

# Classifying $\mathcal{ELH}$ Ontologies in SQL Databases

Vincent Delaitre<sup>1</sup> and Yevgeny Kazakov<sup>2</sup>

<sup>1</sup> École Normale Supérieure de Lyon, Lyon, France  
vincent.delaitre@ens-lyon.org

<sup>2</sup> Oxford University Computing Laboratory, Oxford, England  
yevgeny.kazakov@comlab.ox.ac.uk

**Abstract.** The current implementations of ontology classification procedures use the main memory of the computer for loading and processing ontologies, which soon can become one of the main limiting factors for very large ontologies. We describe a secondary memory implementation of a classification procedure for  $\mathcal{ELH}$  ontologies using an SQL relational database management system. Although secondary memory has much slower characteristics, our preliminary experiments demonstrate that one can obtain a comparable performance to those of existing in-memory reasoners using a number of caching techniques.

## 1 Introduction

The ontology languages OWL and OWL 2 based on description logics (DL) are becoming increasingly popular among ontology developers, largely thanks to the availability of *ontology reasoners* which provide automated support for many ontology development tasks. One of the key ontology development task is *ontology classification*, the goal of which is to compute a hierarchical representation of the subsumption relation between classes of the ontology called *class taxonomy*.

The popularity of OWL and efficiency of ontology reasoners has resulted in the availability of large ontologies such as Snomed CT containing hundreds of thousands of classes. Modern ontology reasoners such as CEL and FaCT++ can classify Snomed CT in a matter of minutes, however scaling these reasoners to ontologies containing millions of classes is problematic due to their high memory consumption. For example, the classification of Snomed CT in CEL and FaCT++ requires almost 1GB of the main memory. In this paper we describe a secondary-memory implementation of the classification procedure for the DL  $\mathcal{ELH}$ —the fragment of OWL used by Snomed CT—in SQL databases. Our reasoner can classify Snomed CT in less than 20 minutes using less than 32MB of RAM.

To the best of our knowledge, secondary-memory (database) algorithms and optimizations for ontology reasoning have been studied only very recently. Lutz et al. have proposed a method for conjunctive query answering over  $\mathcal{EL}$  ontologies using databases [1], but the main focus of their work is on optimizing query response time once the ontology is “compiled” into a database. The IBM SHER system ([www.alphaworks.ibm.com/tech/sher](http://www.alphaworks.ibm.com/tech/sher)) has a “db-backed” module, which presumably can perform secondary-memory reasoning in  $\mathcal{EL}^+$ , but currently not much information is available about this module.

**Table 1.** The syntax and semantics of  $\mathcal{ELH}$

Name	Syntax	Semantics
Concepts:		
atomic concept	$A$	$A^{\mathcal{I}}$ (given)
top concept	$\top$	$\Delta^{\mathcal{I}}$
conjunction	$C \sqcap D$	$C^{\mathcal{I}} \cap D^{\mathcal{I}}$
existential restriction	$\exists r.C$	$\{x \in \Delta^{\mathcal{I}} \mid \exists y \in \Delta^{\mathcal{I}} : \langle x, y \rangle \in r^{\mathcal{I}} \wedge y \in C^{\mathcal{I}}\}$
Axioms:		
concept inclusion	$C \sqsubseteq D$	$C^{\mathcal{I}} \subseteq D^{\mathcal{I}}$
role inclusion	$r \sqsubseteq s$	$r^{\mathcal{I}} \subseteq s^{\mathcal{I}}$

## 2 Preliminaries

In this section we introduce the lightweight description logic  $\mathcal{ELH}$  and the classification procedure for  $\mathcal{ELH}$  ontologies [2].

### 2.1 The Syntax and Semantics of $\mathcal{ELH}$

A description logic *vocabulary* consists of countably infinite sets  $\mathbf{N}_C$  of *atomic concepts*, and  $\mathbf{N}_R$  of *atomic roles*. The syntax and semantics of  $\mathcal{ELH}$  is summarized in Table 1. The set of  $\mathcal{ELH}$  *concepts* is recursively defined using the constructors in the upper part of Table 1, where  $A \in \mathbf{N}_C$ ,  $r \in \mathbf{N}_R$ , and  $C, D$  are concepts. A *terminology* or *ontology* is a set  $\mathcal{O}$  of axioms in the lower part of Table 1 where  $C, D$  are concepts and  $r, s \in \mathbf{N}_R$ . We use *concept equivalence*  $C \equiv D$  as an abbreviation for two concept inclusion axioms  $C \sqsubseteq D$  and  $D \sqsubseteq C$ .

