Joint Search by Social and Spatial Proximity

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Abstract—The diffusion of social networks introduces new challenges and opportunities for advanced services, especially so with their ongoing addition of location-based features. We show how applications like company and friend recommendation could significantly benefit from incorporating social and spatial proximity, and study a query type that captures these two-fold semantics. We develop highly scalable algorithms for its processing, and enhance them with elaborate optimizations. Finally, we use real social network data to empirically verify the efficiency and efficacy of our solutions.

1 INTRODUCTION

The emergence of social networks (SNs) brings a new era in the organization and browsing of online information. Manufacturers and service providers are becoming increasingly interested in exploiting popular SNs to promote their products and services. Recently, Microsoft’s search engine (Bing) has integrated social information from Facebook to return web pages that are popular among the friends of users [1]. Studies like [2] have investigated the influence between users of SNs and quantified the probability of a user performing an action (e.g., purchase a product) after his/her friend(s) did. Current text search systems have also incorporated social influence into query processing by taking into account friend relationships for the ranking of documents/objects [3], [4].

On the other hand, location-based services are an indispensable feature in SNs. This fact becomes increasingly prominent as the number of users who access SN applications on mobile devices is growing steadily. The most popular SN, Facebook, includes a set of location-based features, while others (such as Foursquare) are explicitly based on the management of user locations. Motivated by this trend, we investigate the integration of social and spatial information in a single query.

Consider a service like badoo.com, where a user \( u_1 \) who is looking for company to have lunch or watch a movie, may browse the profiles of nearby users and invite them to join him/her. Existing systems apply a traditional \( k \)-nearest neighbor query [5], potentially with some binary conditions (regarding age, sex, etc), to provide \( u_1 \) with the profiles of users in the vicinity. While recommended users are indeed near \( u_1 \) geographically, his/her true preferences of companions would be better captured if SN information was also taken into account. Assume, for example, that the users’ Euclidean coordinates and social connections are as shown in Figures 1(a) and 1(b) respectively. The closest user to \( u_1 \) in the spatial domain is \( u_5 \). However, \( u_4 \) might be a better match because he locates only slightly farther (compared to \( u_5 \)) but is “closer” in the social network. Conversely, the closest user socially (\( u_2 \)) may be too far spatially. Therefore, to provide meaningful recommendations, both social proximity and spatial proximity should be incorporated into the search.

In this paper we propose and study the social and spatial ranking query (SSRQ). SSRQ reports the top-\( k \) users in the SN based on a ranking function that incorporates social and spatial distance from the query user. Our key contributions are:

- We conduct the first study on a joint search by social and spatial user proximity.
- We propose a suite of processing methodologies, including a highly scalable and robust approach that relies on indexing and social summaries.
- We equip the latter with sophisticated optimizations, based on computation sharing, intermediate result caching and an accuracy-enhancing strategy that complements social summaries in proximity estimation.
- We use real SN data to experimentally evaluate our algorithms.
2 RELATED WORK

2.1 Social Influence and Proximity Measures

The influence between two users captures the probability that one user follows the other’s actions. The influence information stemming from SNs can improve marketing strategies, for instance, by recommending products to users based on the purchases of their contacts [6]. Existing work focuses primarily on finding the top-\(k\) most influential users from a graph of influence scores [2] or learning the influence scores based on users’ past propagation of actions [7], [8]. Recently, [9] proposed an approach to directly obtain the top-\(k\) most influential users from historical data, without the intermediate step of constructing an influence graph.

Many measures are proposed for computing the influence between two users (vertices) in a social graph. Simple measures rely either on the shortest path distance or on vertex neighborhoods – i.e., the social proximity of two users may be defined as the inverse of their shortest path distance in the SN [3], [4] or as the number of their common friends [10]. Sophisticated proximity measures involve a combination of infinite sums over the ensemble of all paths between two vertices and their common neighbors (e.g., Katz measure, rooted PageRank, escape probability); [11] is an extensive survey on this subject.

2.2 Multiple-domain Search

Objects associated with multiple domain attributes have attracted considerable research interest. Web pages with geographic information and Flickr photos with geo-tags require query processing on both the spatial and textual domains. Spatial keyword search [12] retrieves objects that are not only close to users in physical space but which also match a set of keywords. [13] proposed the IR-tree data structure, which extends the R-tree with inverted files. This index can be used to efficiently support novel types of spatio-textual queries (e.g., [14]). A similar data structure appears in [15] to support a reverse form of spatial keyword search.

Location-based SNs, such as Foursquare, Whrrl and Gowalla, record users’ location history (e.g., check-ins). In [16], Scellato et al. observe that in a location-based social network, 30\% of new friends made are place friends, i.e., individuals who have visited the same places. Hence, they build a supervised learning framework which predicts new friend links based on the number of common contacts and common check-ins. In [17], Ye et al. observe that if a place is visited by friends of a user, this place is probably of higher interest to the user. Also, if a user has many nearby check-ins with another, one’s preferred places may also be appealing to the other. These two factors, combined with potential geographic influence among the places themselves, are used to make location recommendations to SN users. The result in [17] is a set of places of interest, while in our problem the result comprises \(k\) other SN users.

Both aforementioned studies measure social proximity between users as the number of their common friends. In our case, social influence is extended to more than two hops in the SN and defined according to shortest path distance in the social graph. Also, in the spatial domain, both [17] and [16] consider historical check-ins, whereas we only consider the current locations of users, targeting present-time applications.

Armazenoglou et al. [18] propose a general framework for queries over geo-social network data. They decouple the storage of the social network data from the geographic data; queries are evaluated as in a distributed database. The system supports searching for crisp structural patterns that appear in the social graph, which are spatially ranked. For example, the “nearest friends” query finds the \(k\) friends of a user \(u\) who are closest to a given location \(q\). Our problem and solutions are different, since we integrate ranking at both social and spatial dimensions.

In [19], Cho et al. analyze the location data of SN users and notice that an individual’s periodic movements which may seem random, are actually likely to correlate with the movements of his/her social contacts. This leads to a model of human mobility based on social links. Another related application is proximity detection in SNs. The goal is to continuously report to each user who, among his/her social contacts, is within a certain distance from the user’s current location. The problem was introduced in [20] in the context of a P2P network. Subsequent approaches include dead reckoning [21] and adaptive safe region techniques [22], as well as constraint detection formulations [23]. Proximity detection considers only immediate friends of users and a fixed radius around their locations. In contrast, in SSRQ the result may include users at an unpredictable number of social hops and at variable spatial distances from the query user.

Bao et al. [24] propose a location-aware newsfeed system. This enables users to browse spatially related messages from their friends or registered news sources. Unlike SSRQ (which selects users), that system filters news-feeds/messages. Also, it considers only immediate (1-hop) friends and news sources.

