

# A Verified Information-Flow Architecture

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# Crash/ SAFE



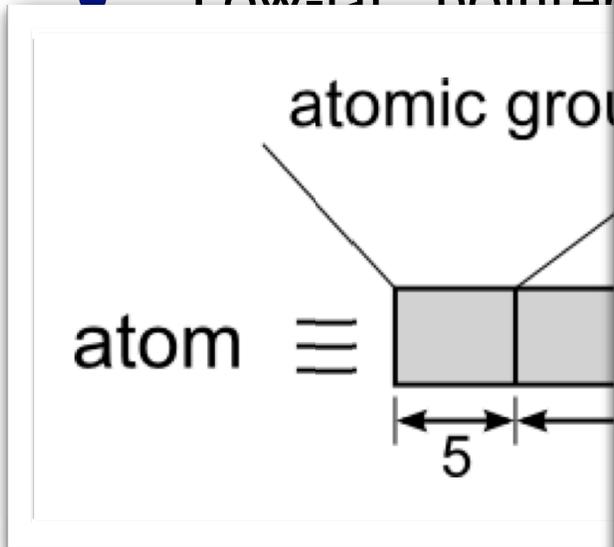
**BAE SYSTEMS**

# SAFE

- Clean-slate redesign of the entire system stack
  - Hardware
  - System software
  - Programming languages
- Support for critical security invariants at all levels
  - Memory safety
  - Strong dynamic typing
  - Information flow and access control
- Verification of key mechanisms deeply integrated into design process

# SAFE: Hardware

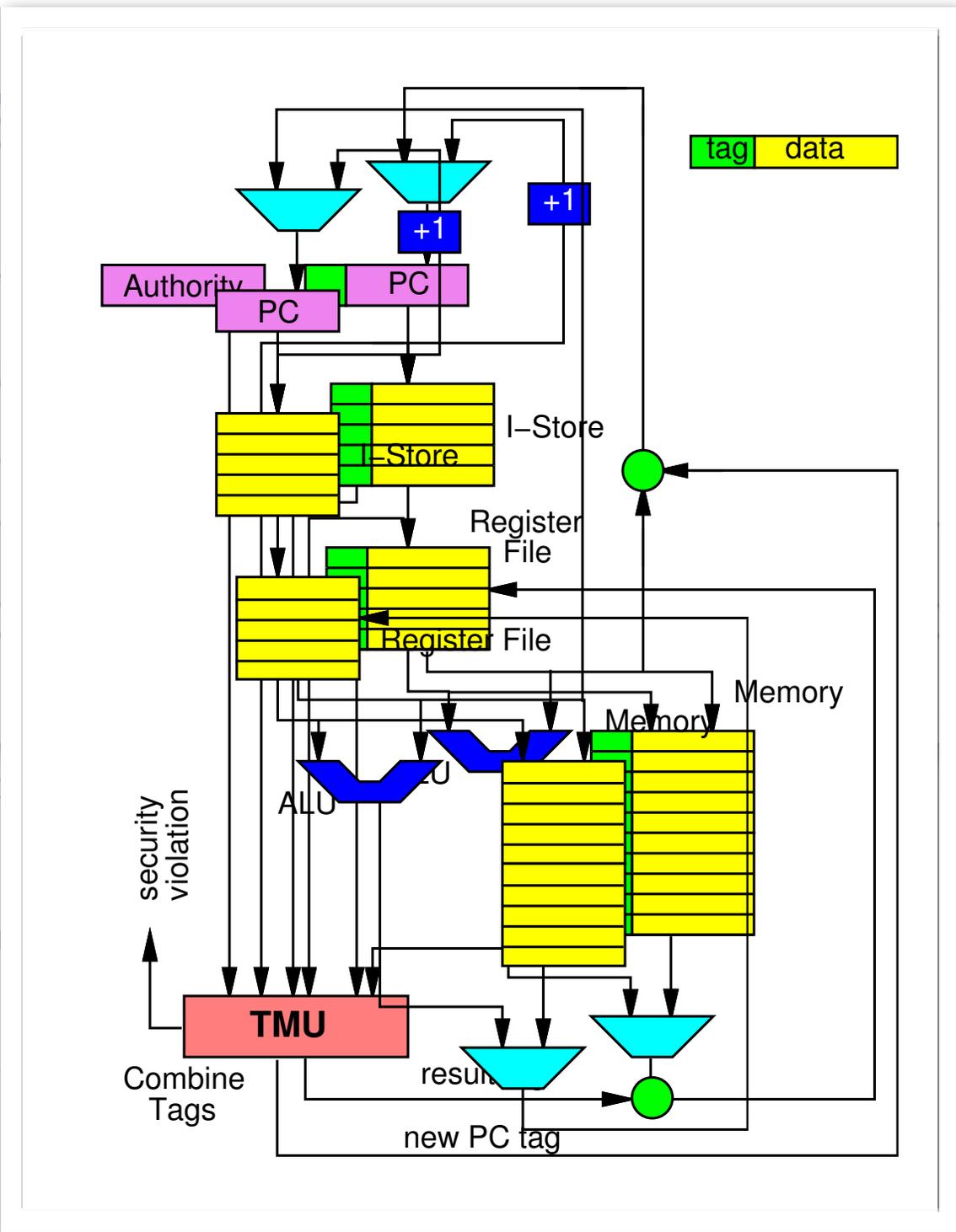
- “Low-fat” pointers



- Hardware rule co

- And more...

- Lightweight transa
- Linear pointers
- Hardware-support



# Why new hardware?

- Explore how to spend hardware resources on security effectively
- Reconsider traditional sources of complexity and vulnerability
- Remove application compiler, libraries, etc. from TCB
  - Strong attack model

# **This work...**

*Formal Model of SAFE's Hardware  
Tagging and Low-Level Tag-  
Management Software*

*Proof of correctness*

# **Goal for today...**

**Explain HW/SW architecture;  
Sketch proof architecture**

# Simplifications

- Deterministic, **single-threaded** machine
- Conventional memory model
  - pointers are just integers
  - single kernel protection domain
- Stack instead of registers
- No downgrading, public labels, dynamic principal generation, ...
- No exception handling
  - security violation halts the whole machine
- One-line rule cache