The semantics of  $\mathcal{ELH}$  is defined using interpretations. An *interpretation* is a pair  $\mathcal{I} = (\Delta^{\mathcal{I}}, \cdot^{\mathcal{I}})$  where  $\Delta^{\mathcal{I}}$  is a non-empty set called *the domain of the interpretation* and  $\cdot^{\mathcal{I}}$  is the *interpretation function*, which assigns to every  $A \in \mathbf{N}_C$  a set  $A^{\mathcal{I}} \subseteq \Delta^{\mathcal{I}}$ , and to every  $r \in \mathbf{N}_R$  a relation  $r^{\mathcal{I}} \subseteq \Delta^{\mathcal{I}} \times \Delta^{\mathcal{I}}$ . The interpretation is extended to concepts according to the right column of Table 1. An interpretation  $\mathcal{I}$  *satisfies an axiom*  $\alpha$  (written  $\mathcal{I} \models \alpha$ ) if the respective condition to the right of the axiom in Table 1 holds;  $\mathcal{I}$  is a *model of an ontology*  $\mathcal{O}$  (written  $\mathcal{I} \models \mathcal{O}$ ) if  $\mathcal{I}$  satisfies every axiom in  $\mathcal{O}$ . We say that  $\alpha$  is a (*logical*) *consequence* of  $\mathcal{O}$ , or *is entailed* by  $\mathcal{O}$  (written  $\mathcal{O} \models \alpha$ ) if every model of  $\mathcal{O}$  satisfies  $\alpha$ .

*Classification* is a key reasoning problem for description logics and ontologies, which requires to compute the set of *direct subsumptions*  $A \sqsubseteq B$  between atomic concepts that are entailed by  $\mathcal{O}$ .

### 2.2 Normalization of $\mathcal{ELH}$ Ontologies

Normalization is a preprocessing stage that eliminates nested occurrences of complex concept from  $\mathcal{ELH}$  ontologies using auxiliary atomic concepts and axioms. The resulting ontology will contain only axioms of the forms:

$$A \sqsubseteq B, \quad A \sqcap B \sqsubseteq C, \quad A \sqsubseteq \exists r.B, \quad \exists s.B \sqsubseteq C, \quad r \sqsubseteq s, \quad (1)$$

$$\begin{array}{lll}
\text{IR1 } \frac{}{A \sqsubseteq A} & \text{IR2 } \frac{}{A \sqsubseteq \top} & \text{CR1 } \frac{A \sqsubseteq B}{A \sqsubseteq C} : B \sqsubseteq C \in \mathcal{O} \\
\text{CR2 } \frac{A \sqsubseteq B \quad A \sqsubseteq C}{A \sqsubseteq D} : B \sqcap C \sqsubseteq D \in \mathcal{O} & \text{CR3 } \frac{A \sqsubseteq B}{A \sqsubseteq \exists r.C} : B \sqsubseteq \exists r.C \in \mathcal{O} & \\
\text{CR4 } \frac{A \sqsubseteq \exists r.B}{A \sqsubseteq \exists s.B} : r \sqsubseteq s \in \mathcal{O} & \text{CR5 } \frac{A \sqsubseteq \exists s.B \quad B \sqsubseteq C}{A \sqsubseteq D} : \exists s.C \sqsubseteq D \in \mathcal{O} & 
\end{array}$$