2.3 Shortest Path and Distance Computation

A traditional type of graph search is shortest path computation from a source to a target vertex. Dijkstra’s algorithm starts from the source and iteratively expands the network using a priority heap, until the target is reached. To prune the search space and direct the graph expansion, \(A^*\) algorithm prioritizes the visiting order of nodes by estimating their distance to the target. [25] introduces the landmark approach which selects a set of vertices as landmarks in the
graph and pre-computes distances from every vertex to each landmark. Given two vertices and their distances to a specific landmark, the triangular inequality produces a lower bound on the distance between the two vertices. Using multiple landmarks, we derive an equal number of lower bounds, among which the tightest can be used to enhance $A^*$ search. [26] extends this approach using a hierarchy of landmarks.

An approach to compute approximate distances between vertices in a graph is to construct oracles which provide constant query time while having linear space requirements. Theoretical results on distance oracles appear in [27], [28]. Sarma et al. [29] propose landmark based oracles which guarantee the theoretical result of [28] and experimentally outperform [27] and [28]. Distance oracles are not effective in our problem, which involves distance computations in a social graph, because we require exact distances, not approximate. Moreover, the theoretical error bounds of distance oracles are too loose and they are known to be poorly suited for social networks [29]. In [30], Cheng et al. propose a 2-hop cover data structure which supports efficient distance queries for a general graph with $O(|V||E|^{1/2})$ space. It is inapplicable to our setting because, for the density and scale of real SNs, its space requirements are prohibitive.

### 2.4 Top-$k$ Processing

Our problem is related to top-$k$ processing. A top-$k$ query specifies a preference function $f$ over the $m$ attributes of a dataset and retrieves the $k$ tuples that minimize (or maximize) this function. A thorough survey of top-$k$ processing techniques is given in [31]. Here we survey the 	extit{threshold algorithm} (TA) and its variants [32] due to their higher relevance to SSRQ.

Assume that there are $m$ repositories (sorted lists), one for each of the data attributes. The repository for the $i$-th attribute keeps all tuple identifiers sorted in ascending order of the $i$-th attribute. Two types of access are possible on each repository, 	extit{sorted} and 	extit{random}. Sorted access allows serial retrieval of elements (i.e., pairs of tuple identifier and its $i$-th attribute value) by iterative “get-next” operations, starting from the first element in the list, then moving to the second, etc. On the other hand, random access allows retrieving the attribute of any tuple in a repository directly.

TA requires that the preference function $f$ is increasingly monotone on all $m$ attributes. It probes (via sorted access) the repositories in a round-robin fashion. For each element pulled from a list, it computes the $f$ value of the corresponding tuple by fetching its remaining $m - 1$ attributes from the other repositories via random accesses. It maintains an interim result of the top-$k$ tuples seen so far. It also keeps a threshold $\tau$ computed as the value of $f$ over the last attribute values pulled from each of the $m$ repositories. Essentially, $\tau$ is a lower bound on the $f$ value of any non-encountered tuple further down the lists. TA terminates when $\tau$ is no smaller than any of the $f$ values in the interim result (which is then reported as the final result).

TA assumes that random access is possible. NRA is the 	extit{no random access} version of the algorithm, where only sorted access is available on the repositories. The repositories are probed in round-robin order. For every encountered tuple, NRA maintains a lower and an upper bound of its $f$ value. The lower bound (the upper bound) is computed by replacing the unseen attributes of the tuple with the last value pulled from the corresponding repository (the maximum possible value in the corresponding repository). NRA terminates when the $k$ smallest upper bounds among seen tuples are no greater than the lower bound of any other encountered tuple.

Another variant of TA is the 	extit{combined algorithm} (CA). TA assumes that random and sorted access have the same cost. CA, instead, considers that random access is costlier than sorted. It proceeds similarly to NRA, but it periodically performs one random access. Specifically, for every $k$ sorted accesses, one random access is made; $k$ is set to the ratio of random access cost to sorted access cost.

Bruno et al. [33] consider top-$k$ queries in web-accessible databases. The data consists of a sorted list and a set of random access lists. Since random access is expensive, the authors propose that when an object is encountered in the sorted list, only a selected subset of the random access lists is probed to refine the object’s $f$ value bounds.

### 3 Problem Setting

The problem setting includes a set of users $U$ and an undirected social graph $G = (V, E)$. Each user $u_i \in U$ has spatial coordinates in Euclidean space. The users may move dynamically; our system/query only considers their current (i.e., last reported) location. The social graph $G$ includes a vertex $v_i \in V$ for every user $u_i \in U$. We establish the convention that vertex $v_i$ corresponds to user $u_i$, i.e., the mapping is implied by the subscripts. We do not unify the two notations to help distinguish between spatial and social context. Every edge $(v_i, v_j)$ in $E$ represents a friend relationship between users $u_i, u_j$ and is associated with a numerical weight that indicates the strength of the relationship – the smaller the weight, the stronger the friendship. In previous work, given the topology of a social network, the weights are mined from past propagation of user actions [7], [8]. We make no assumption about the weights other than them being positive numbers. We consider that $G$ is undirected, but our work extends to directed graphs easily.

#### 3.1 Ranking Function

We define 	extit{spatial proximity} between users $u_i$ and $u_j$ as their Euclidean distance $d(u_i, u_j)$. On the other hand,
we measure social proximity between vertices \( v_i \) and \( v_j \) based on their shortest path distance in \( G \), and denote it as \( p(v_i, v_j) \). We use this formulation because (i) it is simple and (ii) it is demonstrated to effectively capture social proximity/influence [3], [4].

Following common practice in combining measurements from different domains, we apply a linear function over the (normalized) social and spatial proximity to rank users [13], [34], [14]. Specifically, given a query user \( u_q \), the ranking of \( u_i \in U \) is determined by function \( f \) as:

\[
f(u_q, u_i) = \alpha \cdot p(v_q, v_i) + (1 - \alpha) \cdot d(u_q, u_i) \tag{1}
\]

where \( \alpha \) is a (user- or application-specified) real number between 0 and 1 that determines the relative significance of proximity in the two domains. The smaller the value of \( \alpha \) for a user, the more suitable he/she is for \( u_q \). Note that our definition (and implementation) uses normalized social and spatial proximities, by dividing \( d(u_q, u_i) \) and \( p(v_q, v_i) \) with the maximum pairwise distance in Euclidean space and in the social graph respectively. For simplicity, we omit the denominators from the presentation.

### 3.2 Query Formulation

In this work, we propose the social and spatial ranking query (SSRQ) where a user \( u_q \) (or an application) provides parameter \( \alpha \) and asks for the top-\( k \) users who minimize function \( f \), with respect to his/her current location and social links. Formally:

**Definition 1 (SSRQ):** Given a set of users \( U \), the underlying social graph \( G \), a query user \( u_q \in U \), and a preference parameter \( \alpha \), SSRQ returns the \( k \) users \( u \) in \( U - \{u_q\} \) with the smallest \( f(u_q, u) \) values.

That is, for every \( u' \notin R \) and \( u' \neq u_q \) it holds that

\[
f(u_q, u') \geq f_k
\]

where \( f_k \) is the maximum (i.e., least preferable) ranking value \( f \) across all users in the result \( R \) of the query. In Table 1 we summarize the frequently used notation.

### 4 Preliminary Solutions

We first present two simple solutions, namely Social First Approach and Spatial First Approach; then we hybridize them into an elaborate solution called Twofold Search Approach.