*Major*

*Minor*

# Outline

Concrete  
Machine

Abstract  
IFC Machine



Concrete  
Machine

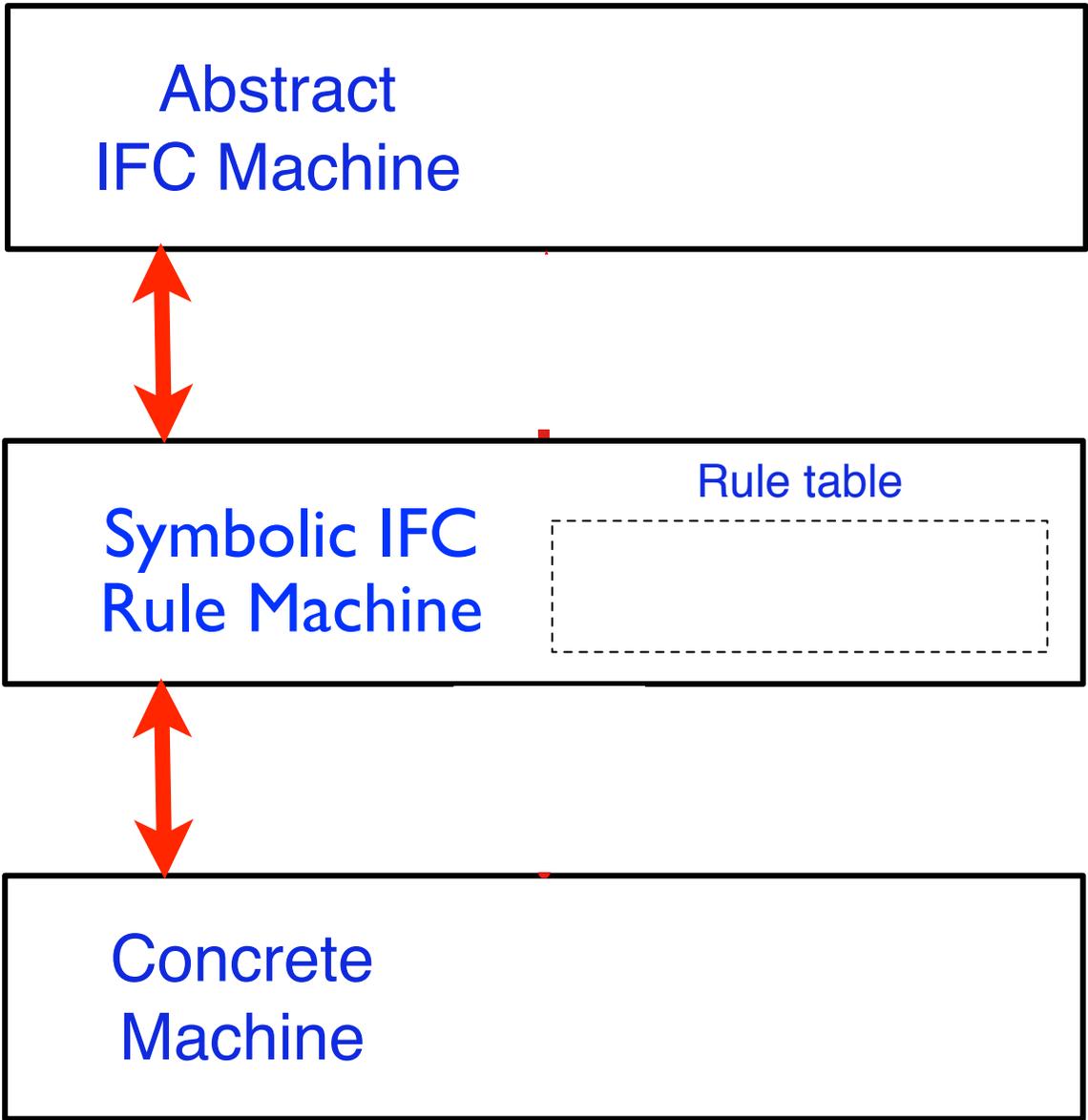
Abstract  
IFC Machine

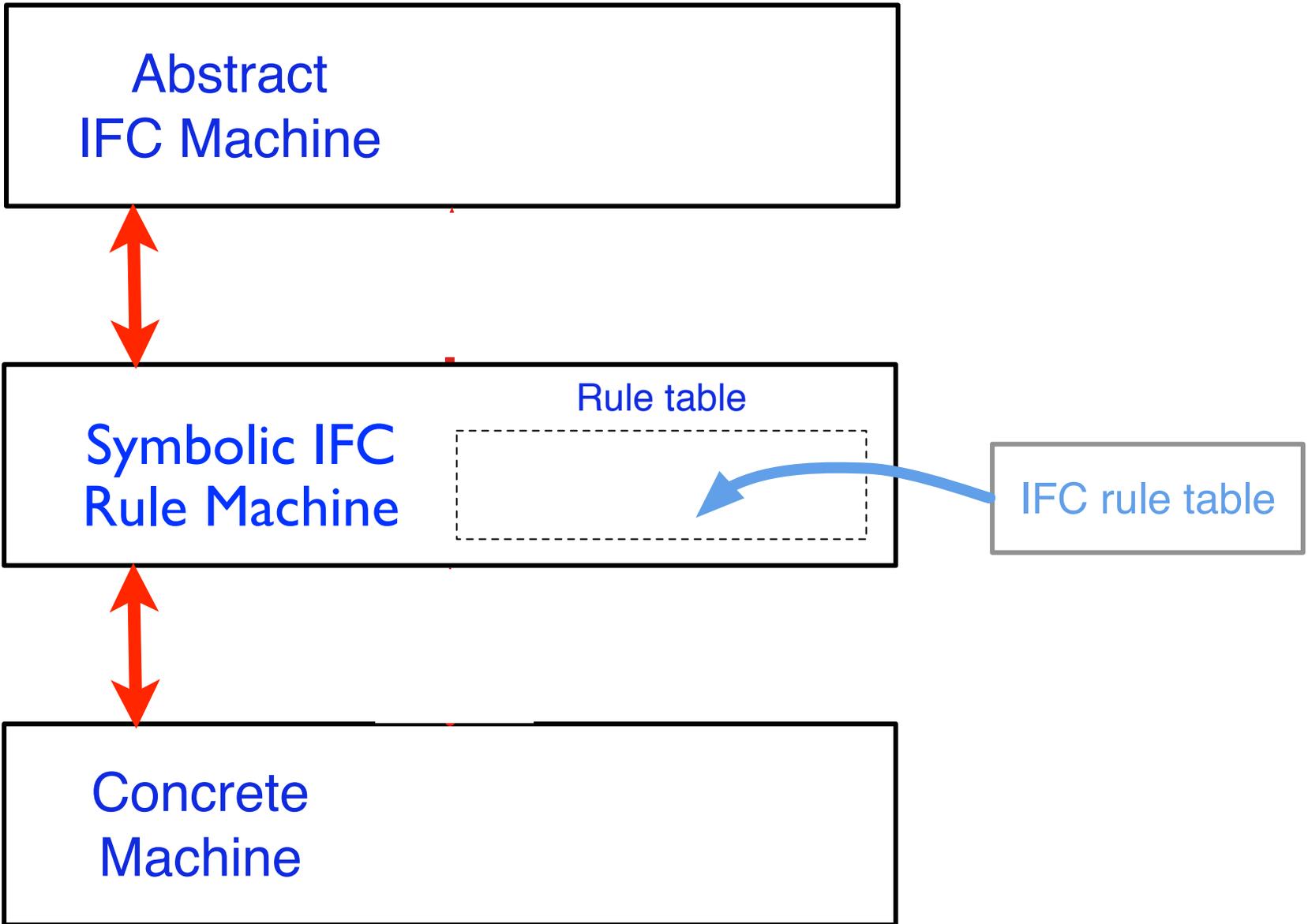


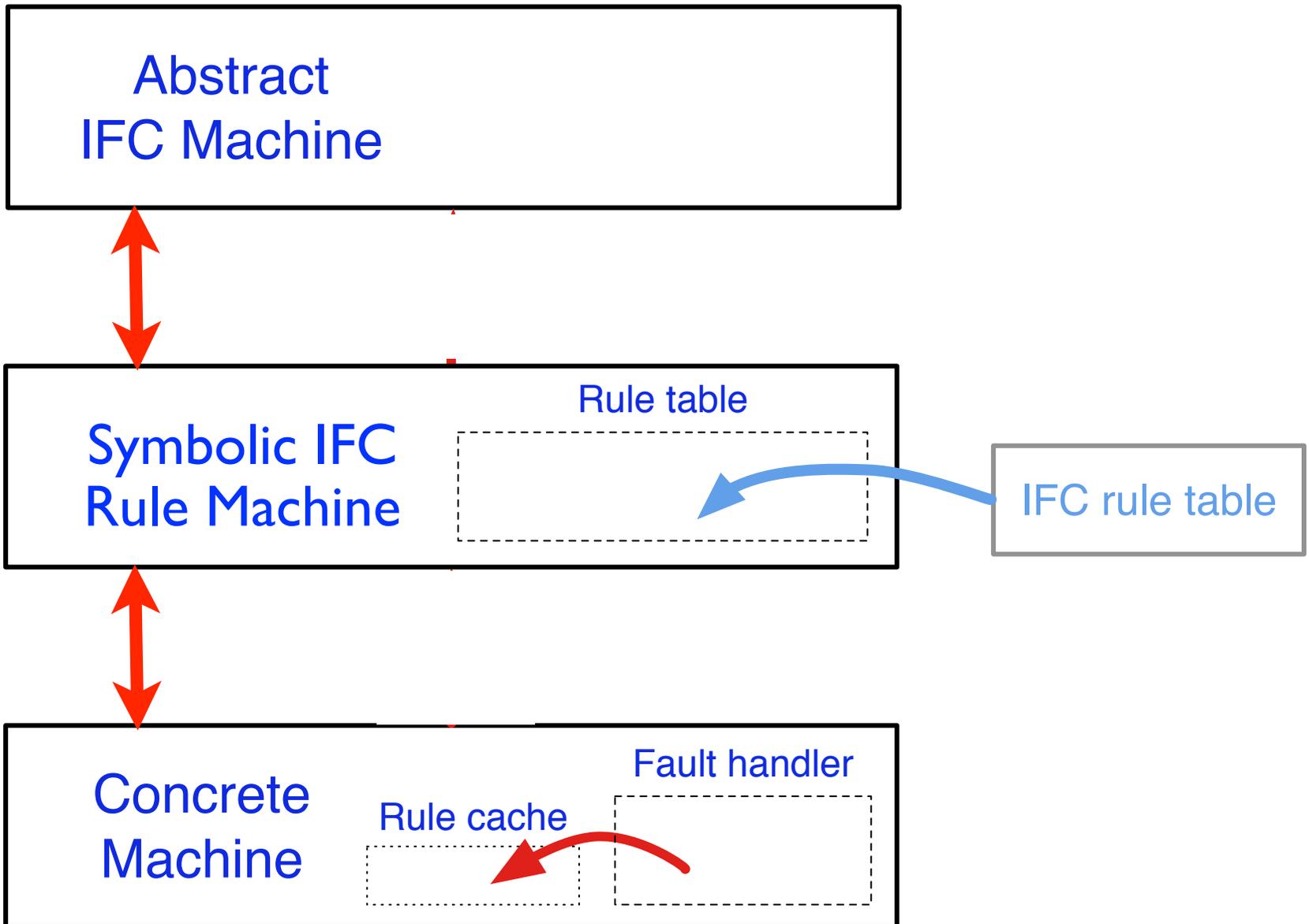
Symbolic IFC  
Rule Machine

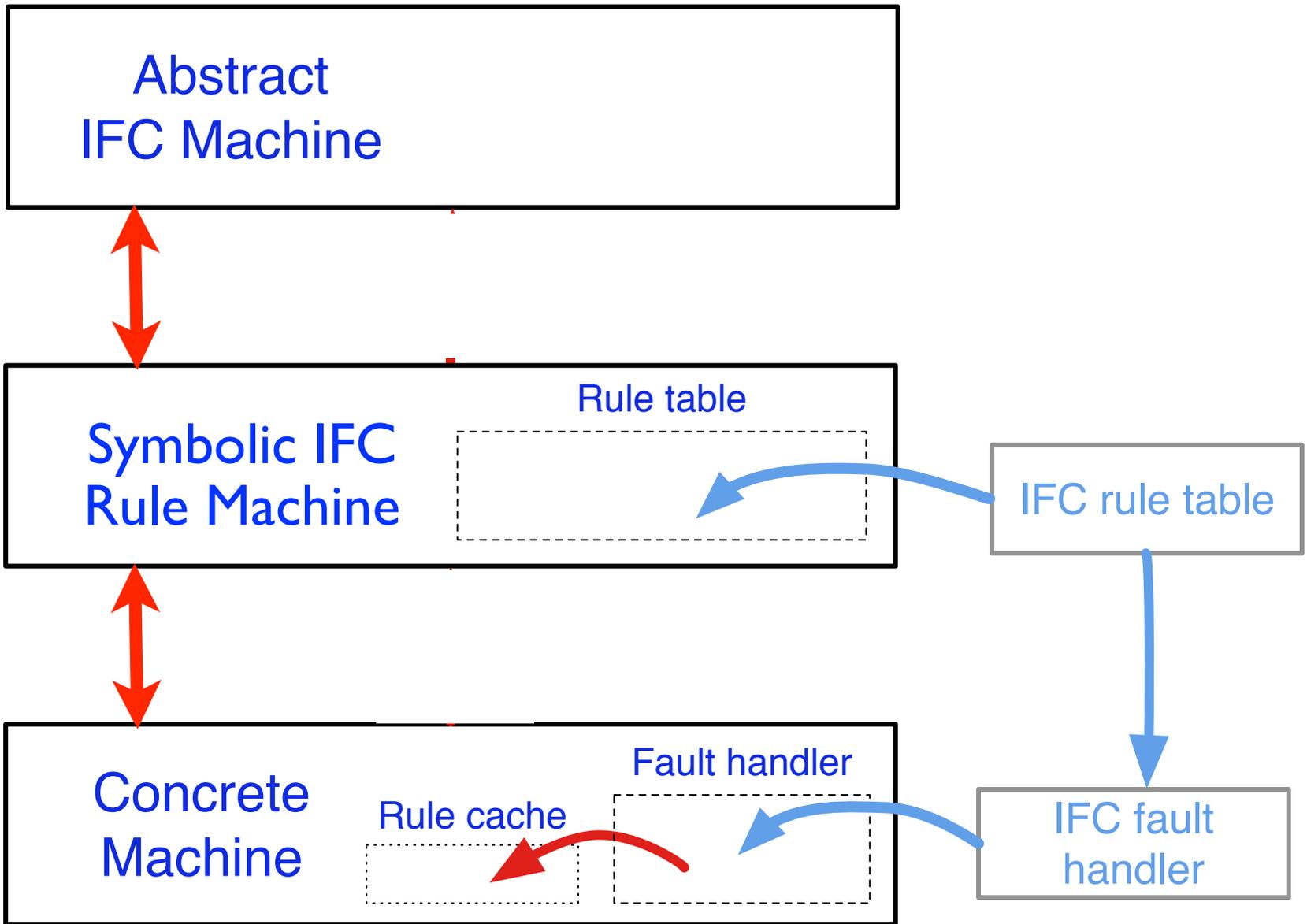


Concrete  
Machine









# Abstract Machine

# Non-interference

- We design the abstract machine so that it is easy to prove a non-interference property
  - Strictly: termination-insensitive non-interference
  - Over arbitrary semi-lattice of labels, from point of view of arbitrary observer
- Roughly: “high” inputs cannot affect “low” outputs.
  - If two executions of a program start with the same “low” data, the “low” parts of their output traces will be the same