**Fig. 1.** The Completion Rules for  $\mathcal{ELH}$

where  $A, B, C \in \mathbf{N}_C$  and  $r, s \in \mathbf{N}_R$ . Given an  $\mathcal{ELH}$  concept  $C$ , let  $\text{sub}(C)$  be the set of *sub-concepts* of  $C$  recursively defined as follows:  $\text{sub}(A) = \{A\}$  for  $A \in \mathbf{N}_C$ ,  $\text{sub}(\top) = \{\top\}$ ,  $\text{sub}(C \sqcap D) = \{C \sqcap D\} \cup \text{sub}(C) \cup \text{sub}(D)$ , and  $\text{sub}(\exists r.C) = \{\exists r.C\} \cup \text{sub}(C)$ . Given an  $\mathcal{ELH}$  ontology  $\mathcal{O}$ , define the set of *negative / positive / all concepts in  $\mathcal{O}$*  by respectively  $\text{sub}^-(\mathcal{O}) = \{\text{sub}(C) \mid C \sqsubseteq D \in \mathcal{O}\}$ ,  $\text{sub}^+(\mathcal{O}) = \{\text{sub}(D) \mid C \sqsubseteq D \in \mathcal{O}\}$ , and  $\text{sub}(\mathcal{O}) = \text{sub}^-(\mathcal{O}) \cup \text{sub}^+(\mathcal{O})$ . For every  $C \in \text{sub}(\mathcal{O})$  we define a function  $\text{nf}(C)$  as follows:  $\text{nf}(A) = A$ , if  $A \in \mathbf{N}_C$ ,  $\text{nf}(\top) = \top$ ,  $\text{nf}(C \sqcap D) = A_C \sqcap A_D$ , and  $\text{nf}(\exists r.C) = \exists r.A_C$ , where  $A_C$  and  $A_D$  are fresh atomic concepts introduced for  $C$  and  $D$ .

The result of applying *normalization* to  $\mathcal{O}$  is the ontology  $\mathcal{O}'$  consisting of the following axioms: (i)  $A_C \sqsubseteq A_D$  for  $C \sqsubseteq D \in \mathcal{O}$ , (ii)  $r \sqsubseteq s$  for  $r \sqsubseteq s \in \mathcal{O}$ , (iii)  $\text{nf}(C) \sqsubseteq A_C$  for  $C \in \text{sub}^-(\mathcal{O})$ , and (iv)  $A_D \sqsubseteq \text{nf}(D)$  for  $D \in \text{sub}^+(\mathcal{O})$ , where the axioms of the form  $A \sqsubseteq B \sqcap C$  are replaced with a pair of axioms  $A \sqsubseteq B$  and  $A \sqsubseteq C$ . It has been shown [2] that this transformation preserves all original subsumptions between atomic concepts in  $\mathcal{O}$ .

### 2.3 Completion Rules

In order to classify a normalized  $\mathcal{ELH}$  ontology  $\mathcal{O}$ , the procedure applies the completion rules in Fig. 1. The rules derive new axioms of the form  $A \sqsubseteq B$  and  $C \sqsubseteq \exists r.D$  which are logical consequences of  $\mathcal{O}$ , where  $A, B, C$ , and  $D$  are atomic concepts or  $\top$ , and  $r, s$  atomic roles. Rules **IR1** and **IR2** derive trivial axioms for  $A \in \mathbf{N}_C \cap \text{sub}(\mathcal{O})$ . The remaining rules are applied to already derived axioms and use the normalized axioms in  $\mathcal{O}$  as side conditions. The completion rules are applied until no new axiom can be derived, i.e., the resulting set of axioms is closed under all inference rules. It has been shown [2] that the rules **IR1–CR5** are *sound* and *complete*, that is, a concept subsumption  $A \sqsubseteq B$  is entailed by  $\mathcal{O}$  if and only if it is derivable by these rules.

## 3 Implementing $\mathcal{ELH}$ Classification in a Database

In this section we describe the basic idea of our database implementation for the  $\mathcal{ELH}$  classification procedure, the performance problems we face with, and our solutions to these problems. Although our presentation is specific to the MySQL syntax, the procedure can be implemented in any other SQL database system.



role inclusions  $r \sqsubseteq s$  in  $\mathcal{O}$ . Table `ax_conj` is obtained from the rows of table `conj` with negative flag. Likewise, tables `ax_exis_pos` and `ax_exis_neg` are obtained from the rows of `exis` with respectively positive and negative flags.

Once the tables for normal form of the axioms are computed, it is possible to apply inference rules in Fig. 1 using SQL joins to derive new subsumptions. In the next sections we describe both steps of the classification procedure in detail.

## 3.2 Normalization

The first problem appears when trying to assign the same ids to the same concept occurring in the ontology. Since our goal is to design a scalable procedure which can deal with very large ontologies, we cannot load the whole ontology into the main memory before assigning ids. Hence all tables in Fig. 2 should be constructed “on the fly” while reading the ontology.