#### 4.1 One Domain Approach

**Social First Approach.** A preliminary approach for SSRQ processing is the Social First Algorithm (SFA). The main idea in SFA is to consider users in increasing social distance from the query user. To achieve this, SFA expands the social graph around \( v_q \) using Dijkstra’s algorithm. For every encountered user (i.e., for every vertex popped from Dijkstra’s search heap), it also computes the Euclidean distance from \( u_q \) and, in turn, the \( f \) value. The first \( k \) users are placed in the interim result \( R \). For any subsequent user \( u \), if his/her \( f \) value is smaller than the current \( f_k \) (the \( k \)-th largest \( f \) score in \( R \)), he/she enters the interim result (and evicts from it the user with the maximum \( f \) value). The termination condition of SFA is based on the fact that the social distance of every un-processed user is lower-bounded by that of the last vertex encountered by Dijkstra’s algorithm. Therefore, if \( v \) is the last vertex popped from Dijkstra’s heap, expression \( \theta = \alpha \cdot p(v_q, v) \) lower-bounds the \( f \) value of every non-encountered user. Hence, set \( R \) is guaranteed to include the correct result when \( \theta \geq f_k \), i.e., it is safe for SFA to terminate.

**Spatial First Approach.** Spatial First Approach (SPA) is another preliminary solution. It processes users in increasing spatial distance from the query user. For this purpose, SPA uses an incremental nearest neighbor (NN) search in the Euclidean space. To efficiently perform this search, a regular grid index is built on the user locations and a branch-and-bound algorithm is used to retrieve the NNs; this combination is the most suitable for dynamic spatial data kept in main memory [35]. For every encountered user, SPA directly calculates their social distance to the query user and inserts them into the interim result \( R \) if necessary, similar to SFA. If \( u \) is the last NN retrieved, expression \( \theta = (1 - \alpha) \cdot d(u_q, u) \) lower-bounds the \( f \) value of every non-encountered user. Hence, set \( R \) is guaranteed to be correct when \( \theta \geq f_k \).

Although SFA and SPA are intuitive and simple, they suffer from a major drawback. They are unaware of either the spatial distance or the social distance of the un-processed users, i.e., the value of \( \theta \) relies solely on either social or spatial information and, therefore, may be too loose. This shortcoming motivates the algorithm described next.

#### 4.2 Twofold Search Approach

In this section we describe an SSRQ processing approach which performs concurrently a social and a
spatial search, thus termed twofold search algorithm (TSA). This twofold search equips TSA with two lower bounds for un-processed users (one on their social and the other on their spatial distance from \(u_q\)), thus deriving a tighter overall bound on \(f\) and alleviating the main drawback of SFA and SPA. The social search around \(u_q\) is performed by Dijkstra’s algorithm, similar to SFA. The second search is an incremental NN retrieval in the Euclidean space, similar to SPA. TSA executes in two phases.

In the first phase, the two searches proceed simultaneously, by iteratively reporting the next closest user in their respective domain, and alternating with each other in a round-robin manner. Whenever the social search is invoked, the encountered user is evaluated, i.e., its \(f\) value is computed and checked against the current \(f_k\) for potential inclusion into the interim result \(R\). Note that evaluation is fast in this case, because Euclidean distance from \(u_q\) is trivial to compute. In contrast, when the spatial search is invoked, the encountered user is either (i) ignored if he/she has already been encountered by the social search or (ii) placed in a candidate set \(Q\). Set \(Q\) keeps users that are only partially evaluated, because computing their social distance from \(q\) requires expensive processing. The spatial and social search, due to their incremental nature, can be seen as sorted lists (repositories). In this aspect, the first phase of TSA follows a hybrid paradigm between TA and NRA (covered in Section 2.4) in that both sorted and random access is possible in the spatial domain, while only sorted accesses are made in the social dimension.

Regarding the termination condition of the first phase, let \(t_p\) be the social distance of the last user encountered by the social search, and \(t_s\) be the Euclidean distance of the last reported spatial NN. The \(f\) value of every user that is not encountered by any of the two searches is lower-bounded by value \(\theta = \alpha \cdot t_p + (1 - \alpha) \cdot t_s\). The first phase of TSA stops when \(\theta \geq f_k\). From the definition of bound \(\theta\) it follows that:

\[ \text{Lemma 1: The final query result may only include users that are already in the interim result } R \text{ or in the candidate set } Q \text{ derived from the first phase of TSA.} \]

Based on Lemma 1, the second phase of TSA ignores any non-encountered users and aims at evaluating (or disqualifying) candidates in \(Q\). The \(f\) value of every candidate is lower-bounded by expression \(\theta' = \alpha \cdot t_p + (1 - \alpha) \cdot t'_d\) where \(t'_d\) is the Euclidean distance of the closest candidate to \(u_q\) (in the spatial domain), while \(t_p\) is as previously defined. If \(\theta' \geq f_k\), TSA can terminate. It is obvious that continuing the NN search in the spatial domain cannot affect \(\theta'\) and would therefore be a waste of computations. Hence, in the second phase of the algorithm only the social search continues.

In the second phase, whenever a vertex is output by the Dijkstra search, we perform the following investigation. If the vertex does not belong to \(Q\), it is ignored (by Lemma 1 it cannot be part of the result). If the vertex is in \(Q\), it is removed from \(Q\), it is evaluated and (should its \(f\) value be smaller than \(f_k\)) it is included into \(R\). In either case, \(\theta'\) is updated to reflect the new \(t_p\). TSA terminates when \(\theta' \geq f_k\).

Algorithm 1 outlines TSA. Lines 7-8 include an important detail. In the first phase, it is possible that a candidate is encountered by Euclidean NN search and subsequently discovered by social search too. In this case, it must be removed from \(Q\), since it is fully evaluated. Leaving such candidates in \(Q\) would unnecessarily burden the second phase.

### Algorithm 1 TSA(G, \(\alpha\), \(k\), \(u_q\))

// Input: \(G\) the social graph  
// \(\alpha\): the preference parameter  
// \(k\): the requested number of users  
// \(u_q\): the query user  
1: Initialize Dijkstra and incremental NN search at \(u_q\)  
2: Initialize result set \(R = \emptyset\); candidate set \(Q = \emptyset\)  
3: while Dijkstra’s heap is non-empty do  
4: Pop next vertex \(v\) en-heap unvisited adj. vertices  
5: if \(f(u_q, u) \leq f_k\) then  
6: Update result \(R\), value \(f_k\), and value \(t_p\) \n7: if \(u \in Q\) then  
8: Remove \(v\) from \(Q\)  
9: Fetch the next nearest neighbor \(u_{nn}\) of \(u\)  
10: if \(u_{nn}\) was not encountered by Dijkstra search then  
11: Insert \(u_{nn}\) into the candidate set \(Q\)  
12: Update value \(t_d\) to \(d(u_q, u_{nn})\)  
13: Set \(\theta = \alpha \cdot t_p + (1 - \alpha) \cdot t_d\)  
14: if \(\theta \geq f_k\) then Break  
15: Set value \(t'_d = \min_{u \in Q} d(u_q, u)\)  
16: Set \(\theta' = \alpha \cdot t_p + (1 - \alpha) \cdot t'_d\)  
17: while \(Q\) is not empty and \(\theta' < f_k\) do  
18: Fetch the next vertex \(v\) from social search  
19: if \(u \in Q\) then \(\triangleright \) \(u\) is the user corresponding to \(v\)  
20: if \(f(u_q, u) \leq f_k\) then  
21: Update result \(R\) and value \(f_k\)  
22: Remove \(u\) from \(Q\) and update value \(t'_d\)  
23: Update value \(t_p\)  
24: Update \(\theta' = \alpha \cdot t_p + (1 - \alpha) \cdot t'_d\)  
25: Return \(R\)

### TSA Example: Figure 2 illustrates eight users \(u_1, u_2, \ldots, u_8\) and \(u_q\). It also includes a table with the Euclidean and social distances of these eight users from \(u_q\), sorted on the former. The order of users in
ascending social distance is \( v_1, v_4, v_8, v_5, v_3, v_2, v_6, v_7 \).

