: (Int,Int) => Boolean) = { ... }  
}  
  
abstract class A2 {  
  def less(x1: Int, x2: Int): Boolean  
  def sort(a: Array[Int]) = { ... }  
}
```

- When would you use A1? What about A2?
- Who provides the **less** parameters of A1 and A2?

```
class A1 {  
  def sort(a: Array[Int], less: (Int,Int) => Boolean) = { ... }  
}  
  
abstract class A2 {  
  def less(x1: Int, x2: Int): Boolean  
  def sort(a: Array[Int]) = { ... }  
}
```

- When would you use A1? What about A2?
- Who provides the less parameters of A1 and A2?

```
class A1 {  
  def sort(a: Array[Int], less: (Int,Int) => Boolean) = { ... }  
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abstract class A2 {  
  def less(x1: Int, x2: Int): Boolean  
  def sort(a: Array[Int]) = { ... }  
}
```

Client program of A1

```
val a = Array(3,2,1)  
  
val s1 = new A1; s1 sort (a, _<_); println(a mkString ",")
```

- When would you use A1? What about A2?
- Who provides the less parameters of A1 and A2?

```
class A1 {  
  def sort(a: Array[Int], less: (Int,Int) => Boolean) = { ... }  
}  
  
abstract class A2 {  
  def less(x1: Int, x2: Int): Boolean  
  def sort(a: Array[Int]) = { ... }  
}
```

Client program of A1

```
val a = Array(3,2,1)  
  
val s1 = new A1; s1 sort (a, _<_); println(a mkString ",")  
  
object s2 extends A2 { def less(x1:Int, x2:Int) = x1 > x2 }  
s2 sort a; println(a mkString ",")
```

Subclass of A2

Two notions of abstraction

```
class A1 {  
  def sort(a: Array[Int], less: (Int,Int) => Boolean) = { ... }  
}  
  
abstract class A2 {  
  def less(x1: Int, x2: Int): Boolean  
  def sort(a: Array[Int]) = { ... }  
}
```

1. Parameterisation (i.e., parameter passing).
2. Abstract members -- abstract methods

Two notions of abstraction

```
class A1 {  
  def sort(a: Array[Int], less: (Int,Int) => Boolean) = { ... }  
}  
  
abstract class A2 {  
  def less(x1: Int, x2: Int): Boolean  
  def sort(a: Array[Int]) = { ... }  
}
```

1. Parameterisation (i.e., parameter passing).
2. Abstract members -- abstract methods

Two notions of abstraction

```
class A1 {  
  def sort(a: Array[Int], less: (Int,Int) => Boolean) = { ... }  
}  
  
abstract class A2 {  
  val a: Array[Int]  
  def less(x1: Int, x2: Int): Boolean  
  def sort() = { ... }  
}
```

1. Parameterisation (i.e., parameter passing).
2. Abstract members -- abstract methods, **abstract values**

Two notions of abstraction

```
class A1[T] {  
  def sort(a: Array[T], less: (T,T) => Boolean) = { ... }  
}  
  
abstract class A2 {  
  val a: Array[Int]  
  def less(x1: Int, x2: Int): Boolean  
  def sort() = { ... }  
}
```

1. Parameterisation (i.e., parameter passing).
2. Abstract members -- abstract methods, abstract values

Two notions of abstraction

```
class A1[T] {  
  def sort(a: Array[T], less: (T,T) => Boolean) = { ... }  
}  
  
abstract class A2 {  
  type T  
  val a: Array[T]  
  def less(x1: T, x2: T): Boolean  
  def sort() = { ... }  
}
```

1. Parameterisation (i.e., parameter passing).
2. Abstract members -- abstract methods, abstract values, **abstract types**

Two notions of abstraction