We have divided every table in Fig. 2 in two parts: the first is constructed after reading axiom (2), the second is constructed after reading axiom (3), except for table `ax_r_incl` which is constructed after reading axiom (4). Suppose we have just processed axiom (2) and are now reading axiom (3). The concept `Heart` did not occur before, so we need to assign it with a fresh `id = 6` and add a row into the table `at_conc`. The concept `Organ`, however, has been added before and we need to reuse the old `id = 2`. Thus table `at_conc` acts as a lookup table for atomic concepts: if a new atomic concept occurs in this table then we reuse its `id`, otherwise, we introduce a fresh `id` and add a row into this table. This strategy works quite well for in-memory lookup. However it is hopelessly slow for external memory lookup due to the considerably slow disc access time. Moreover, since executing a query in a database management system, such as MySQL, involves an overhead on opening connection, performing transaction, and parsing the query, executing a query one by one for every atomic concept is hardly practical.

In order to solve this problem, we use temporary in-memory tables to buffer the newly added concepts. We assign fresh `ids` regardless of whether the concept has been read before or not, and later restore uniqueness of the `ids` using a series of SQL queries. The tables are similar to those used for storing original `ids`, except that the tables for conjunctions and existential restrictions have an additional column `depth` representing the nesting depth of the concepts. In addition, there is a new table `map` which is used for resolving `ids` in case of duplicates. The sizes of temporary tables can be tuned for best speed/memory performance.

Fig. 3 presents the contents of the temporary tables after reading axiom (3) assuming that axiom (2) is already processed. In order to resolve `ids` for all buffered atomic concept we perform the following SQL queries:

```
1: INSERT IGNORE INTO at_conc SELECT * FROM tmp_at_conc;
2: INSERT INTO map SELECT tmp_at_conc.id, at_conc.id
   FROM tmp_at_conc JOIN at_conc USING (name);
```

The first query inserts all buffered atomic concepts into the main table; duplicate insertions are ignored using a uniqueness constraint on the field `name` in table `at_conc`. The second query creates a mapping between temporary `ids` and original

tmp_at_conc		tmp_at_role		tmp_conj					map			
name	id	name	id	A	□	B	pos	neg	id	depth	tmp.id	orig.id
Heart	6	belongsTo	8	9/4	10	✓	11	1			7	2
Organ	7			7/2	12	✓	13	2			9	4
MuscularSystem	9											
CirculatorySystem	10											
tmp_exis												
				∃	r.	B	pos	neg	id	depth		
							8	11	✓	12	1	

**Fig. 3.** Temporary tables after reading axiom (3). The entries *id1/id2* represent ids before/after mapping temporary ids to original ids using table **map**.

ids to be used for replacement of the ids in complex concepts containing atomic ones. The query can be optimized to avoid trivial mappings.

Replacement of ids and resolving of duplicate ids in complex concepts is done recursively over the depth  $d$  of concepts starting from  $d = 1$ . Processing conjunctions of the depth  $d$  is done using the following SQL queries:

- 1: UPDATE tmp\_conj SET A = map.orig\_id WHERE tmp\_conj.A = map.tmp\_id;
- 2: UPDATE tmp\_conj SET B = map.orig\_id WHERE tmp\_conj.B = map.tmp\_id;
- 3: INSERT INTO conj SELECT \* FROM tmp\_conj WHERE tmp\_conj.depth =  $d$   
ON DUPLICATE KEY UPDATE pos = (conj.pos || tmp\_conj.pos),  
neg = (conj.neg || tmp\_conj.neg);
- 4: INSERT INTO map SELECT tmp\_conj.id, conj.id FROM tmp\_conj JOIN conj  
USING (A, B) WHERE tmp\_conj.depth =  $d$ ;

The first two queries restore original ids for columns  $A$  and  $B$ . The resulting rows with depth  $d$  are then inserted into the main conjunction table, or update the polarities in case of duplicates (line 3). Finally, new mappings between ids for conjunctions of depth  $d$  are added (line 4). The ids for existential restrictions are resolved analogously.

