Preface

Generic programming is about making programming more effective by making it more general. This volume is about a novel form of genericity in programs, based on parameterizing programs by the structure of the data they manipulate. The material is based on lectures presented at a summer school on Generic Programming held at the University of Oxford in August 2002.

The lectures by Hinze and Jeuring introduced Generic Haskell, an extension of the Haskell programming language that allows the programmer to define a function by induction on the structure of types. The implementation of Generic Haskell provided a valuable tool for students to experiment with applications of this form of datatype genericity. The lecture material in this volume is divided into two parts. The first part (“practice and theory”) introduces Generic Haskell and the theory that underlies its design. The second part (“applications”) discusses three advanced applications of Generic Haskell in some depth.

The value of generic programming is illusory unless the nature and extent of the genericity can be described clearly and precisely. The lectures by Backhouse and Crole delve deeper into the theoretical basis for datatype genericity. Backhouse reviews the notion of parametric polymorphism (a notion well known to functional programmers) and then shows how this notion is extended to higher-order notions of parametricity. These are used to characterize what it means for a value to be stored in a datatype. Also, transformations on data structures are given precise specifications in this way. Underlying this account are certain basic notions of category theory and allegory theory. Crole presents the category theory needed for a deeper understanding of mechanisms for defining datatypes.

The final chapter, by Fiadeiro, Lopes and Wermelinger applies the mathematical “technology” of parameterization to the larger-scale architectural structure of programs. The description of a system is split into components and their interactions; architectural connectors are parameterized by components, leading to an overall system structure consisting of components and connector instances establishing the interactions between the components.

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