```
class A1[T <: List[Any]] {  
  def sort(a: Array[T], less: (T,T) => Boolean) = { ... }  
}  
  
abstract class A2 {  
  type T  
  val a: Array[T]  
  def less(x1: T, x2: T): Boolean  
  def sort() = { ... }  
}
```

1. Parameterisation (i.e., parameter passing).
2. Abstract members -- abstract methods, abstract values, abstract types

Two notions of abstraction

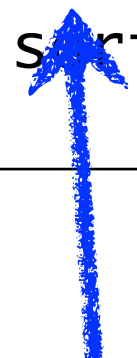
```
class A1[T <: List[Any]] {  
  def sort(a: Array[T], less: (T,T) => Boolean) = { ... }  
}  
  
abstract class A2 {  
  type T <: List[Any]  
  val a: Array[T]  
  def less(x1: T, x2: T): Boolean  
  def sort() = { ... }  
}
```

1. Parameterisation (i.e., parameter passing).
2. Abstract members -- abstract methods, abstract values, **abstract types with bounds**.

Usually, a client program of A1 knows what T, a and less are, but a subclass of A1 doesn't.



```
class A1[T <: List[Any]] {  
  def sort(a: Array[T], less: (T,T) => Boolean) = { ... }  
}  
  
abstract class A2 {  
  type T <: List[Any]  
  val a: Array[T]  
  def less(x1: T, x2: T): Boolean  
  def sort() = { ... }  
}
```



Usually, a subclass of A1 knows what T, a and less are, but a client program of A1 doesn't.

Learning outcome

- Can use abstract members in writing Scala programs.
- Can describe the meaning of abstract types.
- Can understand how to use abstract types for hiding implementation details.

Syntax: Declaration

- Just declare, but don't give a definition.
- It works for all of abstract values, methods and types.

```
abstract class Sort {  
  type T <: List[Any]  
  val a: Array[T]  
  def less(x1: T, x2: T): Boolean  
  def sort() = { ... }  
}
```

Syntax: Instantiation

```
abstract class Sort {  
  type T <: List[Any]  
  val a: Array[T]  
  def less(x1: T, x2: T): Boolean  
  def sort() = { ... }  
}
```

- Use overriding.
 1. By subclassing or subtraiting.
 2. By anonymous class.

Syntax: Instantiation

```
abstract class Sort {  
  type T <: List[Any]  
  val a: Array[T]  
  def less(x1: T, x2: T): Boolean  
  def sort() = { ... }  
}
```

- Use overriding.

1. By subclassing or subtraiting.

2. By anonymous class.

```
class MySort extends Sort {  
  type T = List[Int]  
  val a: Array[T] =  
    Array.fill(100)(Nil)  
  def less(x: T, y: T) =  
    x.length < y.length  
}  
val s: Sort = new MySort
```

Syntax: Instantiation

```
abstract class Sort {  
  type T <: List[Any]  
  val a: Array[T]  
  def less(x1: T, x2: T): Boolean  
  def sort() = { ... }  
}
```

- Use overriding.
 1. By subclassing or subtraiting.
 2. By anonymous class.

```
class MySort extends Sort {  
  type T = List[Int]  
  val a: Array[T] =  
    Array.fill(100)(Nil)  
  def less(x: T, y: T) =  
    x.length < y.length  
}  
val s: Sort = new MySort
```

```
val s: Sort =  
  new Sort {  
    type T = List[Int]  
    val a: Array[T] =  
      Array.fill(100)(Nil)  
    def less(x: T, y: T) =  
      x.length < y.length  
  }
```

```

abstract class Sort {
  type T <: List[Any]
  val a: Array[T]
  def less(x1: T, x2: T): Boolean
  def sort() { a.sortWith(less _) }
  def compare(b: Array[T]): Boolean =
    (a zip b) forall (x => less(x._1, x._2))
}

class MySort extends Sort {
  type T = List[Int]
  val a: Array[T] = Array.fill(100)(Nil)
  def less(x:T, y:T) = x.length < y.length
}

val s1: MySort = new MySort; s1.sort()
val s2: MySort = new MySort; s2.sort()
println(s1 compare s2.a)

```

[Q1] What is the output?

1) true 2) false 3) random 4) compile error