### 3.3 Completion under Rules **CR1** and **CR2**

We apply the completion rules from Fig. 1 in the order of priority in which they are listed. That is, we exhaustively apply rule **CR1** before applying rule **CR2**, and perform closure under the rules **CR1** and **CR2** before applying the remaining rules **CR3–CR5**. This decision stems from an observation that closure under rules **CR1** and **CR2** can be computed efficiently using a temporary in-memory table. Indeed, the closure under rules **CR1** and **CR2** of the form  $A \sqsubseteq X$  for a fixed  $A$  can be computed independently of other subsumptions since the premises and the conclusions of these rules share the same concept  $A$ . The main idea is to use a temporary in-memory table to compute a closure for a bounded number of concepts  $A$ , and then output the union of the results into the main on-disc table.

Let **tmp\_subs** be a temporary in-memory table with columns  $A, B$  representing subsumptions between  $A$  and  $B$ , and a column **step** representing the step at which each subsumption has been added. We use a global variable **step** to indicate that rule **CR1** has been already applied for all subsumptions in **tmp\_subs** with

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**Procedure 1** Computing closure under rules **CR1** and **CR2**

---

**close\_CR1()**

---

```
1: REPEAT
2:   SET @size = (SELECT COUNT(*) FROM tmp_subs);
3:   INSERT IGNORE INTO tmp_subs
      SELECT tmp_subs.A, ax_c_incl.B, (step + 1)
      FROM tmp_subs JOIN ax_c_incl ON tmp_subs.B = ax_c_incl.A
      WHERE tmp_subs.step = step;
4:   SET step = step + 1;
5: UNTIL @size = (SELECT COUNT(*) FROM tmp_subs)  -- nothing has changed
6: END REPEAT;
```

---

**close\_CR1\_CR2()**

---

```
7: REPEAT
8:   SET @conj_step = step;
9:   CALL close_CR1();
10:  SET @size = (SELECT COUNT(*) FROM tmp_subs);
11:  INSERT IGNORE INTO tmp_subs SELECT t1.A, ax_conj.C, (step + 1)
      FROM JOIN (tmp_subs AS t1, tmp_subs AS t2, ax_conj)
      ON (t1.B = ax_conj.A AND t2.B = ax_conj.B)
      WHERE (t1.step > @conj_step OR t2.step > @conj_step);
12:  SET step = step + 1;
13: UNTIL @size = (SELECT COUNT(*) FROM tmp_subs)  -- nothing has changed
14: END REPEAT;
```

---

smaller values of `tmp_subs.step`. Then the closure of `tmp_subs` under **CR1** can be computed using the function `close_CR1()` of Procedure 1. The function repeatedly performs joins of the temporary table `tmp_subs` with the table containing concept inclusions `ax_c_incl` and inserts the result back into `tmp_subs` with the increased step. We assume that `tmp_subs` has a uniqueness constraint on the pair  $(A, B)$ , so that duplicate subsumptions are ignored.

The same idea can be used to perform closure under rule **CR2** with the only difference that **CR2** has two premises and therefore requires a more complex join. Since **CR2** is thus more expensive than **CR1**, we execute it with a lower priority. The closure under both rules **CR1** and **CR2** is done using the function `close_CR1_CR2()` of Procedure 1. Here we use a temporary variable `@conj_step` to remember the last time we applied rule **CR2**. After performing the closure under **CR1** (line 9), we make a join on two copies `tmp_subs` and `ax_conj` on new rows (line 11).

### 3.4 Completion under Rules **CR3**–**CR5**

Direct execution of rules **CR3**–**CR5** requires performing many complicated joins. We combine these rules into one inference rule with multiple side conditions:

$$\frac{A \sqsubseteq B}{\exists r.A \sqsubseteq \exists s.B} : r \sqsubseteq s \in \mathcal{O}, \exists r.A \in \text{sub}^+(\mathcal{O}), \exists s.B \in \text{sub}^-(\mathcal{O}) \quad (5)$$

---

**Procedure 2** Saturation under rules **IR1–CR5**.

---

**add\_exis\_incl()**

```
1: TRUNCATE exis_incl;          -- the table used to store new subsumptions
2: INSERT INTO exis_incl SELECT ax_exis_pos.A, ax_exis_neg.C
   FROM JOIN (ax_exis_pos, ax_exis_neg, ax_r_incl, tmp_subs)
   ON (ax_exis_pos.B = tmp_subs.A AND ax_exis_neg.B = tmp_subs.B
       ax_exis_pos.r = ax_r_incl.r AND ax_exis_neg.s = ax_r_incl.s);
3: DELETE FROM exis_incl WHERE exis_incl.A = exis_incl.B;
4: DELETE FROM exis_incl USING exis_incl JOIN ax_c_incl USING (A, B);
5: INSERT INTO ax_c_incl SELECT exis_incl.A, exis_incl.B FROM exis_incl;
```