The figure shows only the subgraph of \( G \) that is related to our example of processing an SSRQ query with \( k = 2 \) and \( \alpha = 0.5 \).

TSA first accesses \( u_1 \) in the social domain with \( f \) value 0.1, and places it into the interim result, i.e., \( R = \{ u_1 \} \). Euclidean NN search fetches \( u_1 \), which is ignored because it was previously fully evaluated. TSA then discovers \( u_4 \) (in the social domain) with \( f \) value 0.45 and sets \( R = \{ u_1, u_4 \} \). Next, it encounters \( u_7 \) in the Euclidean domain and inserts it into \( Q \). The social search then fetches \( u_8 \) with score 0.4 and replaces \( u_4 \) in \( R \). The Euclidean search also retrieves \( u_8 \), which is ignored. At this stage, \( t_p = 0.2 \) and \( t_d = 0.6 \), yielding \( \theta = 0.4 \). On the other hand, \( f_k = 0.4 \) which is no larger than \( \theta \), and therefore the first phase culminates.

The second phase starts with \( Q = \{ u_7 \} \). Currently, the lower bound \( \theta' \) (determined by the Euclidean distance of \( u_7 \) and \( t_p \)) is 0.15, i.e., smaller than \( f_k \). TSA continues the social search and iteratively visits new vertices until either \( u_7 \) is found (and evaluated) or \( t_p \) increases enough so that \( \theta' \geq f_k \). In our example, the algorithm terminates when \( u_7 \) is encountered by social search, replacing \( u_8 \) in the result. TSA reports \( R = \{ u_1, u_7 \} \).

**TSA with Quick Combine:** Quick Combine [31] is a popular alternative to round-robin probing for ranked search. This heuristic decides which search (social or spatial) to probe next based on (i) an estimate of how rapidly the distances increase in each domain, and (ii) how large the preference coefficient (\( \alpha \) and \( (1-\alpha) \)) on each domain is. The version of TSA that utilizes Quick Combine in its first phase is denoted as TSA-QC.

**TSA with Landmarks:** An enhancement to TSA is possible if used in conjunction with the landmark approach. Specifically, in a pre-processing stage, a number of vertices in \( G \) are chosen as landmarks using the selection technique in [25] and their distances from every other vertex are computed and recorded. Before the second phase of TSA starts, we use the landmark information to derive a lower bound of \( p(u_q, u) \) for every candidate \( u \in Q \). In turn, this produces a lower bound of the candidate’s \( f \) value (the Euclidean distance of \( u \) is already known). If that lower bound is no smaller than \( f_k \), the candidate is eliminated from \( Q \).

5 **AGGREGATE INDEX SEARCH**

Although TSA and its landmark-aided version utilize tighter bounds than SFA/SPA, they may still visit numerous users who are close in the social graph but far away in the spatial domain, and vice versa. The reason is that the two searches are oblivious of each other, and may be accessing completely different users. This motivates a new approach, called **aggregate index search (AIS)**, which summarizes both social and spatial information into the same index, and runs a unified search on it.

The index is a spatial access method that additionally incorporates (aggregate) social information. Given an index node, we devise a mechanism that provides a lower bound for the \( f \) values of all underlying users. This bound is used in a branch-and-bound process to quickly identify users that are close in both domains. The approach incorporates a novel aggregation of landmark information to provide social summaries at index nodes, as well as optimized graph access techniques and adaptations of landmarks, tailored to the characteristics of SSRQ. We first describe the core of the approach, followed by optimizations in its submodules.

5.1 **Aggregate Index and Query Processing**

The AIS index is a spatial data structure with embedded social information. It could use any spatial access method as a basis (e.g., an R-tree, a k-d-tree, etc). However, we choose a multi-level regular grid because (i) it supports fast location updates [36], [37] and (ii) it facilitates our branch-and-bound SSRQ search (the latter being the reason we prefer it over a single-level grid). Each index node is parent to \( s \times s \) nodes in the immediately lower level, where \( s \) is an integer parameter that determines the partitioning granularity into child nodes. The lowest level contains leaf cells. Each leaf cell \( C \) holds the users that lie inside its spatial extent. Figure 3 illustrates an internal index node which is parent to \( s \times s \) leaf cells, in an example where \( s = 2 \). Note that the multi-level grid does not have to be a tree, i.e., it does not necessarily have a root. We may instead keep only a certain number of its lowest levels¹.

The social summaries kept in the index rely on landmark information. AIS requires that a set of landmarks is used and that each vertex \( v_i \in V \) is associated with a vector including its distances from every landmark. Assuming that there are \( M \) landmarks, we denote the distance between vertex \( v_i \) and the \( j \)-th landmark as \( m_{ij} \). The social summary kept with each cell consists of two vectors, \( \hat{m} \) and \( \hat{m} \), both of length \( M \). Consider first vector \( \hat{m} \). Its \( j \)-th element is symbolized as \( \hat{m}[j] \) and is the maximum path distance between any user in cell \( C \) and the \( j \)-th landmark. Formally, \( \hat{m}[j] = \max_{v_i \in C} m_{ij} \). Similarly, the \( j \)-th element of vector \( \hat{m} \) indicates the minimum path distance between any user in \( C \) and the \( j \)-th landmark, i.e., \( \hat{m}[j] = \min_{v_i \in C} m_{ij} \). This information is propagated upwards, setting the social summaries of internal index nodes according to the full set of users they cover.

¹. This is the case in our experiments, where keeping the lowest two levels from a three-level hierarchy generally yields favorable performance.
Fig. 3. Internal and leaf cells in AIS index

Fig. 4. AIS bound example

To enable a branch-and-bound search in the index we need to derive a lower bound on the $f$ values of users in a (internal or leaf) cell $C$. We first define a lower bound on the spatial domain. Given a query user $u_q$, we denote as $\hat{d}(u_q, C)$ the minimum Euclidean distance between $u_q$ and any point in $C$. If $u_q$ is inside $C$, then $\hat{d}(u_q, C) = 0$. In all other cases, $\hat{d}(u_q, C)$ equals the distance between $u_q$ and the closest point on the boundary of $C$. For example, in Figure 4(a) the minimum distance between $u_1$ and the illustrated cell is determined by the horizontal projection line shown dashed. On the other hand, $\hat{d}(u_q, C)$ equals the length of the diagonal dashed line.