# Abstract Machine

Instruction memory (user)



Machine state

<i>instr</i>	::=		Instructions
		Output	output top of stack
		Sub	subtract
		Push <i>n</i>	push constant integer
		Load	indirect load from data memory
		Store	indirect store to data memory
		Jump	unconditional indirect jump
		Bnz <i>n</i>	conditional relative jump
		Call	indirect call
		Ret	return



# Abstract Machine

Instruction memory (user)



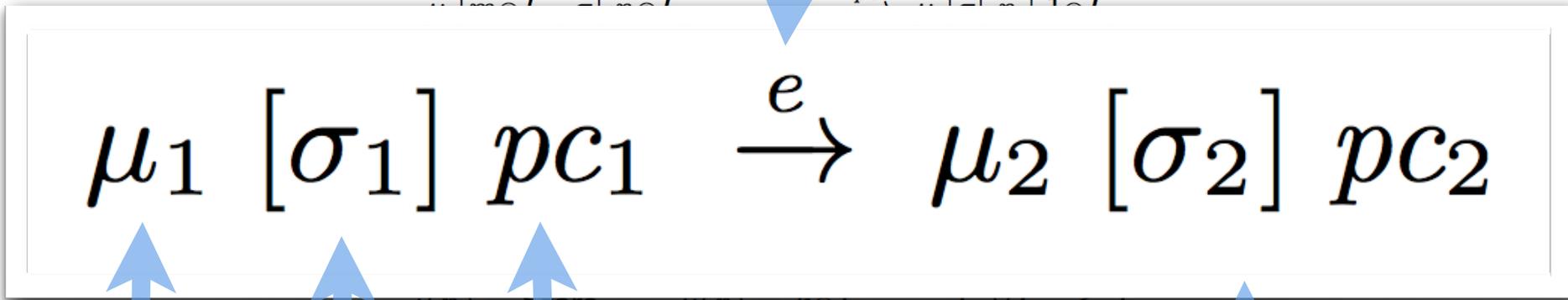
Output



$$\frac{\iota(n) = \text{Sub}}{\mu \quad [n_1 @ L_1, n_2 @ L_2, \sigma] \quad n @ L_{pc} \xrightarrow{\tau} \mu \quad [(n_1 - n_2) @ (L_1 \vee L_2), \sigma] \quad n+1 @ L_{pc}}$$

output

$$\frac{\iota(n) = \text{Output}}{\mu \quad [m @ L_1, \sigma] \quad n @ L_{pc} \xrightarrow{\tau} \mu \quad [m @ L_1 \vee L_{pc}, \sigma] \quad n+1 @ L_{pc}}$$



memory

stack

pc

next state

$$\frac{\iota(n) = \text{Store} \quad \mu(p) = \kappa @ L_3 \quad L_1 \vee L_{pc} \leq L_3 \quad \mu(p) \leftarrow (m @ L_1 \vee L_2 \vee L_{pc}) = \mu'}{\mu \quad [p @ L_1, m @ L_2, \sigma] \quad n @ L_{pc} \xrightarrow{\tau} \mu' \quad [\sigma] \quad n+1 @ L_{pc}}$$

$$\frac{\iota(n) = \text{Jump}}{\mu \quad [n' @ L_1, \sigma] \quad n @ L_{pc} \xrightarrow{\tau} \mu \quad [\sigma] \quad n' @ (L_1 \vee L_{pc})}$$

$$\frac{\iota(n) = \text{Bnz } k \quad n' = n + (m = 0)?1 : k}{\mu \quad [m @ L_1, \sigma] \quad n @ L_{pc} \xrightarrow{\tau} \mu \quad [\sigma] \quad n' @ (L_1 \vee L_{pc})}$$

$$\frac{\iota(n) = \text{Call}}{\mu \quad [n' @ L_1, a, \sigma] \quad n @ L_{pc} \xrightarrow{\tau} \mu \quad [a, n+1 @ L_{pc}; \sigma] \quad n' @ (L_1 \vee L_{pc})}$$

$$\frac{\iota(n) = \text{Ret}}{\mu \quad [n' @ L_1; \sigma] \quad n @ L_{pc} \xrightarrow{\tau} \mu \quad [\sigma] \quad n' @ L_1}$$

$$\iota(n) = \text{Sub}$$

$$\frac{\mu \quad [n_1 @ L_1, n_2 @ L_2, \sigma] \quad n @ L_{pc} \quad \xrightarrow{\tau}}{\mu \quad [(n_1 - n_2) @ (L_1 \vee L_2), \sigma] \quad n+1 @ L_{pc}}$$

$$\iota(n) = \text{Sub}$$

$$\frac{\mu \quad [n_1 @ L_1, n_2 @ L_2, \sigma] \quad n @ L_{pc} \quad \xrightarrow{\tau}}{\mu \quad [(n_1 - n_2) @ (L_1 \vee L_2), \sigma] \quad n+1 @ L_{pc}}$$

$$\frac{\iota(n) = \text{Store} \quad \mu(p) = k @ L_3 \quad L_1 \vee L_{pc} \leq L_3 \quad \mu(p) \leftarrow (m @ L_1 \vee L_2 \vee L_{pc}) = \mu'}{\mu \quad [p @ L_1, m @ L_2, \sigma] \quad n @ L_{pc} \quad \xrightarrow{\tau} \quad \mu' \quad [\sigma] \quad n+1 @ L_{pc}}$$

$$\iota(n) = \text{Jump}$$

$$\frac{\mu \quad [n' @ L_1, \sigma] \quad n @ L_{pc} \quad \xrightarrow{\tau} \quad \mu \quad [\sigma] \quad n' @ (L_1 \vee L_{pc})}{\iota(n) = \text{Bnz } k \quad n' = n + (m = 0)?1 : k}$$

$$\frac{\mu \quad [m @ L_1, \sigma] \quad n @ L_{pc} \quad \xrightarrow{\tau} \quad \mu \quad [\sigma] \quad n' @ (L_1 \vee L_{pc})}{\iota(n) = \text{Call}}$$

$$\iota(n) = \text{Call}$$

$$\frac{\mu \quad [n' @ L_1, a, \sigma] \quad n @ L_{pc} \quad \xrightarrow{\tau} \quad \mu \quad [a, n+1 @ L_{pc}; \sigma] \quad n' @ (L_1 \vee L_{pc})}{\iota(n) = \text{Ret}}$$

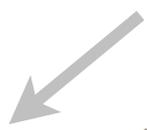
$$\iota(n) = \text{Ret}$$

$$\frac{\mu \quad [n' @ L_1; \sigma] \quad n @ L_{pc} \quad \xrightarrow{\tau} \quad \mu \quad [\sigma] \quad n' @ L_1}$$

# Example

Suppose:

$$l = [\dots, \text{Sub}, \dots]$$

*index n* 

Then:

$$\begin{array}{llll} \mu & [7@ \perp, 5@ \top] & n@ \perp & \longrightarrow \\ \mu & [2@ \top] & (n+1)@ \perp & \end{array}$$

$$\frac{\iota(n) = \text{Sub}}{\mu \quad [n_1 @ L_1, n_2 @ L_2, \sigma] \quad n @ L_{pc} \quad \xrightarrow{\tau} \quad \mu \quad [(n_1 - n_2) @ (L_1 \vee L_2), \sigma] \quad n+1 @ L_{pc}}$$

$\iota(n) = \text{Output}$

$$\iota(n) = \text{Bnz } k \quad n' = n + ((m = 0)?1 : k)$$

$$\mu \quad [m @ L_1, \sigma] \quad n @ L_{pc} \quad \xrightarrow{\tau} \quad \mu \quad [\sigma] \quad n' @ (L_1 \vee L_{pc})$$

$$\frac{\iota(n) = \text{Store} \quad \mu(p) = k @ L_3 \quad L_1 \vee L_{pc} \leq L_3 \quad \mu(p) \leftarrow (m @ L_1 \vee L_2 \vee L_{pc}) = \mu'}{\mu \quad [p @ L_1, m @ L_2, \sigma] \quad n @ L_{pc} \quad \xrightarrow{\tau} \quad \mu' \quad [\sigma] \quad n+1 @ L_{pc}}$$

$\iota(n) = \text{Jump}$

$$\mu \quad [n' @ L_1, \sigma] \quad n @ L_{pc} \quad \xrightarrow{\tau} \quad \mu \quad [\sigma] \quad n' @ (L_1 \vee L_{pc})$$

$$\iota(n) = \text{Bnz } k \quad n' = n + (m = 0)?1 : k$$

$$\mu \quad [m @ L_1, \sigma] \quad n @ L_{pc} \quad \xrightarrow{\tau} \quad \mu \quad [\sigma] \quad n' @ (L_1 \vee L_{pc})$$

$\iota(n) = \text{Call}$

$$\mu \quad [n' @ L_1, a, \sigma] \quad n @ L_{pc} \quad \xrightarrow{\tau} \quad \mu \quad [a, n+1 @ L_{pc}; \sigma] \quad n' @ (L_1 \vee L_{pc})$$