---

**saturate(N)** -- *N* is a parameter for temporary subsumption table

---

```
6: INSERT INTO queue SELECT at_conc.id, true FROM at_conc;
7: INSERT INTO queue SELECT ax_exis_pos.B, true FROM ax_exis_pos;
8: INSERT INTO subs SELECT queue.id, queue.id FROM queue;      -- rule IR1
9: INSERT INTO subs SELECT queue.id, top_id FROM queue;        -- rule IR2
10: REPEAT
11:  TRUNCATE tmp_queue;    -- to store the first N unprocessed elements
12:  INSERT INTO tmp_queue SELECT queue.id FROM queue
   WHERE queue.flag = true LIMIT N;
13:  UPDATE queue, tmp_queue SET queue.flag = false
   WHERE queue.id = tmp_queue.id;
14:  TRUNCATE tmp_subs; SET step = 0;
15:  INSERT INTO tmp_subs SELECT subs.A, subs.B, step           -- fetching
   FROM subs JOIN tmp_queue ON subs.A = tmp_queue.id; -- to process
16:  CALL close_CR1_CR2();      -- close under rules CR1 and CR2
17:  INSERT INTO subs SELECT tmp_subs.A, tmp_subs.B FROM tmp_subs
   WHERE tmp_subs.step > 0;    -- insert back only new subsumptions
18:  CALL add_exis_incl();    -- find and add new existential subsumptions
19:  UPDATE queue, subs, exis_incl SET queue.flag = true
   WHERE (queue.id = subs.A AND subs.B = exis_incl.A);
20: UNTIL (SELECT COUNT(*) FROM tmp_queue) = 0      -- nothing to process
21: END REPEAT;
```

---

Rule (5) derives new inclusions between (ids of) existentially restricted concepts occurring in the ontology using previously derived subsumptions. The main idea is to repeatedly derive these new inclusions, adding them into table **ax\_c\_incl**, and performing incremental closure of the letter under rules **CR1** and **CR2**.

Inference (5) is implemented using the function **add\_exis\_incl()** of Procedure 2. The conclusion of the inference is computed using a complex join query (line 2) and stored in a new table **exis\_incl**. The result is subsequently filtered by removing trivial inclusions (line 3), and inclusions that occur in table **ax\_c\_incl** (line 4). The new subsumptions are added into **ax\_c\_incl** (line 5).

Function **saturate(N)** implements our overall strategy of rule applications. Table **queue** stores all concepts *A* for which subsumptions  $A \sqsubseteq X$  are to be computed as indicated in column **flag**. It is sufficient to consider only atomic concepts (line 6), and concepts occurring under positive existential restrictions

(line 7). The computed subsumptions are saved in table `subs`, which is initialized according to rules `IR1` and `IR2` (lines 8-9). The concepts in `queue` are processed by portions of  $N$  elements ( $N$  is the given parameter) using a temporary table `tmp_queue`. At the beginning of every iteration, table `tmp_queue` is filled with first  $N$  unprocessed elements from `queue` (line 12), which are then labeled as processed (line 13). The table `tmp_subs` is filled with the corresponding subsumptions from `subs` (line 15), closed under rules `CR1` and `CR2` (line 16), and new subsumptions are inserted back into `subs` (line 17). After that, new inclusions between existential restrictions are derived using (5) (line 18), and elements  $A$  in `queue` for which new inclusions can yield new subsumptions, are labeled as unprocessed (line 19).

### 3.5 Transitive Reduction

The output of the classification algorithm is not the set of all subsumptions between sub-concepts of an ontology, but a *taxonomy* which contains only *direct* subsumptions between atomic concepts. In order to compute the taxonomy, the set of all subsumptions between atomic concepts should be transitively reduced. Transitive reduction of a transitive subsumption relation can be done by applying one step of transitive closure and marking the resulting relations as “not-direct”, thus finding the remaining set of “direct” subsumptions. Although this can be easily implemented in databases with just one join, we found that this approach has a poor performance because it requires to make a large number of on-disc updates, namely, marking subsumptions as non-direct. In contrast, the number of direct subsumptions is usually much smaller. A solution to this problem involves the usage of a temporary in-memory table. We repeatedly fetch into the table all subsumption relations  $A \sqsubseteq X$  for a bounded number of atomic concepts  $A$ , perform transitive reduction according to the method described above, and output the direct subsumptions into the on-disk taxonomy. This algorithm can be also extended to handle equivalence classes of atomic concepts.