```
abstract class Sort {  
  type T <: List[Any]  
  val a: Array[T]  
  def less(x1: T, x2: T): Boolean  
  def sort() { a.sortWith(less) }  
  def compare(b: Array[T]): Boolean =  
    (a zip b) forall (x => less(x._1, x._2))  
}  
class MySort extends Sort {  
  type T = List[Int]  
  val a: Array[T] = Array.fill(100)(Nil)  
  def less(x:T, y:T) = x.length < y.length  
}  
  
val s1: MySort = new MySort; s1.sort()  
val s2: MySort = new MySort; s2.sort()  
println(s1 compare s2.a)
```

The type T of an MySort object is List[Int], and this is known everywhere.

[Q1] What is the output?

1) true 2) false 3) random 4) compile error

```
abstract class Sort {  
  type T <: List[Any]  
  val a: Array[T]  
  def less(x1: T, x2: T): Boolean  
  def sort() { a.sortWith(less) }  
  def compare(b: Array[T]): Boolean =  
    (a zip b) forall (x => less(x._1, x._2))  
}  
class MySort extends Sort {  
  type T = List[Int]  
  val a: Array[T] = Array.fill(100)(Nil)  
  def less(x:T, y:T) = x.length < y.length  
}  
  
val s1: Sort = new MySort; s1.sort()  
val s2: Sort = new MySort; s2.sort()  
println(s1 compare s2.a)
```

[Q2] What is the output?

1) true 2) false 3) random 4) compile error

```

abstract class Sort {
  type T <: List[Any]
  val a: Array[T]
  def less(x1: T, x2: T): Boolean
  def sort() { a.sortWith(less) }
  def compare(b: Array[T]): Boolean =
    (a zip b) forall (x => less(x._1, x._2))
}

class MySort extends Sort {
  type T = List[Int]
  val a: Array[T] = Array.fill(100)(Nil)
  def less(x:T, y:T) = x.length < y.length
}

val s1: Sort = new MySort; s1.sort()
val s2: Sort = new MySort; s2.sort()
println(s1 compare s2.a)

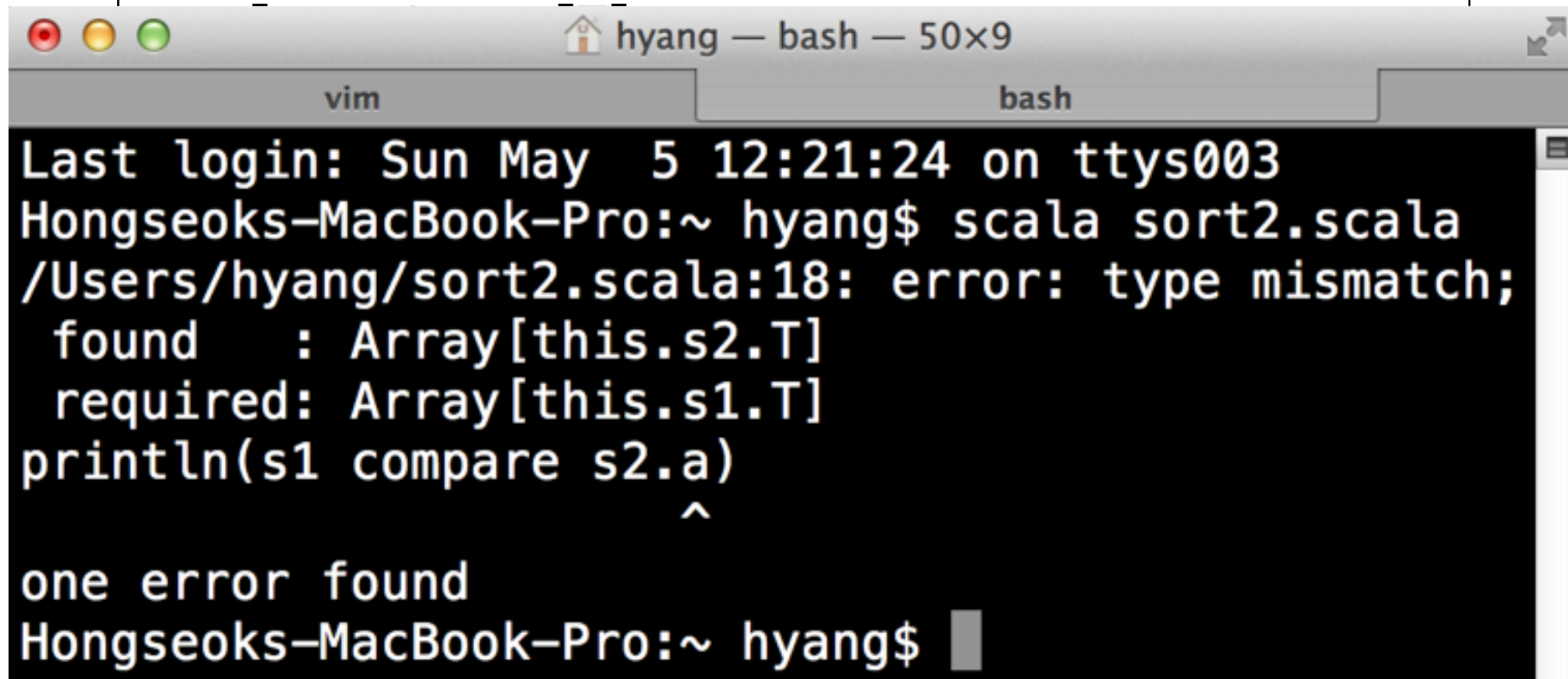
```

Each object of type Sort has its own T, whose identity is unknown to others.

[Q2] What is the output?

1) true 2) false 3) random 4) compile error