Regarding the social domain, we show how the aggregate landmark information (vectors $\hat{m}$ and $\hat{m}$) can be used to provide a lower bound on $p(v_q, v_i)$ for every $v_i \in C$. Essentially, our technique extends the landmark approach (which was originally proposed for individual vertices) to groups of vertices, i.e., to all vertices under a cell $C$—to the best of our knowledge, it was the first time this is attempted in the literature.

Lemma 2: Given a cell $C$ with social vectors $\hat{m}$ and $\hat{m}$, the following formula provides a lower bound for the shortest path distance between any user in $C$ and the query user $u_q$:

$$\hat{p}(u_q, C) = \max_{1 \leq j \leq M} \begin{cases} \hat{m}[j] - m_{qj} & \text{if } m_{qj} < \hat{m}[j] \\ m_{qj} - \hat{m}[j] & \text{if } m_{qj} > \hat{m}[j] \\ 0 & \text{otherwise} \end{cases}$$

$$\hat{p}(u_q, C) = \max_{1 \leq j \leq M} \begin{cases} \hat{m}[j] - m_{qj} & \text{if } m_{qj} < \hat{m}[j] \\ m_{qj} - \hat{m}[j] & \text{if } m_{qj} > \hat{m}[j] \\ 0 & \text{otherwise} \end{cases}$$

Proof: Consider the $j$-th landmark and assume that $m_{qj} < \hat{m}[j]$. For every $u_i \in C$ the triangular inequality suggests that $p(v_q, v_i) \geq |m_{qj} - m_{qj}|$. Since $m_{qj} < \hat{m}[j] \Rightarrow m_{qj} < m_{qj}$, the inequality becomes $p(v_q, v_i) \geq (\hat{m}[j] - m_{qj})$. By definition, $\hat{m}[j] \leq m_{qj}$ and thus $p(v_q, v_i) \geq (\hat{m}[j] - m_{qj})$. As the second part of the inequality is constant for every $u_i \in C$, we deduce that $\min_{u_i \in C} p(v_q, v_i) \geq (\hat{m}[j] - m_{qj})$. The case for $m_{qj} > \hat{m}[j]$ is symmetric. On the other hand, when $\hat{m}[j] \leq m_{qj} \leq \hat{m}[j]$, we can derive no lower bound based on the $j$-th landmark. Finally, we may use the maximum (i.e., tightest) lower bound derived from any landmark as a lower bound for $\min_{u_i \in C} p(v_q, v_i)$.

Figure 4 illustrates a cell $C$ containing three users and the underlying social graph. Vertex $v_6$ is chosen as the single landmark ($M = 1$), and the graph distances of $v_3, v_4, v_5$ are 4, 3, and 1 respectively. Hence, the aggregate information (social summary) kept for this cell is $\hat{m} = 4$ and $\hat{m} = 1$. By Formula 2, we can directly derive a lower bound of the social distance between any user in $C$ and $v_q \equiv v_1$ (without accessing the specific social or landmark information of the users in $C$), i.e., $\hat{p}(v_1, C) = 1$, which in this example is as tight as it would be if the exact landmark information of individual users was accessed.

Combining the lower bound $\hat{d}(u_q, C)$ for Euclidean distance and $\hat{p}(v_q, C)$ for graph distance, we derive a lower bound of the $f$ value for any user in an (internal or leaf) cell $C$.

Theorem 1: Given a cell $C$ with social vectors $\hat{m}$ and $\hat{m}$, the following formula provides a lower bound for the $f$ value of any user in $C$:

$$\minf(u_q, C) = \alpha \cdot \hat{p}(v_q, C) + (1 - \alpha) \cdot \hat{d}(u_q, C)$$

Proof: From Lemma 2 and the definition of $\hat{d}(u_q, C)$ it follows that $f(u_q, u_i) \geq \minf(u_q, C)$ for each $u_i \in C$.

Theorem 1 and metric $\minf$ pave the way for the AIS processing algorithm. The search starts from the top level of the index. All cells in that level are pushed into a min-heap $H$ with keys equal to their $\minf$ values. The head of the heap is iteratively popped. Depending on the type of the popped item we distinguish three cases:

- If the item is an internal index node, we push into $H$ all its child nodes with their individual $\minf$ values as keys.
- If the item is a leaf cell $C$, we push into $H$ all the users $u_i \in C$ with key equal to $\alpha \cdot \hat{p}(v_q, v_i) + (1 - \alpha) \cdot \hat{d}(u_q, u_i)$, where $\hat{p}(v_q, v_i)$ is the lower bound of social distance $p(v_q, v_i)$ derived from the landmark information of $v_i$.
- If the item is a user $u_q$, we compute its exact social distance from $v_q$ (using a submodule described in Section 5.2) and update the interim result $R$ if its $f$-value is lower than $f_k$.

The algorithm terminates when the head of the heap has a key larger than or equal to the current $f_k$.

Algorithm 2 summarizes the process.

AIS benefits from combining spatial and social information in the same index and promptly identifies users that lie nearby $u_q$ in both domains. In particular,
Algorithm 2 AIS\( (G, \alpha, k, u_q) \)

\[
\begin{align*}
// & & & & & & & & & & & & & & & & & & & & & & & \text{// } \alpha: \text{the preference parameter} \\
// & & & & & & & & & & & & & & & & & & & & & & & \text{// } k: \text{the requested number of users} \\
// & & & & & & & & & & & & & & & & & & & & & & & \text{// } u_q: \text{the query user} \\
2: & & & & & & & & & & & & & & & & & & & & & & & \text{// Push into } H \text{ all top-level index nodes with MINF as key} \\
3: & & & & & & & & & & & & & & & & & & & & & & & \text{// while } H \text{ is not empty and } \text{head’s key is less than } f_k \text{ do} \\
4: & & & & & & & & & & & & & & & & & & & & & & & \text{// Pop the head item of } H \\
5: & & & & & & & & & & & & & & & & & & & & & & & \text{// if popped item is an internal index node then} \\
6: & & & & & & & & & & & & & & & & & & & & & & & \text{// for each child } C \text{ of the node do} \\
7: & & & & & & & & & & & & & & & & & & & & & & & \text{// Push } C \text{ into } H \text{ with key } \text{MINF}(u_q, C) \\
8: & & & & & & & & & & & & & & & & & & & & & & & \text{// else if popped item is a leaf cell } C \text{ then} \\
9: & & & & & & & & & & & & & & & & & & & & & & & \text{// for each user } u \in C \text{ do} \\
10: & & & & & & & & & & & & & & & & & & & & & & & \text{// Push } u \text{ into } H \text{ (key } \alpha \cdot p(v_q, v)+(1-\alpha) \cdot d(u_q, u)) \\
11: & & & & & & & & & & & & & & & & & & & & & & & \text{// else if popped item is a user } u \text{ then} \\
12: & & & & & & & & & & & & & & & & & & & & & & & \text{// Call a submodule to compute } p(v_q, v) \\
13: & & & & & & & & & & & & & & & & & & & & & & & \text{// if } f(u_q, u) < f_k \text{ then} \\
14: & & & & & & & & & & & & & & & & & & & & & & & \text{// Update result } R \text{ and value } f_k \\
\end{align*}
\]

it effectively eliminates nodes, cells and users that are only close in the Euclidean space using the social summaries. On the other hand, for users that are only close in the social graph, it avoids eagerly evaluating them.