$\iota(n) = \text{Ret}$

$$\mu \quad [n' @ L_1; \sigma] \quad n @ L_{pc} \quad \xrightarrow{\tau} \quad \mu \quad [\sigma] \quad n' @ L_1$$

$$\iota(n) = \text{Sub}$$

$$\frac{\mu \quad [n_1 @ L_1, n_2 @ L_2, \sigma] \quad n @ L_{pc} \quad \xrightarrow{\tau}}{\mu \quad [(n_1 - n_2) @ (L_1 \vee L_2), \sigma] \quad n+1 @ L_{pc}}$$

$$\iota(n) = \text{Output}$$
$$\iota(n) = \text{Store} \quad \mu(p) = k @ L_3 \quad L_1 \vee L_{pc} \leq L_3$$
$$\mu(p) \leftarrow (m @ L_1 \vee L_2 \vee L_{pc}) = \mu'$$

$$\mu \quad [p @ L_1, m @ L_2, \sigma] \quad n @ L_{pc} \quad \xrightarrow{\tau} \quad \mu' \quad [\sigma] \quad (n+1) @ L_{pc}$$

$$\mu(p) \leftarrow (m @ L_1 \vee L_2 \vee L_{pc}) = \mu'$$

$$\mu \quad [p @ L_1, m @ L_2, \sigma] \quad n @ L_{pc} \quad \xrightarrow{\tau} \quad \mu' \quad [\sigma] \quad n+1 @ L_{pc}$$

$$\iota(n) = \text{Jump}$$

$$\mu \quad [n' @ L_1, \sigma] \quad n @ L_{pc} \quad \xrightarrow{\tau} \quad \mu \quad [\sigma] \quad n' @ (L_1 \vee L_{pc})$$

$$\iota(n) = \text{Bnz } k \quad n' = n + (m = 0) ? 1 : k$$

$$\mu \quad [m @ L_1, \sigma] \quad n @ L_{pc} \quad \xrightarrow{\tau} \quad \mu \quad [\sigma] \quad n' @ (L_1 \vee L_{pc})$$

$$\iota(n) = \text{Call}$$

$$\mu \quad [n' @ L_1, a, \sigma] \quad n @ L_{pc} \quad \xrightarrow{\tau} \quad \mu \quad [a, n+1 @ L_{pc}; \sigma] \quad n' @ (L_1 \vee L_{pc})$$

$$\iota(n) = \text{Ret}$$

$$\mu \quad [n' @ L_1; \sigma] \quad n @ L_{pc} \quad \xrightarrow{\tau} \quad \mu \quad [\sigma] \quad n' @ L_1$$

$\iota(n) = \text{Sub}$

$$\frac{\mu \quad [n_1 @ L_1, n_2 @ L_2, \sigma] \quad n @ L_{pc} \quad \xrightarrow{\tau}}{\mu \quad [(n_1 - n_2) @ (L_1 \vee L_2), \sigma] \quad n+1 @ L_{pc}}$$

$\iota(n) = \text{Output}$

$$\frac{\mu \quad [m @ L_1, \sigma] \quad n @ L_{pc} \quad \xrightarrow{m @ L_1 \vee L_{pc}}}{\mu \quad [\sigma] \quad n+1 @ L_{pc}}$$

$\iota(n) = \text{Push } m$

$$\frac{\mu \quad [\sigma] \quad n @ L_{pc} \quad \xrightarrow{\tau}}{\mu \quad [m @ \perp, \sigma] \quad n+1 @ L_{pc}}$$

$\iota(n) = \text{Load} \quad \mu(p) = m @ L_2$

$$\frac{\mu \quad [p @ L_1, \sigma] \quad n @ L_{pc} \quad \xrightarrow{\tau}}{\mu \quad [m @ L_1 \vee L_2, \sigma] \quad n+1 @ L_{pc}}$$

$\iota(n) = \text{Store} \quad \mu(p) = k @ L_3 \quad L_1 \vee L_{pc} \leq L_3$   
 $\mu(p) \leftarrow (m @ L_1 \vee L_2 \vee L_{pc}) = \mu'$

$$\frac{\mu \quad [p @ L_1, m @ L_2, \sigma] \quad n @ L_{pc} \quad \xrightarrow{\tau}}{\mu' \quad [\sigma] \quad n+1 @ L_{pc}}$$

$\iota(n) = \text{Call}$

$$\frac{\mu \quad [n' @ L_1, a, \sigma] \quad n @ L_{pc} \quad \xrightarrow{\tau}}{\mu \quad [a, n+1 @ L_{pc}; \sigma] \quad n' @ (L_1 \vee L_{pc})}$$

$\iota(n) = \text{Ret}$

$$\frac{\mu \quad [n' @ L_1; \sigma] \quad n @ L_{pc} \quad \xrightarrow{\tau}}{\mu \quad [\sigma] \quad n' @ L_1}$$

# Symbolic IFC Rule Machine

# Symbolic IFC Rule Machine

- Alternative presentation of abstract machine
  - Same machine states
  - Same step relation
- IFC side conditions factored out into a separate, explicit *rule table*

$$\frac{\iota(n) = \text{Sub} \quad \vdash_{\mathcal{R}} (L_{pc}, L_1, L_2, -) \rightsquigarrow_{\text{sub}} L_{rpc}, L_r}{\begin{array}{l} \mu [n_1 @ L_1, n_1 @ L_2, \sigma] \quad n @ L_{pc} \\ \mu [(n_1 - n_2) @ L_r, \sigma] \quad (n+1) @ L_{rpc} \end{array} \xrightarrow{\tau}}$$

$$\frac{\iota(n) = \text{Output} \quad \vdash_{\mathcal{R}} (L_{pc}, -, -, -) \rightsquigarrow_{\text{push}} L_{rpc}, L_r}{\begin{array}{l} \mu [m @ L_1, \sigma] \quad n @ L_r \\ \mu [m @ L_1, \sigma] \quad (n+1) @ L_{rpc} \end{array} \xrightarrow{\tau}}$$

*consult rule table... and opcode... to obtain result tags... for tags...*

$$\frac{\iota(n) = \text{Sub} \quad \vdash_{\mathcal{R}} (L_{pc}, L_1, L_2, -) \rightsquigarrow_{\text{sub}} L_{rpc}, L_r}{\begin{array}{l} \mu [n_1 @ L_1, n_1 @ L_2, \sigma] \quad n @ L_{pc} \\ \mu [(n_1 - n_2) @ L_r, \sigma] \quad (n+1) @ L_{rpc} \end{array} \xrightarrow{\tau}}$$

$$\frac{\iota(n) = \text{Bnz } n \quad n = n + (n = 0) : 1 : n \quad \vdash_{\mathcal{R}} (L_{pc}, L_1, -, -) \rightsquigarrow_{\text{bnz}} L_{rpc}, -}{\mu [m @ L_1, \sigma] \quad n @ L_{pc} \xrightarrow{\tau} \mu [\sigma] \quad n' @ L_{rpc}}$$

$$\frac{\iota(n) = \text{Call} \quad \vdash_{\mathcal{R}} (L_{pc}, L_1, -, -) \rightsquigarrow_{\text{call}} L_{rpc}, L_r}{\mu [n' @ L_1, a, \sigma] \quad n @ L_{pc} \xrightarrow{\tau} \mu [a, (n+1) @ L_r; \sigma] \quad n' @ L_{rpc}}$$

$$\frac{\iota(n) = \text{Ret} \quad \vdash_{\mathcal{R}} (L_{pc}, L_1, -, -) \rightsquigarrow_{\text{ret}} L_{rpc}, -}{\mu [n' @ L_1; \sigma] \quad n @ L_{pc} \xrightarrow{\tau} \mu [\sigma] \quad n' @ L_{rpc}}$$

# IFC Rule Table

*is this operation allowed?*

$\mathcal{R} =$

<i>opcode</i>	<i>allow</i>	<i>new pc label</i> $e_{rpc}$	<i>label for result</i> $e_r$
sub	TRUE	$LAB_{pc}$	$LAB_1 \sqcup LAB_2$
output	TRUE	$LAB_{pc}$	$LAB_1 \sqcup LAB_{pc}$
push	TRUE	$LAB_{pc}$	BOT
load	TRUE	$LAB_{pc}$	$LAB_1 \sqcup LAB_2$
store	$LAB_1 \sqcup LAB_{pc} \sqsubseteq LAB_3$	$LAB_{pc}$	$LAB_1 \sqcup LAB_2 \sqcup LAB_{pc}$
jump	TRUE	$LAB_1 \sqcup LAB_{pc}$	--
bnz	TRUE	$LAB_1 \sqcup LAB_{pc}$	--
call	TRUE	$LAB_1 \sqcup LAB_{pc}$	$LAB_{pc}$
ret	TRUE	$LAB_1$	--

# IFC Rule Table

*subtraction is always allowed*

*pc label is unchanged*

*result label is join of arg labels*

$\mathcal{R} =$

<i>opcode</i>	<i>allow</i>	<i>e<sub>rpc</sub></i>	<i>e<sub>r</sub></i>
sub	TRUE	LAB <sub>pc</sub>	LAB <sub>1</sub> $\sqcup$ LAB <sub>2</sub>
output	TRUE	LAB <sub>pc</sub>	LAB <sub>1</sub> $\sqcup$ LAB <sub>pc</sub>
push	TRUE	LAB <sub>pc</sub>	BOT
load	TRUE	LAB <sub>pc</sub>	LAB <sub>1</sub> $\sqcup$ LAB <sub>2</sub>
store	LAB <sub>1</sub> $\sqcup$ LAB <sub>pc</sub> $\sqsubseteq$ LAB <sub>3</sub>	LAB <sub>pc</sub>	LAB <sub>1</sub> $\sqcup$ LAB <sub>2</sub> $\sqcup$ LAB <sub>pc</sub>
jump	TRUE	LAB <sub>1</sub> $\sqcup$ LAB <sub>pc</sub>	--
bnz	TRUE	LAB <sub>1</sub> $\sqcup$ LAB <sub>pc</sub>	--
call	TRUE	LAB <sub>1</sub> $\sqcup$ LAB <sub>pc</sub>	LAB <sub>pc</sub>
ret	TRUE	LAB <sub>1</sub>	--

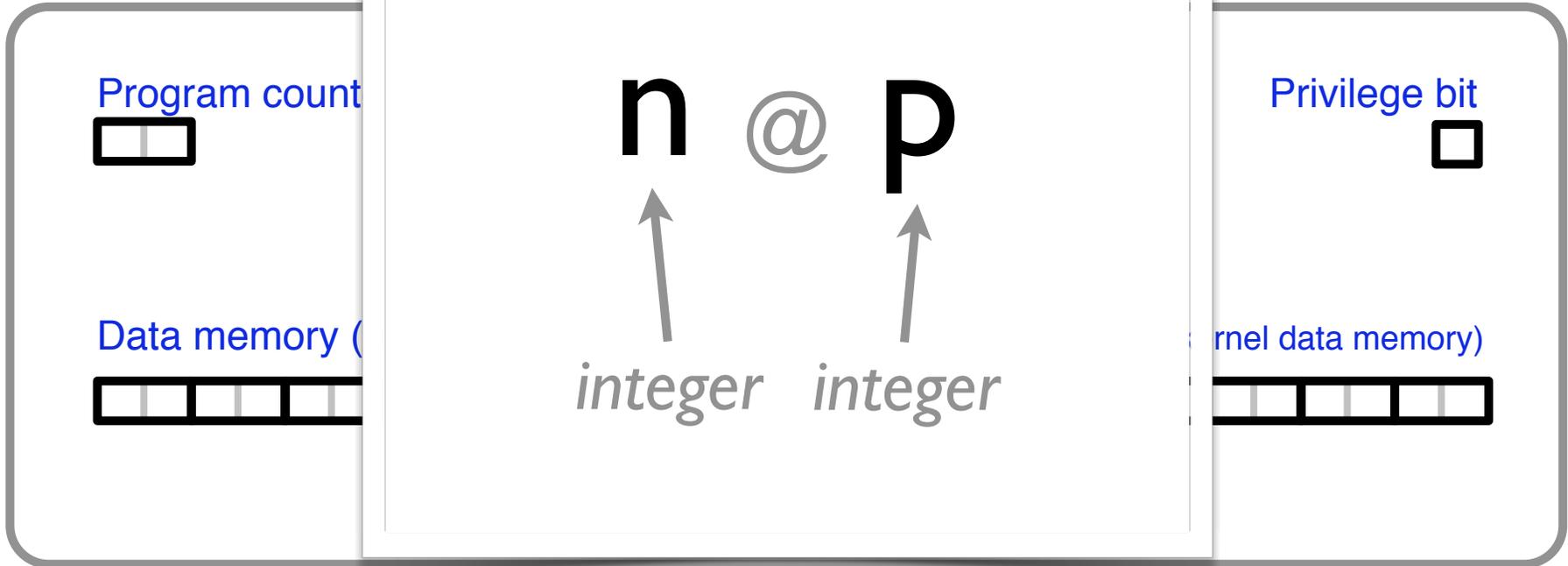
# Concrete Machine

# Concrete machine

Instruction memo



Machine state



ry (kernel)