```
abstract class Sort {  
  type T <: List[Any]
```



A terminal window titled 'hyang — bash — 50x9' with tabs for 'vim' and 'bash'. The terminal shows the command 'scala sort2.scala' being executed. The output is a Scala compilation error: '/Users/hyang/sort2.scala:18: error: type mismatch; found : Array[this.s2.T] required: Array[this.s1.T] println(s1 compare s2.a)'. The error points to the 'a' property access in the 'compare' method call. Below the error, it says 'one error found' and the prompt 'Hongseoks-MacBook-Pro:~ hyang\$' is shown.

```
Last login: Sun May 5 12:21:24 on ttys003  
Hongseoks-MacBook-Pro:~ hyang$ scala sort2.scala  
/Users/hyang/sort2.scala:18: error: type mismatch;  
found   : Array[this.s2.T]  
required: Array[this.s1.T]  
println(s1 compare s2.a)  
                        ^  
one error found  
Hongseoks-MacBook-Pro:~ hyang$
```

```
val s1: Sort = new MySort; s1.sort()  
val s2: Sort = new MySort; s2.sort()  
println(s1 compare s2.a)
```

Each object of type Sort has its own T,
whose identity is unknown to others.

[Q2] What is the output?

- 1) true 2) false 3) random 4) compile error

Semantics of abstract types

```
abstract class Sort {  
  type T  
  ...  
  def compare(b: Array[T]): Boolean ...  
}  
class MySort extends Sort { ... }  
  
val s1: Sort = new MySort  
val s2: Sort = new MySort  
// println(s1 compare s2.a) -- Compile Error
```

- New T for each object s of Sort.
- Thus, $s1.T \neq s2.T$
- This feature is used for fine-tuning a spec about where a method can be used.

Path-dependent type “s.T”

```
abstract class Sort {  
  type T  
  ...  
}  
val s1: Sort = ...  
val s2: Sort = ...
```

```
class Circuit {  
  class Wire { ... }  
  ...  
}  
val c1 = new Circuit  
val c2 = new Circuit  
var w1 = new c1.Wire  
var w2 = new c2.Wire
```

- Type-per-object is also used for inner class.
- All such per-object types are denoted by path-dependent type expressions, such as `x.y.z.T`
- They are called path-dependent types.
- Examples -- `s1.T`, `s2.T`, `c1.Wire`, `c2.Wire`

Path-dependent type “s.T”

```
abstract class Sort {  
  type T  
  ...  
}  
val s1: Sort = ...  
val s2: Sort = ...
```