The aggregate index supports efficient location updates. When a user \( u_i \) moves, the update is dealt with as a deletion in the old cell and an insertion in the new one\(^2\). We first remove \( u_i \) from the user list of the old cell and update the cell’s social summaries – if a component in \( \hat{m} \) or \( \hat{\mu} \) is due to a landmark distance of \( v_i \), the component is recomputed over the remaining users in the cell. Regarding insertion into the new cell, \( u_i \) is added to the cell’s user list and the landmark distances of \( v_i \) are compared against vectors \( \hat{m} \) and \( \hat{\mu} \). If, say, the \( j \)-th landmark distance of \( v_i \) is larger than the corresponding component of \( \hat{v}_j \), the latter is set to \( m_{ij} \). Symmetrically, if \( m_{ij} \neq \hat{m}_{ij} \) we update \( \hat{m}_{ij} \) to \( m_{ij} \). Should there be an update in the social summary of either the old or the new cell of \( u_i \), it may recursively propagate to upper level nodes in a similar manner. Our index design is primarily concerned with location updates, as the positions of SN users change much more frequently/dynamically than the topology of the network. To deal with the latter (i.e., updates in \( G \)) batching could be used in conjunction with dynamic shortest path algorithms, so that landmark information can be incrementally maintained \cite{38, 39}.

An important remark regards a key principle in designing the index for AIS. The index, as described above, partitions the user set according to Euclidean coordinates. Since social summaries are vectors, it is possible to partition the user set (and thus form an index) in the combined social-spatial space. We attempted this approach with little success. We observed that when a space partitioning method is applied to index the combined space, dead space (empty partitions) tends to cripple performance. On the other hand, data partitioning indices cannot effectively balance the relative significance of the two domains (in their bulk-loading and splitting mechanism) without prior knowledge of \( \alpha \) and also lead to oblong boxes that compromise performance. Finally, this combined-space approach (be it with a space or data partitioning index) suffers from the dimensionality curse, needing to cope with \( M+2 \) dimensions. This imposes a serious limitation on the number of landmarks used.

5.2 Graph Search with Computation Sharing

In this section we describe how AIS computes social distances for users \( u \) popped from its search heap \( H \), i.e., we elaborate on Line 12 of Algorithm 2. First, we decide on the processing paradigm to derive the graph distance. Next, we propose two approaches that enable sharing computations (i.e., reusing information) among the different calls of the submodule for the various evaluated users.

Let \( u \) be the user to be evaluated in Line 12, and \( v \) be the corresponding vertex in the social graph. AIS assumes that landmark information is available for all \( v \in V \) in order to build its index. We utilize this landmark information to accelerate the computation of \( p(v_q, v) \) too. That is, as described in Section 2.3, an \( A^* \) search is applicable – the algorithm proceeds like Dijkstra, but en-heaps encountered vertices with a key incremented by a (landmark-derived) underestimate of their distance to the target vertex. This tends to narrow down the search area of the algorithm. To further enhance performance, instead of a straightforward \( A^* \) execution from \( v_q \) to the target vertex \( v \), we follow the bidirectional search paradigm \cite{25}. The idea in this paradigm is to concurrently execute two \( A^* \) searches: one from \( v_q \) to \( v \) (called forward search) and another from \( v \) to \( v_q \) (reverse search). When the two searches meet, a complete path is derived, which provides a preliminary value for \( p(v_q, v) \). This value does not necessarily correspond to the shortest path but facilitates tightening the search; i.e., if the forward or reverse search de-heaps a vertex with key larger than or equal to this distance, the latter can be safely output as the actual graph distance.

The issue is that the above technique is aimed for vertex-to-vertex computations. In AIS instead, we need to perform multiple graph distance calculations from the same source \( v_q \) to different target vertices. Directly applying the bidirectional approach would perform overlapping searches, i.e., it would unnecessarily repeat part of the work multiple times. Consider for instance Figure 5. Assume that in two consecutive executions of Line 12 in Algorithm 2 we are to obtain the graph distances from \( v_q \) to vertices \( v_{11} \)
and \(v_q\) respectively. After the first bidirectional search (between \(v_q\) and \(v_{11}\)), the forward search accesses all vertices inside the dashed boundary. If another bidirectional search is applied between \(v_q\) and \(v_{6}\), forward search starts from scratch and all vertices inside the boundary (i.e., \(v_2, v_3, v_4\)) are visited again.

This observation motivates the idea to share computations among different graph distance computations, and therefore save processing time. Before presenting specific techniques to achieve this goal, we must stress that (unlike [25]) our bidirectional approach does not use \(A^*\) in both directions. Specifically, while the reverse search is a landmark-based \(A^*\) process, for the forward search we employ a plain Dijkstra search, without any aid from landmarks. The reason will become clear shortly.

We describe two complementary computation sharing approaches. The first is conceptually simple.

**Distance caching:** If the target vertex \(v\) was visited by forward search previously, its exact distance has already been computed and can be reported directly. Continuing the example in Figure 5, if \(v_4\) happens to be the next target vertex, its distance from \(v_q\) is already known because the forward search between \(v_q\) and \(v_{11}\) has previously visited it (the distance of any vertex popped from the Dijkstra heap is immediately derived). Similarly, if \(v\) belongs to a previously reported shortest path, its distance from \(v_q\) is also readily available (when a vertex belongs to the shortest path between a source and a target, its distance from either is directly deduced).

**Forward heap caching:** The second technique reuses the search heap of the forward search. Instead of terminating forward search and re-invoking it from scratch for every target vertex, we maintain its heap contents and re-use them between runs. That is, essentially the forward search only pauses when the graph distance to a target vertex \(v\) is found and its state (i.e., its search heap) is maintained. When the distance of the next target \(v'\) is to be computed, the forward search resumes from the point it stopped, using the already populated heap.

Note that for this optimization to be possible, forward search must be implemented as a Dijkstra process. The rationale is that in Dijkstra’s algorithm the keys used in the search heap are irrelevant to the target vertex, and this exactly is the fact that enables reusing the heap for different target vertices. In an \(A^*\) implementation of forward search, the heap keys would be incremented by (landmark-derived) distance bounds that depend on the specific target vertex each time, making the heap useless for different target vertices.

The distance computation submodule of \(AIS\) with all optimizations is outlined by procedure \Graph{GraphDist} (Algorithm 3). \(H_f\) is the search heap of forward search. \(T\) is a table including previously computed shortest paths. \(H_f\) and \(T\) are global variables, i.e., they are retained between the calls of \Graph{GraphDist} and discarded only when \(AIS\) (the calling process) terminates.