Privilege bit



kernel data memory)



Output



# Concrete machine

Instruction memory (user)

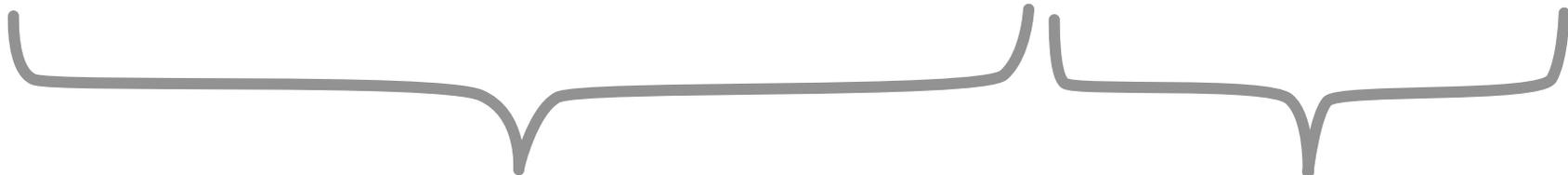


Instruction memory (kernel)



*(single-line)*

## Rule cache:



Inputs

Outputs

Output



# Kernel mode

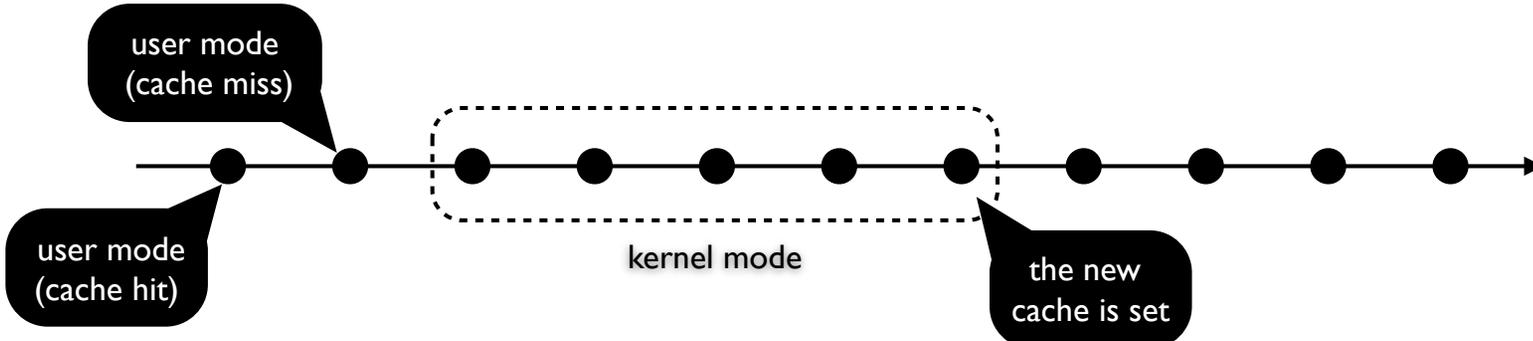
# User mode (cache hit)

# User-to-kernel mode (cache miss)

$\phi(n) = \text{Sub}$   
 $\frac{k \ \kappa \ \mu \ [n_1@-, n_1@-, \sigma] \ n@-}{k \ \kappa \ \mu \ [(n_1 - n_2)@T_-, \sigma] \ n+1@T_-} \xrightarrow{\tau}$   
**privilege bit**

$\iota(n) = \text{Sub}$   
 $\frac{\kappa = \text{sub} \ T_{pc} \ T_1 \ T_2 \ - \ | \ T_{rpc} \ T_r}{u \ \kappa \ \mu \ [n_1@T_1, n_2@T_2, \sigma] \ n@T_{pc} \ \xrightarrow{\tau}$   
 $u \ \kappa \ \mu \ [(n_1 - n_2)@T_r, \sigma] \ n+1@T_{rpc}$   
 $\iota(n) = \text{Output}$   
 $\frac{\kappa = \text{output} \ T_{pc} \ T_1 \ - \ - \ | \ T_{rpc} \ T_r}{u \ \kappa \ \mu \ [a, (n+1)@T_r, u]; \sigma] \ n'@T_{rpc}$

$\iota(n) = \text{Sub}$   
 $\frac{\kappa_i \neq \text{sub} \ T_{pc} \ T_1 \ T_2 \ - \ = \ \kappa_j}{u \ [\kappa_i, \kappa_o] \ \mu \ [n_1@T_1, n_1@T_2, \sigma] \ n@T_{pc} \ \xrightarrow{\tau}$   
 $k \ [\kappa_j, \kappa_-] \ \mu \ [(n@T_{pc}, u); n_1@T_1, n_1@T_2, \sigma] \ 0@T_-$   
 $\iota(n) = \text{Output}$   
 $\frac{\kappa_i \neq \text{output} \ T_{pc} \ T_1 \ - \ - \ = \ \kappa_j}{u \ [\kappa_i, \kappa_o] \ \mu \ [(n@T_{pc}, u); n'@T_1, a, \sigma] \ n@T_{pc} \ \xrightarrow{\tau}$   
 $k \ [\kappa_j, \kappa_-] \ \mu \ [(n@T_{pc}, u); (n'@T_1, \pi); \sigma] \ 0@T_-$



**user memory**  
**kernel memory**  
**stack**

$\kappa = \text{bnz} \ T_{pc} \ T_1 \ - \ - \ | \ T_{rpc} \ -$   
 $n' = n + (m = 0) ? 1 : k$   
 $\frac{u \ \kappa \ \mu \ [m@T_1, \sigma] \ n@T_{pc} \ \xrightarrow{\tau}$   
 $u \ \kappa \ \mu \ [\sigma] \ n'@T_{rpc}$   
 $\iota(n) = \text{Call}$   
 $\frac{\kappa = \text{call} \ T_{pc} \ T_1 \ - \ - \ | \ T_{rpc} \ T_r}{u \ \kappa \ \mu \ [n'@T_1, a, \sigma] \ n@T_{pc} \ \xrightarrow{\tau}$   
 $u \ \kappa \ \mu \ [a, (n+1)@T_r, u]; \sigma] \ n'@T_{rpc}$   
 $\iota(n) = \text{Ret}$   
 $\frac{\kappa = \text{ret} \ T_{pc} \ T_1 \ - \ - \ | \ T_{rpc} \ -}{u \ \kappa \ \mu \ [(n'@T_1, u); \sigma] \ n@T_{pc} \ \xrightarrow{\tau}$   
 $u \ \kappa \ \mu \ [\sigma] \ n'@T_{rpc}$

$\iota(n) = \text{Bnz} \ k$   
 $\frac{\kappa_i \neq \text{bnz} \ T_{pc} \ T_1 \ - \ - \ = \ \kappa_j}{u \ [\kappa_i, \kappa_o] \ \mu \ [m@T_1, \sigma] \ n@T_{pc} \ \xrightarrow{\tau}$   
 $k \ [\kappa_j, \kappa_-] \ \mu \ [(n@T_{pc}, u); m@T_1, \sigma] \ 0@T_-$   
 $\iota(n) = \text{Call}$   
 $\frac{\kappa_i \neq \text{call} \ T_{pc} \ T_1 \ - \ - \ = \ \kappa_j}{u \ [\kappa_i, \kappa_o] \ \mu \ [n'@T_1, a, \sigma] \ n@T_{pc} \ \xrightarrow{\tau}$   
 $k \ [\kappa_j, \kappa_-] \ \mu \ [(n@T_{pc}, u); n'@T_1, a, \sigma] \ 0@T_-$   
 $\iota(n) = \text{Ret}$   
 $\frac{\kappa_i \neq \text{ret} \ T_{pc} \ T_1 \ - \ - \ = \ \kappa_j}{u \ [\kappa_i, \kappa_o] \ \mu \ [(n'@T_1, \pi); \sigma] \ n@T_{pc} \ \xrightarrow{\tau}$   
 $k \ [\kappa_j, \kappa_-] \ \mu \ [(n@T_{pc}, u); (n'@T_1, \pi); \sigma] \ 0@T_-$