```
class Circuit {  
  class Wire { ... }  
  ...  
}  
val c1 = new Circuit  
val c2 = new Circuit  
var w1 = new c1.Wire  
var w2 = new c2.Wire  
w1 = w2
```

compile
error

- Type-per-object is also used for inner class.
- All such per-object types are denoted by path-dependent type expressions, such as `x.y.z.T`
- They are called path-dependent types.
- Examples -- `s1.T`, `s2.T`, `c1.Wire`, `c2.Wire`

Programming challenge: Currencies

- Build a library for currencies.
- At least US Dollar and UK Pound.
- Hide implementation details.
- Support money addition.
- No addition between dollars and pounds.

1. USD & GBP
2. Hiding
3. Addition
4. Don't mix

1. USD & GBP
- ~~2. Hiding~~
3. Addition
4. Don't mix

```
abstract class Currency ...  
  
object Currency {  
  private class UK ... extends Currency ...  
  private class US ... extends Currency ...  
  
  def makeUS(...): Currency = new US(...)  
  def makeUK(...): Currency = new UK(...)  
}
```

1. USD & GBP
- ~~2. Hiding~~
3. Addition
4. Don't mix

```
abstract class Currency {  
  def amount: Long  
  val designation: String  
  def add(c: Currency): Currency ...  
  override def toString = (amount + " " + designation)  
}  
  
object Currency {  
  private class UK ... extends Currency ...  
  private class US ... extends Currency ...  
  
  def makeUS(...): Currency = new US(...)  
  def makeUK(...): Currency = new UK(...)  
}
```

1. USD & GBP
- ~~2. Hiding~~
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```
abstract class Currency {  
  def amount: Long  
  val designation: String  
  def add(c: Currency): Currency ...  
  override def toString = (amount + " " + designation)  
}  
  
object Currency {  
  private class UK(val amount: Long) extends Currency {  
    val designation = "GBP"  
    ...  
  }  
  private class US ... extends Currency ...  
  
  def makeUS(...): Currency = new US(...)  
  def makeUK(...): Currency = new UK(...)  
}
```

- ~~1. USD & GBP~~
- ~~2. Hiding~~
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4. Don't mix

```
abstract class Currency {  
  def amount: Long  
  val designation: String  
  def add(c: Currency): Currency ...  
  override def toString = (amount + " " + designation)  
}  
  
object Currency {  
  private class UK(val amount: Long) extends Currency {  
    val designation = "GBP"  
    ...  
  }  
  private class US(d: Long, p: Long) extends Currency {  
    val amount = d * 100 + p  
    val designation = "USD"  
    ...  
  }  
  def makeUS(...): Currency = new US(...)  
  def makeUK(...): Currency = new UK(...)  
}
```

- ~~1. USD & GBP~~
- ~~2. Hiding~~
3. Addition
4. Don't mix

```
abstract class Currency {  
  def amount: Long  
  val designation: String  
  def add(c: Currency): Currency ...  
  override def toString = (amount + " " + designation)  
}  
  
object Currency {  
  private class UK(val amount: Long) extends Currency {  
    val designation = "GBP"  
    ...  
  }  
  private class US(d: Long, p: Long) extends Currency {  
    val amount = d * 100 + p  
    val designation = "USD"  
    ...  
  }  
  def makeUS(a: Long): Currency = new US(a / 100, a % 100)  
  def makeUK(a: Long): Currency = new UK(a)  
}
```

[Q] Can you
implement add?

- ~~1. USD & GBP~~
- ~~2. Hiding~~
3. Addition
4. Don't mix

```
abstract class Currency {  
  def amount: Long  
  val designation: String  
  def add(c: Currency): Currency ...  
  override def toString = (amount + " " + designation)  
}  
  
object Currency {  
  private class UK(val amount: Long) extends Currency {  
    val designation = "GBP"  
    ...  
  }  
  private class US(d: Long, p: Long) extends Currency {  
    val amount = d * 100 + p  
    val designation = "USD"  
    ...  
  }  
  def makeUS(a: Long): Currency = new US(a / 100, a % 100)  
  def makeUK(a: Long): Currency = new UK(a)  
}
```

[Q] Can you
implement add?