## 4 Experimental Evaluation

We have implemented a prototype reasoner DB<sup>3</sup> in MySQL according to the procedure described in Section 3 (with some small additional optimizations).

In order to evaluate the performance of the reasoner and compare it with existing ontology reasoners, we have performed a series of experiments with four large bio-medical ontologies of various sizes and complexity. The Gene Ontology (GO) ([www.geneontology.org](http://www.geneontology.org)) and National Cancer Institute (NCI) ontology ([www.cancer.gov](http://www.cancer.gov)) are quite big ontologies containing respectively 20,465 and 27,652 classes. Galen<sup>-</sup> containing 23,136 classes is obtain from a version of the OpenGalen ontology ([www.co-ode.org/galen](http://www.co-ode.org/galen)) by removing role functionalities, transitivity, and inverses. The largest tested ontology Snomed based on Snomed CT ([www.ihtsdo.org](http://www.ihtsdo.org)) contains 315,489 classes. We ran the experiments on a

<sup>3</sup> The reasoner is available open source from [db-reasoner.googlecode.com](http://db-reasoner.googlecode.com)

**Table 2.** Time profiles for classification. Time is in seconds.

(a) The stages of the classification procedure					(b) Completion for different N				
Action	NCI	GO	Galen <sup>-</sup>	Snomed	N=	NCI	GO	Galen <sup>-</sup>	Snomed
Loading/Preprocessing	17.85	5.99	23.41	127.51	1000	6.57	8.85	39.12	1067.78
Completion	5.78	7.29	53.13	783.30	2000	6.19	7.65	38.97	844.56
Transitive reduction	10.32	6.10	21.44	249.23	5000	5.78	7.29	53.14	783.30
Formating output	1.56	0.98	2.88	23.76	10000	5.29	6.80	45.78	889.93
Total	35.51	20.36	100.86	1183.80	15000	4.86	6.46	42,35	965.95

**Table 3.** Comparison with other reasoners. Time is in seconds.

Reasoner	NCI	GO	Galen <sup>-</sup>	Snomed
DB	35.51	20.36	100.86	1183.80
CB	7.64	1.23	3.36	45.17
CEL v.1.0	3.60	1.02	169.23	1302.18
FaCT++ v.1.3.0	4.60	10.50	—	965.84
HermiT v.0.9.3	70.23	92.76	—	—

PC with a 2GHz Intel® Core™ 2 Duo processor, a 5400 RPM 2.5" hard drive, and 4GB RAM operated by Ubuntu Linux v.9.04 with MySQL v.5.1.31.

In Table 2 we present detailed timings for classification of the tested ontologies using DB. Table 2(a) lists timings for various stages of the classification procedure described in Section 3. As we can see, for NCI and GO a considerable time is spent on preprocessing and transitive reduction, whereas for Galen<sup>-</sup> and Snomed most time is spent on completion. The reason could be that for NCI and GO inference (5) does not result in many new inclusions. In Table 2(b) we analyze the impact of different values of the parameter N on the times for the completion stage (see Procedure 2). We see that the timings do not differ significantly. In all other experiments, we fix N=5000, which does not result in main memory consumption of MySQL server more than 32MB.

In Table 3, we compare the performance of our reasoner with existing in-memory ontology reasoners CB ([cb-reasoner.googlecode.com](http://cb-reasoner.googlecode.com)), CEL ([inf.tu-dresden.de/systems/cel](http://inf.tu-dresden.de/systems/cel)), FaCT++ ([owl.man.ac.uk/factplusplus](http://owl.man.ac.uk/factplusplus)), and Hermit ([hermit-reasoner.com](http://hermit-reasoner.com)). We can see that the performance of DB is on par with the in-memory reasoners and, in particular, that DB outperforms CEL on Galen<sup>-</sup> and SNOMED, FaCT++ on Galen<sup>-</sup>, and Hermit on all ontologies.

## References

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