## User mode (cache hit)

## User-to-kernel mode (cache miss)

## Kernel mode

$$\begin{array}{l} \iota(n) = \text{Sub} \\ \kappa = \boxed{\text{sub} \mid T_{pc} \mid T_1 \mid T_2 \mid - \mid T_{rpc} \mid T_r} \\ \hline \text{u } \kappa \mu \ [n_1 @ T_1, n_2 @ T_2, \sigma] \ n @ T_{pc} \xrightarrow{\tau} \\ \text{u } \kappa \mu \ [(n_1 - n_2) @ T_r, \sigma] \ n+1 @ T_{rpc} \end{array}$$

$$\begin{array}{l} \iota(n) = \text{Output} \\ \kappa = \boxed{\text{output} \mid T_{pc} \mid T_1 \mid - \mid T_{rpc} \mid T_r} \\ \hline \text{u } \kappa \mu \ [m @ T_1, \sigma] \ n @ T_{pc} \xrightarrow{m @ T_r} \\ \text{u } \kappa \mu \ [\sigma] \ n+1 @ T_{rpc} \end{array}$$

$$\begin{array}{l} \iota(n) = \text{Sub} \\ \kappa_i \neq \boxed{\text{sub} \mid T_{pc} \mid T_1 \mid T_2 \mid -} = \kappa_j \\ \hline \text{u } [\kappa_i, \kappa_o] \mu \ [n_1 @ T_1, n_1 @ T_2, \sigma] \ n @ T_{pc} \xrightarrow{\tau} \\ \text{k } [\kappa_j, \kappa_e] \mu \ [(n @ T_{pc}, \text{u}); n_1 @ T_1, n_1 @ T_2, \sigma] \ 0 @ T \end{array}$$

$$\begin{array}{l} \iota(n) = \text{Output} \\ \kappa_i \neq \boxed{\text{output} \mid T_{pc} \mid T_1 \mid -} = \kappa_j \\ \hline \text{u } [\kappa_i, \kappa_o] \mu \ [m @ T_1, \sigma] \ n @ T_{pc} \xrightarrow{\tau} \\ \text{k } [\kappa_i, \kappa_e] \mu \ [(n @ T_{pc}, \text{u}); m @ T_1, \sigma] \ 0 @ T \end{array}$$

$$\begin{array}{l} \phi(n) = \text{Sub} \\ \hline \text{k } \kappa \mu \ [n_1 @ -, n_1 @ -, \sigma] \ n @ - \xrightarrow{\tau} \\ \text{k } \kappa \mu \ [(n_1 - n_2) @ T_r, \sigma] \ n+1 @ T \end{array}$$

$$\begin{array}{l} \phi(n) = \text{Push } m \\ \hline \text{k } \kappa \mu \ [\sigma] \ n @ - \xrightarrow{\tau} \text{k } \kappa \mu \ [m @ T_r, \sigma] \ n+1 @ T \end{array}$$

$$\begin{array}{l} \phi(n) = \text{Load} \quad \kappa(p) = m @ T_1 \\ \hline \text{k } \kappa \mu \ [m @ T_1, \sigma] \ n @ T \end{array}$$

$\iota(n) = \text{Sub}$

$\kappa = \boxed{\text{sub} \mid T_{pc} \mid T_1 \mid T_2 \mid - \mid T_{rpc} \mid T_r}$

$$\begin{array}{l} \text{u } \kappa \mu \ [n_1 @ T_1, n_2 @ T_2, \sigma] \ n @ T_{pc} \xrightarrow{\tau} \\ \text{u } \kappa \mu \ [(n_1 - n_2) @ T_r, \sigma] \ n+1 @ T_{rpc} \end{array}$$

$$\begin{array}{l} n' = n + (m = 0) ? 1 : k \\ \hline \text{u } \kappa \mu \ [m @ T_1, \sigma] \ n @ T_{pc} \xrightarrow{\tau} \\ \text{u } \kappa \mu \ [\sigma] \ n' @ T_{rpc} \end{array}$$

$$\begin{array}{l} \iota(n) = \text{Call} \\ \kappa = \boxed{\text{call} \mid T_{pc} \mid T_1 \mid - \mid T_{rpc} \mid T_r} \\ \hline \text{u } \kappa \mu \ [n' @ T_1, a, \sigma] \ n @ T_{pc} \xrightarrow{\tau} \\ \text{u } \kappa \mu \ [a, (n+1 @ T_r, \text{u}); \sigma] \ n' @ T_{rpc} \end{array}$$

$$\begin{array}{l} \iota(n) = \text{Ret} \\ \kappa = \boxed{\text{ret} \mid T_{pc} \mid T_1 \mid - \mid T_{rpc} \mid -} \\ \hline \text{u } \kappa \mu \ [(n' @ T_1, \text{u}); \sigma] \ n @ T_{pc} \xrightarrow{\tau} \\ \text{u } \kappa \mu \ [\sigma] \ n' @ T_{rpc} \end{array}$$

$$\begin{array}{l} \iota(n) = \text{Bnz } k \\ \kappa_i \neq \boxed{\text{bnz} \mid T_{pc} \mid T_1 \mid -} = \kappa_j \\ \hline \text{u } [\kappa_i, \kappa_o] \mu \ [m @ T_1, \sigma] \ n @ T_{pc} \xrightarrow{\tau} \\ \text{k } [\kappa_j, \kappa_e] \mu \ [(n @ T_{pc}, \text{u}); m @ T_1, \sigma] \ 0 @ T \end{array}$$

$$\begin{array}{l} \iota(n) = \text{Call} \\ \kappa_i \neq \boxed{\text{call} \mid T_{pc} \mid T_1 \mid -} = \kappa_j \\ \hline \text{u } [\kappa_i, \kappa_o] \mu \ [n' @ T_1, a, \sigma] \ n @ T_{pc} \xrightarrow{\tau} \\ \text{k } [\kappa_j, \kappa_e] \mu \ [(n @ T_{pc}, \text{u}); n' @ T_1, a, \sigma] \ 0 @ T \end{array}$$

$$\begin{array}{l} \iota(n) = \text{Ret} \\ \kappa_i \neq \boxed{\text{ret} \mid T_{pc} \mid T_1 \mid -} = \kappa_j \\ \hline \text{u } [\kappa_i, \kappa_o] \mu \ [(n' @ T_1, \pi); \sigma] \ n @ T_{pc} \xrightarrow{\tau} \\ \text{k } [\kappa_j, \kappa_e] \mu \ [(n @ T_{pc}, \text{u}); (n' @ T_1, \pi); \sigma] \ 0 @ T \end{array}$$

## User mode (cache hit)

$$\begin{array}{c} \iota(n) = \text{Sub} \\ \kappa = \boxed{\text{sub} \mid T_{pc} \mid T_1 \mid T_2 \mid - \mid T_{rpc} \mid T_r} \\ \hline \text{u } \kappa \mu \quad [n_1 @ T_1, n_2 @ T_2, \sigma] \quad n @ T_{pc} \xrightarrow{\tau} \\ \text{u } \kappa \mu \quad [(n_1 - n_2) @ T_r, \sigma] \quad n + 1 @ T_{rpc} \end{array}$$

$$\begin{array}{c} \iota(n) = \text{Output} \\ \kappa = \boxed{\text{output} \mid T_{pc} \mid T_1 \mid - \mid - \mid T_{rpc} \mid T_r} \\ \hline \text{u } \kappa \mu \quad [m @ T_1, \sigma] \quad n @ T_{pc} \xrightarrow{m @ T_r} \end{array}$$

## User-to-kernel mode (cache miss)

$$\begin{array}{c} \iota(n) = \text{Sub} \\ \kappa_i \neq \boxed{\text{sub} \mid T_{pc} \mid T_1 \mid T_2 \mid -} = \kappa_j \\ \hline \text{u } [\kappa_i, \kappa_o] \mu \quad [n_1 @ T_1, n_2 @ T_2, \sigma] \quad n @ T_{pc} \xrightarrow{\tau} \\ \text{k } [\kappa_j, \kappa_-] \mu \quad [(n @ T_{pc}, u); n_1 @ T_1, n_2 @ T_2, \sigma] \quad 0 @ T_- \end{array}$$

$$\begin{array}{c} \iota(n) = \text{Output} \\ \kappa_i \neq \boxed{\text{output} \mid T_{pc} \mid T_1 \mid - \mid -} = \kappa_j \\ \hline \text{u } [\kappa_i, \kappa_o] \mu \quad [m @ T_1, \sigma] \quad n @ T_{pc} \xrightarrow{\tau} \end{array}$$

## Kernel mode

$$\begin{array}{c} \phi(n) = \text{Sub} \\ \hline \text{k } \kappa \mu \quad [n_1 @ -, n_2 @ -, \sigma] \quad n @ - \xrightarrow{\tau} \\ \text{k } \kappa \mu \quad [(n_1 - n_2) @ T_-, \sigma] \quad n + 1 @ T_- \end{array}$$

$$\begin{array}{c} \phi(n) = \text{Push } m \\ \hline \text{k } \kappa \mu \quad [\sigma] \quad n @ - \xrightarrow{\tau} \text{k } \kappa \mu \quad [m @ T_-, \sigma] \quad n + 1 @ T_- \end{array}$$

$$\begin{array}{c} \phi(n) = \text{Load} \quad \kappa(p) = m @ T_1 \end{array}$$

$\iota(n) = \text{Sub}$

$\kappa_i \neq \boxed{\text{sub} \mid T_{pc} \mid T_1 \mid T_2 \mid -} = \kappa_j$

$$\begin{array}{c} \text{u } [\kappa_i, \kappa_o] \mu \quad [n_1 @ T_1, n_2 @ T_2, \sigma] \quad n @ T_{pc} \xrightarrow{\tau} \\ \text{k } [\kappa_j, \kappa_-] \mu \quad [(n @ T_{pc}, u); n_1 @ T_1, n_2 @ T_2, \sigma] \quad 0 @ T_- \end{array}$$

$$\begin{array}{c} \text{u } \kappa \mu \quad [n' @ T_1, \sigma] \quad n @ T_{pc} \xrightarrow{\tau} \\ \text{u } \kappa \mu \quad [\sigma] \quad n' @ T_{rpc} \end{array}$$

$$\begin{array}{c} \iota(n) = \text{Bnz } k \\ \kappa = \boxed{\text{bnz} \mid T_{pc} \mid T_1 \mid - \mid - \mid T_{rpc} \mid -} \\ n' = n + (m = 0) ? 1 : k \\ \hline \text{u } \kappa \mu \quad [m @ T_1, \sigma] \quad n @ T_{pc} \xrightarrow{\tau} \\ \text{u } \kappa \mu \quad [\sigma] \quad n' @ T_{rpc} \end{array}$$

$$\begin{array}{c} \iota(n) = \text{Call} \\ \kappa = \boxed{\text{call} \mid T_{pc} \mid T_1 \mid - \mid - \mid T_{rpc} \mid T_r} \\ \hline \text{u } \kappa \mu \quad [n' @ T_1, a, \sigma] \quad n @ T_{pc} \xrightarrow{\tau} \\ \text{u } \kappa \mu \quad [a, (n + 1 @ T_r, u); \sigma] \quad n' @ T_{rpc} \end{array}$$

$$\begin{array}{c} \iota(n) = \text{Ret} \\ \kappa = \boxed{\text{ret} \mid T_{pc} \mid T_1 \mid - \mid - \mid T_{rpc} \mid -} \\ \hline \text{u } \kappa \mu \quad [(n' @ T_1, u); \sigma] \quad n @ T_{pc} \xrightarrow{\tau} \\ \text{u } \kappa \mu \quad [\sigma] \quad n' @ T_{rpc} \end{array}$$