- ~~1. USD & GBP~~
- ~~2. Hiding~~
- ~~3. Addition~~
4. Don't mix

```
abstract class Currency {  
  def amount: Long  
  val designation: String  
  def add(c: Currency): Currency  
  override def toString = (amount + " " + designation)  
}  
  
object Currency {  
  private class UK(val amount: Long) extends Currency {  
    val designation = "GBP"  
    def add(c: Currency) = makeUK(amount+c.amount)  
  }  
  private class US(d: Long, p: Long) extends Currency {  
    val amount = d * 100 + p  
    val designation = "USD"  
    def add(c: Currency) = makeUS(amount+c.amount)  
  }  
  def makeUS(a: Long): Currency = new US(a / 100, a % 100)  
  def makeUK(a: Long): Currency = new UK(a)  
}
```

It mixes
dollars and
pounds

Key idea -- Abstract type

```
abstract class Currency {  
  def amount: Long  
  val designation: String  
  def add(c: Currency): Currency  
  override def toString = (amount + " " + designation)  
}
```

Key idea -- Abstract type

```
abstract class CurrencyZone {  
  type T <: Currency  
  
  abstract class Currency {  
    def amount: Long  
    val designation: String  
    def add(c: T): T  
    override def toString = (amount + " " + designation)  
  }  
}
```

New spec -- add now accepts money in a particular yet unknown currency T.

Key idea -- Abstract type

Abstract factory method for T here, because T is unique per object.

```
abstract class CurrencyZone {  
  type T <: Currency  
  def make(amount: Long): T  
  
  abstract class Currency {  
    def amount: Long  
    val designation: String  
    def add(c: T): T  
    override def toString = (amount + " " + designation)  
  }  
}
```

New spec -- add now accepts money in a particular yet unknown currency T.

Key idea -- Abstract type

Abstract factory method for T here, because T is unique per object.

```
abstract class CurrencyZone {  
  type T <: Currency  
  def make(amount: Long): T  
  
  abstract class Currency {  
    def amount: Long  
    val designation: String  
    def add(c: T): T = make(amount + c.amount)  
    override def toString = (amount + " " + designation)  
  }  
}
```

New spec -- add now accepts money in a particular yet unknown currency T.

```
abstract class CurrencyZone {  
  type T <: Currency  
  def make(amount: Long): T  
  
  abstract class Currency {  
    def amount: Long  
    val designation: String  
    ... }  
}
```

```
abstract class CurrencyZone {  
  type T <: Currency  
  def make(amount: Long): T  
  
  abstract class Currency {  
    def amount: Long  
    val designation: String  
    ... }  
}
```

```
object UK extends CurrencyZone {
```

```
}  
object US extends CurrencyZone {
```

```
}
```

Two T's -- one unique to UK,
and another to the US obj.
Hence, no mix in add.

```
abstract class CurrencyZone {  
  type T <: Currency  
  def make(amount: Long): T  
  
  abstract class Currency {  
    def amount: Long  
    val designation: String  
    ... }  
}  
  
object UK extends CurrencyZone {  
  class Pound(...) extends Currency ...  
  
  type T = Pound  
}  
  
object US extends CurrencyZone {  
  
}
```

```
abstract class CurrencyZone {
  type T <: Currency
  def make(amount: Long): T

  abstract class Currency {
    def amount: Long
    val designation: String
    ... }
}

object UK extends CurrencyZone {
  class Pound(...) extends Currency ...

  type T = Pound
  def make(amount: Long) = new Pound(amount)
}

object US extends CurrencyZone {
```

```
abstract class CurrencyZone {  
  type T <: Currency  
  def make(amount: Long): T  
  
  abstract class Currency {  
    def amount: Long  
    val designation: String  
    ... }  
}  
  
object UK extends CurrencyZone {  
  class Pound(val amount: Long) extends Currency {  
    val designation = "GBP"  
  }  
  type T = Pound  
  def make(amount: Long) = new Pound(amount)  
}  
object US extends CurrencyZone {  
  
}
```