![Forward search](image)

**Algorithm 3** \Graph{GraphDist}(\(G, v_q, v, H_f, T\))

1. if \(v\) was previously visited by forward search then
2. Return the stored distance of \(v\)
3. else if \(v\) appears in any path in \(T\) then
4. Return the stored distance of \(v\)
5. Set \(\text{MinDist} = +\infty\) and \(\text{ShortestPath} = \{}\)
6. Initialize an \(A^*\) process at \(v\) for the reverse search
7. while \(\text{MinDist} > \text{head's key in heap of rev. search}\) do
8. Fetch next vertex \(v_f\) from forward search (from \(H_f\))
9. if \(v_f\) was previously visited by reverse search then
10. if \(p(v_q, v_f) + p(v_f, v) < \text{MinDist}\) then
11. Set \(\text{MinDist} = p(v_q, v_f) + p(v_f, v)\)
12. Update \(\text{ShortestPath}\) accordingly
13. Fetch next vertex \(v_r\) from reverse search
14. if \(v_r\) was previously visited by forward search then
15. if \(p(v_q, v_r) + p(v_r, v) < \text{MinDist}\) then
16. Set \(\text{MinDist} = p(v_q, v_r) + p(v_r, v)\)
17. Update \(\text{ShortestPath}\) accordingly
18. Do not push nodes adj. to \(v_r\) into rev. heap
19. Store \(\text{ShortestPath}\) in \(T\)
20. Return \(\text{MinDist}\)

### 5.3 Improving on Landmark Lower Bounds

Referring to the general \(AIS\) algorithm, as described in Section 5.1, vertices are evaluated in an order dictated by a lower bound of their \(f\) values (see Line 10 in Algorithm 2). This lower bound is derived in part by landmark estimates of the social distance between \(v_q\) and the vertices. It is a known fact that landmarks often produce very loose lower bounds, which may lead \(AIS\) to evaluate target vertices that in reality lie too far from \(v_q\) in the social graph.

Consider for instance Figure 6, and assume that \(v_5\) is used as the landmark. Vertices \(v_q\) and \(v_7\) are almost equi-distant from the landmark, yielding a lowered bound \(\hat{p}(v_q, v_7) = 1\). This is a large underestimate of the actual distance and may lead in evaluating \(v_7\) (via expensive search in \(G\)), although it is actually...
The second condition is to avoid re-inserting a vertex whose graph distance is readily available (because it has been visited by forward search, or because it belongs to an already computed shortest path).

5.4 Graph Distance Pre-computation

Given that social search dominates the processing cost (in all approaches), pre-computing social distances between vertices could possibly improve performance. Materializing all-pair social distances requires a prohibitive amount of storage; for the Foursquare graph in our experiments, which contains around 2 million users, we need roughly 16 TB to store all-pair distances. To alleviate this problem, we could instead materialize for each user the distances of the $t$ socially closest vertices. To utilize the pre-computation, we replace SFA’s Dijkstra component with the pre-computed distance list. In case the algorithm exhausts the list of $t$ social neighbors (without terminating), it falls back to our best method, AIS. Note that pre-computation is applicable to SPA and TSA as well, but with limited success, because these algorithms may encounter a socially distant candidate (outside the pre-computed list) very early in their execution.

6 Experimental Evaluation

In this section we experimentally evaluate the SSRQ techniques proposed in the paper. All methods were implemented in C++ and the experiments conducted on an Intel Core2Duo 2.66GHz CPU machine with 8 GB memory, running on Ubuntu 10.04.

We use two real datasets, Gowalla and Foursquare. Table 2 provides some of their characteristics; the last column indicates their average vertex degree. Gowalla, obtained from snap.stanford.edu, contains 196K users. Foursquare, used in [40], [41], contains 1.88M users. Due to privacy constraints, the location records for some users are unavailable. Thus, we only have access to the historical positions of 54.4% of users in Gowalla and those of 60.3% of users in Foursquare.\(^3\) From the locations available for a user, we assign him/her the one with the highest frequency of visits.

| Name       | $|V|$     | $|E|$        | # locations | Deg. |
|------------|---------|-------------|-------------|------|
| Gowalla    | 196,590 | 1,900,654   | 107,092     | 9.7  |
| Foursquare | 1,880,405| 17,838,254 | 1,133,936   | 9.5  |

Neither of the social networks has explicit information about the edge weights. Based on a common methodology [2], [42], we derive this information from the degrees of vertices incident to the edges. Intuitively, the more the friends of a user, the looser the connection to them, i.e., the larger the edge weight.

\(^3\) Users with no available location are considered infinitely far away from any other user.
Fig. 7. Insights into the nature of SSRO query

Thus, edge weights are set proportionally to the product of degrees of the vertices (users) they connect, i.e., the weight of edge \((v_i, v_j)\) is set to \(\frac{\text{deg}(v_i) \cdot \text{deg}(v_j)}{\text{max_degree}^2}\), where \(\text{deg}(v_i)\) and \(\text{deg}(v_j)\) are the degrees of vertices \(v_i\) and \(v_j\) respectively, and \(\text{max_degree}\) is the maximum vertex degree in the social graph.

Table 3 includes the tested value ranges for the query and system parameters in our setup. In each experiment, unless otherwise stated, the parameters are set to the default values shown in the table. Data and indices for all methods are kept in memory. The main performance factor in our evaluation is run-time, i.e., query processing cost. We also report the pop ratio, computed as \(\frac{|V_{pop}|}{|V|}\), where \(|V_{pop}|\) is the number of vertices popped from the search heaps of the methods. Importantly, the pop ratio measurements are also indicative of performance (specifically, I/O cost) in an alternative setting where the social graph is stored on the disk. Every reported measurement is the average across 1,000 SSRO random queries.

TABLE 3

<table>
<thead>
<tr>
<th>Parameter</th>
<th>Default</th>
<th>Range</th>
</tr>
</thead>
<tbody>
<tr>
<td>size of result (k)</td>
<td>30</td>
<td>10, 20, 30, 40, 50</td>
</tr>
<tr>
<td>preference parameter (\alpha)</td>
<td>0.3</td>
<td>0.1, 0.3, 0.5, 0.7, 0.9</td>
</tr>
<tr>
<td>grid granularity (s)</td>
<td>10</td>
<td>5, 10, 15, 20, 25</td>
</tr>
</tbody>
</table>

We first study our data and the nature of SSRO. In Figure 7(a) we record the number of hops (away from \(v_q\)) where the furthest SSRO result is found. We plot the AVG and MAX of these numbers (across the 1,000 queries run for each \(k\) value tested). Prefix “F.” corresponds to Foursquare and “G.” to Gowalla. We see that results may lie several hops away from \(v_q\), in some cases reaching up to 8 hops.

In Figure 7(b) we investigate the similarity (i) between the SSRO result and the \(k\) Euclidean NNs of \(v_q\) and (ii) between the SSRO result and the \(k\) socially closest users to \(v_q\). In either case, we compute the Jaccard ratio, a standard measure of set similarity [43]. Given two sets, it is defined as the cardinality of their intersection divided by the cardinality of their union; its domain is 0 (unrelated sets) to 1 (identical sets). We plot results for different \(\alpha\) values in Foursquare, i.e., we vary the relative importance of spatial and social proximity. The Jaccard ratio is below 0.1 in all cases, indicating that the nature of SSRO is very different from either social or spatial NN search. Results in Gowalla are similar and omitted for brevity.