$$\begin{array}{c} \kappa_i \neq \boxed{\text{jump} \mid T_{pc} \mid T_1 \mid - \mid -} = \kappa_j \\ \hline \text{u } [\kappa_i, \kappa_o] \mu \quad [n' @ T_1, \sigma] \quad n @ T_{pc} \xrightarrow{\tau} \\ \text{k } [\kappa_j, \kappa_-] \mu \quad [(n @ T_{pc}, u); n' @ T_1, \sigma] \quad 0 @ T_- \end{array}$$

$$\begin{array}{c} \iota(n) = \text{Bnz } k \\ \kappa_i \neq \boxed{\text{bnz} \mid T_{pc} \mid T_1 \mid - \mid -} = \kappa_j \\ \hline \text{u } [\kappa_i, \kappa_o] \mu \quad [m @ T_1, \sigma] \quad n @ T_{pc} \xrightarrow{\tau} \\ \text{k } [\kappa_j, \kappa_-] \mu \quad [(n @ T_{pc}, u); m @ T_1, \sigma] \quad 0 @ T_- \end{array}$$

$$\begin{array}{c} \iota(n) = \text{Call} \\ \kappa_i \neq \boxed{\text{call} \mid T_{pc} \mid T_1 \mid - \mid -} = \kappa_j \\ \hline \text{u } [\kappa_i, \kappa_o] \mu \quad [n' @ T_1, a, \sigma] \quad n @ T_{pc} \xrightarrow{\tau} \\ \text{k } [\kappa_j, \kappa_-] \mu \quad [(n @ T_{pc}, u); n' @ T_1, a, \sigma] \quad 0 @ T_- \end{array}$$

$$\begin{array}{c} \iota(n) = \text{Ret} \\ \kappa_i \neq \boxed{\text{ret} \mid T_{pc} \mid T_1 \mid - \mid -} = \kappa_j \\ \hline \text{u } [\kappa_i, \kappa_o] \mu \quad [(n' @ T_1, \pi); \sigma] \quad n @ T_{pc} \xrightarrow{\tau} \\ \text{k } [\kappa_j, \kappa_-] \mu \quad [(n @ T_{pc}, u); (n' @ T_1, \pi); \sigma] \quad 0 @ T_- \end{array}$$

## User mode (cache hit)

$$\begin{array}{l}
 \iota(n) = \text{Sub} \\
 \kappa = \boxed{\text{sub} \mid T_{pc} \mid T_1 \mid T_2 \mid - \mid T_{rpc} \mid T_r} \\
 \hline
 \text{u } \kappa \mu \quad [n_1 @ T_1, n_2 @ T_2, \sigma] \quad n @ T_{pc} \xrightarrow{\tau} \\
 \text{u } \kappa \mu \quad [(n_1 - n_2) @ T_r, \sigma] \quad n+1 @ T_{rpc}
 \end{array}$$

$$\begin{array}{l}
 \iota(n) = \text{Output} \\
 \kappa = \boxed{\text{output} \mid T_{pc} \mid T_1 \mid - \mid - \mid T_{rpc} \mid T_r} \\
 \hline
 \text{u } \kappa \mu \quad [m @ T_1, \sigma] \quad n @ T_{pc} \xrightarrow{m @ T_r} \\
 \text{u } \kappa \mu \quad [\sigma] \quad n+1 @ T_{rpc}
 \end{array}$$

## User-to-kernel mode (cache miss)

$$\begin{array}{l}
 \iota(n) = \text{Sub} \\
 \kappa_i \neq \boxed{\text{sub} \mid T_{pc} \mid T_1 \mid T_2 \mid -} = \kappa_j \\
 \hline
 \text{u } [\kappa_i, \kappa_o] \mu \quad [n_1 @ T_1, n_1 @ T_2, \sigma] \quad n @ T_{pc} \xrightarrow{\tau} \\
 \text{k } [\kappa_j, \kappa_c] \mu \quad [(n @ T_{pc}, \text{u}); n_1 @ T_1, n_1 @ T_2, \sigma] \quad 0 @ T_1
 \end{array}$$

$$\begin{array}{l}
 \iota(n) = \text{Output} \\
 \kappa_i \neq \boxed{\text{output} \mid T_{pc} \mid T_1 \mid - \mid -} = \kappa_j \\
 \hline
 \text{u } [\kappa_i, \kappa_o] \mu \quad [m @ T_1, \sigma] \quad n @ T_{pc} \xrightarrow{\tau} \\
 \text{k } [\kappa_i, \kappa_c] \mu \quad [(n @ T_{pc}, \text{u}); m @ T_1, \sigma] \quad 0 @ T_1
 \end{array}$$

## Kernel mode

$$\begin{array}{l}
 \phi(n) = \text{Sub} \\
 \hline
 \text{k } \kappa \mu \quad [n_1 @ -, n_1 @ -, \sigma] \quad n @ - \xrightarrow{\tau} \\
 \text{k } \kappa \mu \quad [(n_1 - n_2) @ T_-, \sigma] \quad n+1 @ T_-
 \end{array}$$

$$\begin{array}{l}
 \phi(n) = \text{Push } m \\
 \hline
 \text{k } \kappa \mu \quad [\sigma] \quad n @ - \xrightarrow{\tau} \text{k } \kappa \mu \quad [m @ T_-, \sigma] \quad n+1 @ T_-
 \end{array}$$

$$\begin{array}{l}
 \phi(n) = \text{Load} \quad \kappa(p) = m @ T_1 \\
 \hline
 \text{k } \kappa \mu \quad [m @ T_1, \sigma] \quad n @ T_- \xrightarrow{\tau} \text{k } \kappa \mu \quad [\sigma] \quad n+1 @ T_-
 \end{array}$$

$$\phi(n) = \text{Sub}$$

$$\begin{array}{l}
 \text{k } \kappa \mu \quad [n_1 @ -, n_2 @ -, \sigma] \quad n @ - \xrightarrow{\tau} \\
 \text{k } \kappa \mu \quad [(n_1 - n_2) @ T_-, \sigma] \quad n+1 @ T_-
 \end{array}$$

$$\begin{array}{l}
 \iota(n) = \text{Bnz } k \\
 \kappa = \boxed{\text{bnz} \mid T_{pc} \mid T_1 \mid - \mid - \mid T_{rpc} \mid -} \\
 n' = n + (m = 0) ? 1 : k \\
 \hline
 \text{u } \kappa \mu \quad [m @ T_1, \sigma] \quad n @ T_{pc} \xrightarrow{\tau} \\
 \text{u } \kappa \mu \quad [\sigma] \quad n' @ T_{rpc}
 \end{array}$$

$$\begin{array}{l}
 \iota(n) = \text{Call} \\
 \kappa = \boxed{\text{call} \mid T_{pc} \mid T_1 \mid - \mid - \mid T_{rpc} \mid T_r} \\
 \hline
 \text{u } \kappa \mu \quad [n' @ T_1, a, \sigma] \quad n @ T_{pc} \xrightarrow{\tau} \\
 \text{u } \kappa \mu \quad [a, (n+1 @ T_r, \text{u}); \sigma] \quad n' @ T_{rpc}
 \end{array}$$

$$\begin{array}{l}
 \iota(n) = \text{Ret} \\
 \kappa = \boxed{\text{ret} \mid T_{pc} \mid T_1 \mid - \mid - \mid T_{rpc} \mid -} \\
 \hline
 \text{u } \kappa \mu \quad [(n' @ T_1, \text{u}); \sigma] \quad n @ T_{pc} \xrightarrow{\tau} \\
 \text{u } \kappa \mu \quad [\sigma] \quad n' @ T_{rpc}
 \end{array}$$

$$\text{k } [\kappa_j, \kappa_c] \mu \quad [(n @ T_{pc}, \text{u}); n @ T_1, \sigma] \quad 0 @ T_1$$

$$\begin{array}{l}
 \iota(n) = \text{Bnz } k \\
 \kappa_i \neq \boxed{\text{bnz} \mid T_{pc} \mid T_1 \mid - \mid -} = \kappa_j \\
 \hline
 \text{u } [\kappa_i, \kappa_o] \mu \quad [m @ T_1, \sigma] \quad n @ T_{pc} \xrightarrow{\tau} \\
 \text{k } [\kappa_j, \kappa_c] \mu \quad [(n @ T_{pc}, \text{u}); m @ T_1, \sigma] \quad 0 @ T_1
 \end{array}$$

$$\begin{array}{l}
 \iota(n) = \text{Call} \\
 \kappa_i \neq \boxed{\text{call} \mid T_{pc} \mid T_1 \mid - \mid -} = \kappa_j \\
 \hline
 \text{u } [\kappa_i, \kappa_o] \mu \quad [n' @ T_1, a, \sigma] \quad n @ T_{pc} \xrightarrow{\tau} \\
 \text{k } [\kappa_j, \kappa_c] \mu \quad [(n @ T_{pc}, \text{u}); n' @ T_1, a, \sigma] \quad 0 @ T_1
 \end{array}$$

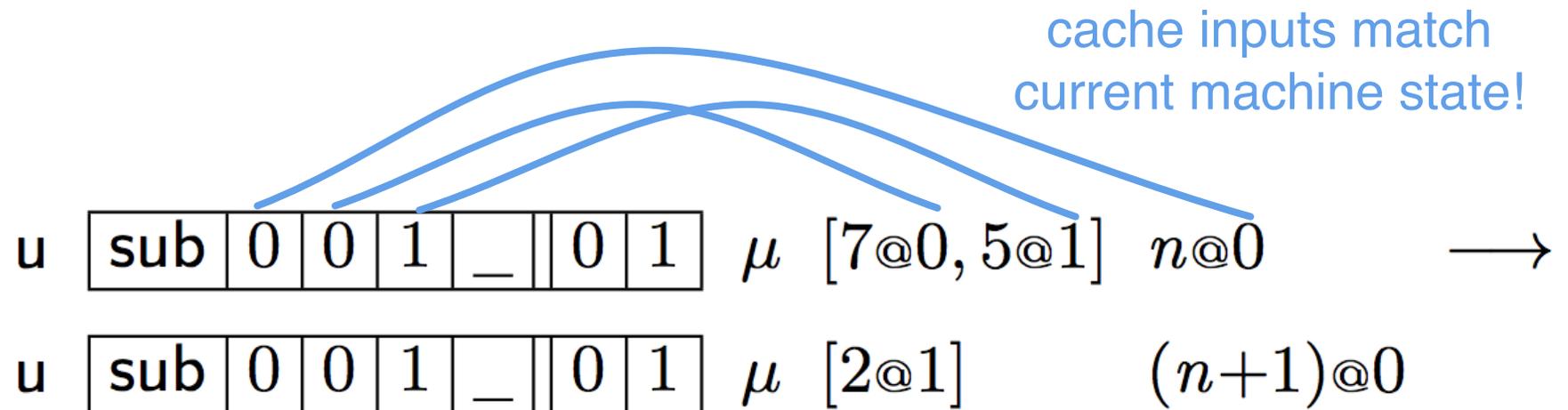
$$\begin{array}{l}
 \iota(n) = \text{Ret} \\
 \kappa_i \neq \boxed{\text{ret} \mid T_{pc} \mid T_1 \mid - \mid -} = \kappa_j \\
 \hline
 \text{u } [\kappa_i, \kappa_o] \mu \quad [(n' @ T_1, \pi); \sigma] \quad n @ T_{pc} \xrightarrow{\tau} \\
 \text{k } [\kappa_j, \kappa_c] \mu \quad [(n @ T_{pc}, \text{u}); (n' @ T_1, \pi); \sigma] \quad 0 @ T_1
 \end{array}$$