[Q1] Complete the definition of the US object.

```
abstract class CurrencyZone {  
  type T <: Currency  
  def make(amount: Long): T  
  
  abstract class Currency {  
    def amount: Long  
    val designation: String  
    ... }  
}  
  
object UK extends CurrencyZone {  
  class Pound(val amount: Long) extends Currency {  
    val designation = "GBP"  
  }  
  type T = Pound  
  def make(amount: Long) = new Pound(amount)  
}  
  
object US extends CurrencyZone {  
  
  type T = ...  
  def make(amount: Long) = ...  
}
```

[Q1] Complete the definition of the US object.

```
abstract class CurrencyZone {  
  type T <: Currency  
  def make(amount: Long): T  
  
  abstract class Currency {  
    def amount: Long  
    val designation: String  
    ... }  
}
```

```
object UK extends CurrencyZone {  
  class Pound(val amount: Long) extends Currency {  
    val designation = "GBP"  
  }  
  type T = Pound  
  def make(amount: Long) = new Pound(amount)  
}
```

```
object US extends CurrencyZone {  
  class Dollar(d: Long, p: Long) extends Currency {  
    val amount = 100 * d + p  
    val designation = "USD"  
  }  
  type T = Dollar  
  def make(amount: Long) = new Dollar(amount / 100, amount % 100)  
}
```

```
abstract class CurrencyZone {  
  type T <: Currency  
  def make(amount: Long): T  
  
  abstract class Currency {  
    def amount: Long  
    val designation: String  
    ... }  
}
```

```
object UK extends CurrencyZone {  
  class Pound(val amount: Long) extends Currency {  
    val designation = "GBP"  
  }  
  type T = Pound  
  def make(amount: Long) = new Pound(amount)  
}
```

```
object US extends CurrencyZone {  
  class Dollar(d: Long, p: Long) extends Currency {  
    val amount = 100 * d + p  
    val designation = "USD"  
  }  
  type T = Dollar  
  def make(amount: Long) = new Dollar(amount / 100, amount % 100)  
}
```

[Q1] Complete the definition of the US object.
[Q2] Why no private?

```

abstract class CurrencyZone {
  type T <: Currency
  def make(amount: Long): T

  abstract class Currency {
    def amount: Long
    val designation: String
    ... }
}

```

[Q1] Complete the definition of the US object.
[Q2] Why no private?

```

val UKZone : CurrencyZone = UK
val USZone : CurrencyZone = US

```

```

private object UK extends CurrencyZone {
  class Pound(val amount: Long) extends Currency {
    val designation = "GBP"
  }
  type T = Pound
  def make(amount: Long) = new Pound(amount)
}

private object US extends CurrencyZone {
  class Dollar(d: Long, p: Long) extends Currency {
    val amount = 100 * d + p
    val designation = "USD"
  }
  type T = Dollar
  def make(amount: Long) = new Dollar(amount / 100, amount % 100)
}

```

Abstract type

- Can be used to hide implementation details.
- It is unique per each object.
- This unique-per-object semantics enables us to achieve a stronger guarantee using types.

Summary

- Abstraction in Scala can be achieved by parameter passing and abstract members.
- Abstract types have unique-per-object semantics.
- This semantics can be used to achieve a stronger guarantee about programs.
- Read Chapter 20.

Optional reading

Section 5 of the Scala design paper:

<http://www.scala-lang.org/docu/files/ScalaOverview.pdf>

```
abstract class SubjectObserver {  
  type S <: Subject  
  type O <: Observer  
  abstract class Subject { this : S =>  
    private var observers: List[O] = List()  
    def subscribe(obs: O) =  
      observers = obs :: observers  
    def publish =  
      for (val obs <- observers) obs.notify(this)  
  }  
  trait Observer {  
    def notify(sub: S): unit  
  }  
}
```

```
object SensorReader extends SubjectObserver {  
  type S = Sensor  
  type O = Display  
  abstract class Sensor extends Subject {  
    val label: String  
    var value: double = 0.0  
    def changeValue(v: double) = {  
      value = v  
      publish  
    }  
  }  
  class Display extends Observer {  
    def println(s: String) = ...  
    def notify(sub: Sensor) =  
      println(sub.label + "_has_value_" + sub.value)  
  }  
}
```