Next we compare the different SSRO approaches. SFA and SPA are described in Section 4. TSA is the landmark-aided version of the algorithm in Section 4.2 (we disregard its non-landmark counterpart because it consistently performs worse). TSA-QC is the Quick Combine version of TSA. AIS is the best-performing version of aggregate index search from Section 5 (its different flavors are evaluated later). We finetuned the landmark-based methods with respect to \(M\) (number of landmarks) and set it to 8.

Figure 8 investigates performance for different values of \(k\). Figures 8(a) and 8(b) show that processing in Gowalla is faster than Foursquare – the reason is that SSRO search in Gowalla, regardless of the algorithm chosen, generally reaches fewer users than in Foursquare, as shown in Figure 7(a). The run-time increases with \(k\), because the search area in both the social and the spatial domain expands for larger \(k\).

Just for this experiment, in the run-time charts we include variants SFA-CH, SPA-CH and TSA-CH (of SFA, SPA, TSA) where we replaced the Dijkstra-based social distance computation module with the state-of-the-art pre-computation-based technique for shortest path computation, CH, from [44]. These variants are slower than vanilla SFA/SPA/TSA, because (i) CH is better suited to low-degree graphs (such as planar graphs) and (ii) in vanilla methods, shortest paths are produced incrementally (they all have \(v_q\) as source), thus essentially sharing/reusing computations.

Turning to the relative performance of our algorithms, Figures 8(c) and 8(d) verify that SFA and SPA process more vertices than TSA, due to their looser termination conditions. However, the difference in run-time is not as wide as in pop ratio, the reason being TSA’s overhead in maintaining two bounds (one spatial and one social). TSA-QC performs better.
than TSA in Gowalla when \( k \) is small but is slower than TSA in Foursquare in all settings. We suspect that this is due to the different social/spatial distributions in the two datasets. AIS visits fewer than 6% and 3% of the vertices in Gowalla and Foursquare respectively, while the other approaches visit more than 90% in most cases. This demonstrates that the aggregate index search paradigm vastly reduces the number of expanded vertices (especially in large SNs), which implies significantly shorter processing time.

In Figure 9 we test different values of \( \alpha \), i.e., different weighing of social versus spatial proximity. SFA examines vertices in increasing social distance order, which implies that for large \( \alpha \) the first few processed vertices are highly likely to already produce the result. TSA and TSA-QC are also more socially-led (than spatially), since their second phase relies entirely on graph search, thus benefiting from a large \( \alpha \). On the other hand, it is spatially-led and hence its performance worsens with \( \alpha \), albeit only slightly. Importantly, our most advanced method, AIS, is robust to \( \alpha \) and retains its clear lead over alternatives.

Aggregate index search provides a flexible framework, which can be equipped with different techniques and optimizations. Here we evaluate its three most representative versions: (i) AIS-BID is a direct implementation of Algorithm 2 using the bidirectional search in [25] for graph distance computations and no other optimization; (ii) AIS uses all optimizations except the delayed evaluation strategy; and (iii) AIS uses all optimizations.

In Figure 10 we compare these algorithms for various values of \( k \). The behavior of AIS-BID demonstrates that, although the search technique proposed in [25] is more efficient than other flavors of bidirectional search, it is unable to yield favorable performance without our further enhancements. This fact is also supported by the pop ratio charts. The comparison between AIS and AIS reveals that the delayed evaluation mechanism improves performance, albeit to a moderate degree.

In Figure 11 we evaluate the pre-computation technique (from Section 5.4) against AIS. We present runtime versus \( t \), i.e., versus the number of cached social neighbors per user. Pre-computation yields minor improvements in the larger graph (Foursquare) but significant in the smaller one (Gowalla). The reason is that, as shown in Figure 7(a), in Foursquare search expands more hops away from \( v_q \), thus being more likely to reach a vertex outside the cache.

In Figure 12, we measure the effect of \( s \), i.e., the granularity of the grid index, on SPA, AIS-BID, AIS, and AIS. Recall that a larger \( s \) implies more cells with smaller size each. This parameter affects performance in two conflicting ways: (i) as \( s \) grows, more cells lie in the vicinity of the query user and therefore more computations are needed to calculate distance bounds for them; (ii) on the other hand, smaller grid cells provide more accurate summaries (be them Euclidean or social) about the underlying users, and increase the effectiveness of pruning. Value \( s = 10 \) strikes a favorable balance between these factors, although the methods are not very sensitive to it.
Fig. 13. Experiments with Twitter

For generality, in Figure 13 we use a real dataset, Twitter, with higher average degree than our default datasets (its average degree is 57.7). It contains 124K Twitter users in Singapore who made geo-tagged tweets in 2013; a user’s location is derived from his/her latest tweet. The charts (versus $k$ and $\alpha$) show similar trends to our default datasets. A difference is that the run-time increases less sharply with $k$, because the larger degree implies that more candidates (users) are reachable with fewer hops from $u_q$.

Finally, we generate synthetic data to examine parameters we cannot control in the real SNs. In Figure 14(a), we generate data with different correlations between the social and spatial distances. We use the social distances derived from Foursquare, but assign to users artificial locations as follows. For each $v_q$, we generate the spatial distance of user $u$ from $u_q$ by formula $\tilde{d} = \rho \cdot p(v_q, v) + \epsilon$, where $\epsilon$ is a random number in range $[-0.15, 0.15]$ and $\rho$ is 1 (for positive-correlation dataset) or -1 (for negative-correlation dataset). Based on the generated $\tilde{d}$ (normalized in the [0,1] range), we place the user at a random point on the circle with radius $\tilde{d}$ from $u_q$. We also generate a third dataset, where the spatial locations of users are randomly permuted, so as to create a dataset with independent correlation between social and spatial proximity.

All algorithms require the shortest time when data are positively correlated and the longest when they are negatively correlated. In the positive correlation case, users that are socially near $v_q$ tend to also lie close by in the Euclidean space. Hence, search encounters the top-k users early on and terminates quicker. The situation is reversed for negatively correlated data, because socially near users are spatially far, and vice versa, implying that the top-k users tend to lie far from the query in either of the two domains, if not in both. AIS is the method of choice in all cases, furthermore demonstrating robustness to the type of correlation between spatial and social distance.

In Figure 14(b), we show performance for different SN sizes. Starting with Foursquare as a basis, we extracted from it SNs of different sizes using the structure-preserving Forest Fire Sampling technique [45]. As the number of SN vertices is tripled from 0.6M to 1.8M, the running time of all algorithms increases almost linearly, with AIS scaling much more gracefully than competitors.

Fig. 14. Experiments with synthetic data

7 CONCLUSION

We study a query type that captures proximity in the combined social-spatial domain. Our most efficient algorithm relies on an aggregate index that supports estimates of combined proximity. Experiments on actual social networks demonstrate that it is highly scalable and robust. A direction for future work is joint social and spatial processing on networks stored in a distributed manner.

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REFERENCES