# Example (cache hit case)

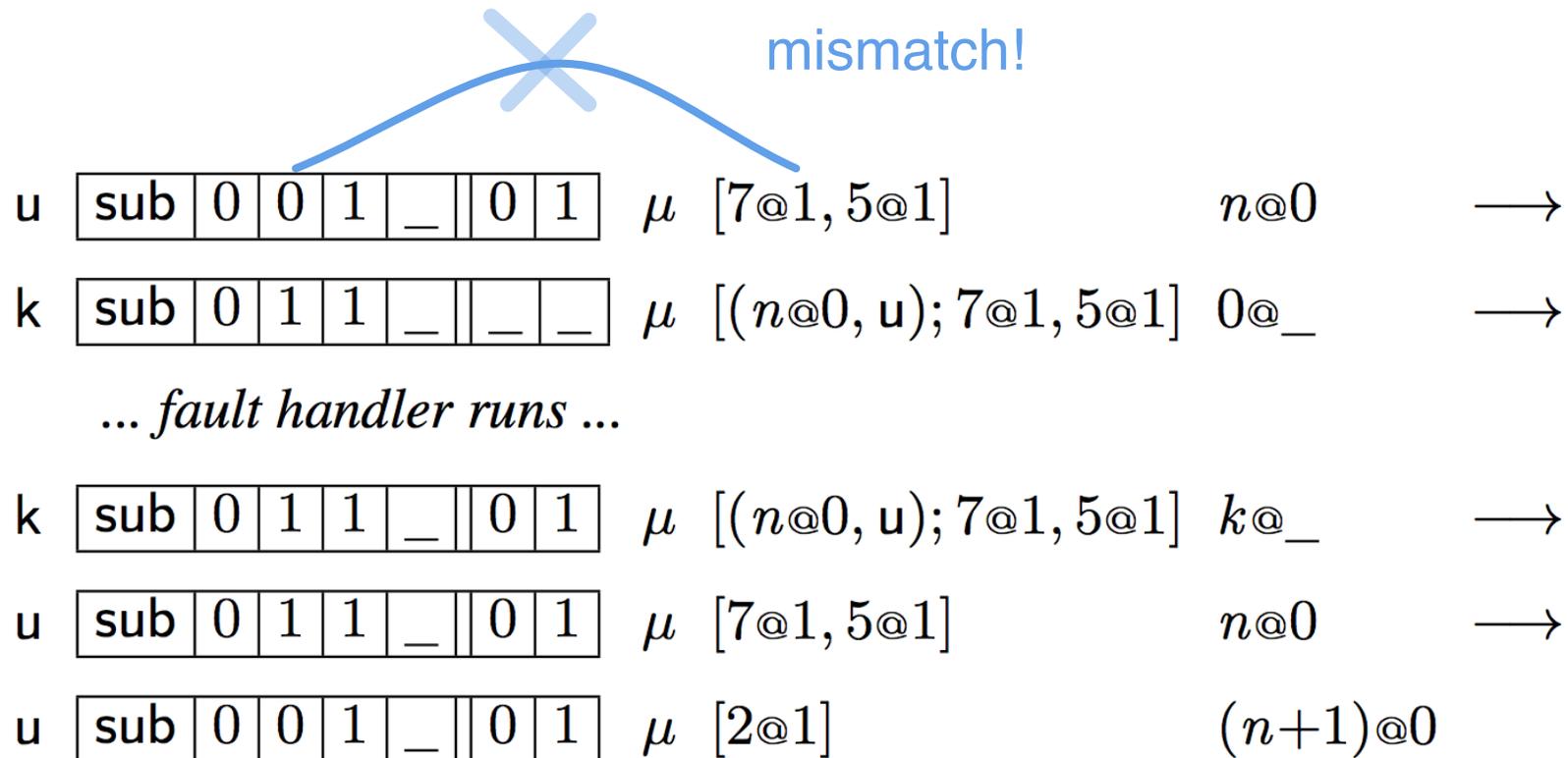
Suppose

tag 0 represents label  $\perp$

tag 1 represents label  $\top$



# Example (cache miss case)



# Fault Handler

# IFC RULE TABLE

<i>opcode</i>	<i>allow</i>	<i>e<sub>rpc</sub></i>	<i>e<sub>r</sub></i>
sub	TRUE	LAB <sub>pc</sub>	LAB <sub>1</sub> $\sqcup$ LAB <sub>2</sub>
output	TRUE	LAB <sub>pc</sub>	LAB <sub>1</sub> $\sqcup$ LAB <sub>pc</sub>
push	TRUE	LAB <sub>pc</sub>	BOT
load	TRUE	LAB <sub>pc</sub>	LAB <sub>1</sub> $\sqcup$ LAB <sub>2</sub>
store	LAB <sub>1</sub> $\sqcup$ LAB <sub>pc</sub> $\sqsubseteq$ LAB <sub>3</sub>	LAB <sub>pc</sub>	LAB <sub>1</sub> $\sqcup$ LAB <sub>2</sub> $\sqcup$ LAB <sub>pc</sub>
jump	TRUE	LAB <sub>1</sub> $\sqcup$ LAB <sub>pc</sub>	--
bnz	TRUE	LAB <sub>1</sub> $\sqcup$ LAB <sub>pc</sub>	--
call	TRUE	LAB <sub>1</sub> $\sqcup$ LAB <sub>pc</sub>	LAB <sub>pc</sub>
ret	TRUE	LAB <sub>1</sub>	--

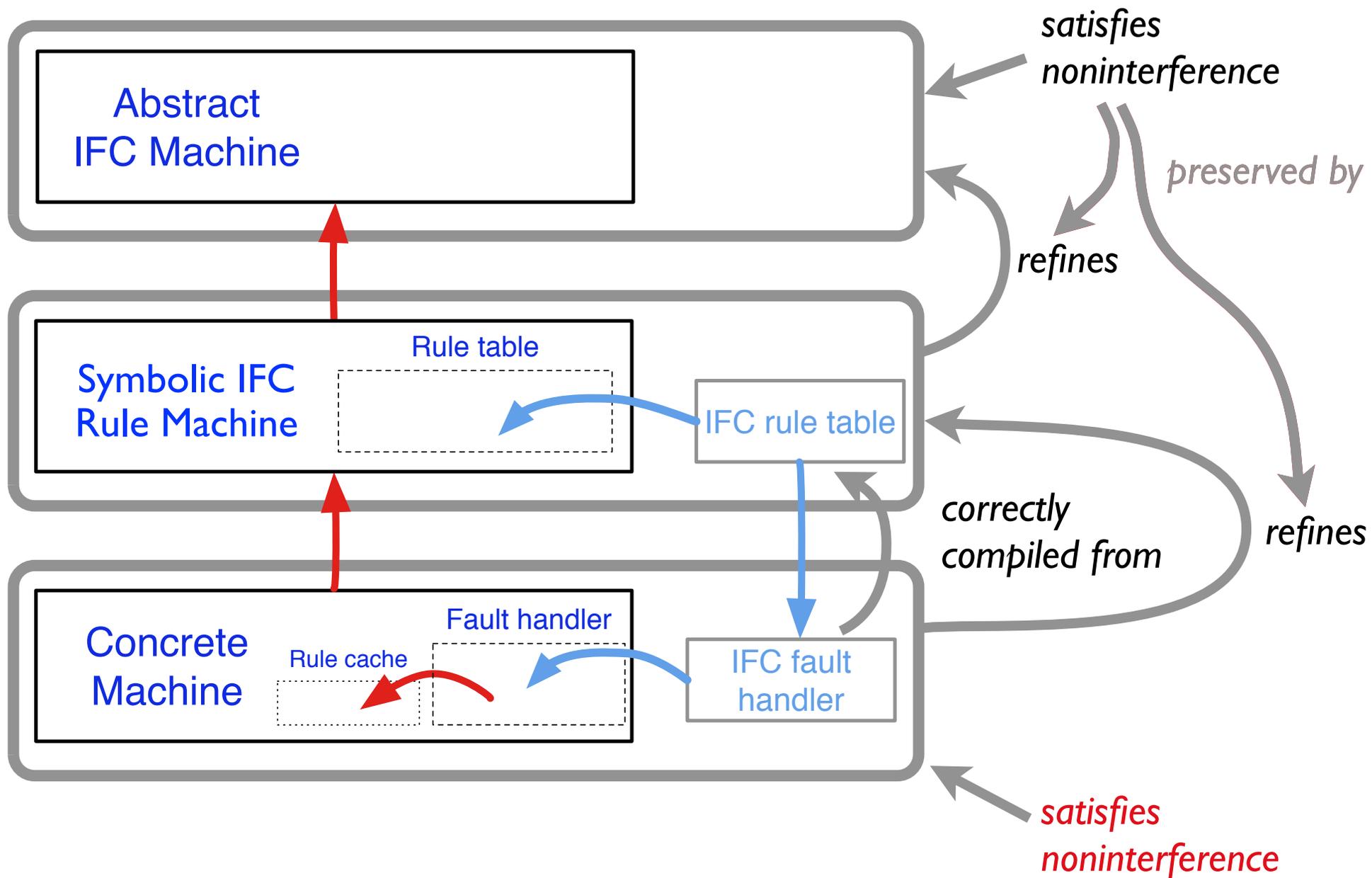
FAULT  
HANDLER

# Handler Generation

- IFC rule table entries form a small DSL for computing labels and booleans
  - parameterized over lattice  $\perp$ ,  $\sqcup$  and  $\sqsubseteq$
- The handler is constructed by compiling the DSL into concrete machine instructions
  - Table-driven interpreter would be an alternative
- We use structured code generators to simplify verification

# Non-interference for concrete machine

- Running this particular fault handler
- Together with arbitrary user code



# Points to note

- Refinement framework *very* useful for reasoning
  - start with concrete object
  - propose abstracted version
    - incorporate convenient structure and annotations
  - prove refinement
  - prove interesting property of abstract object
  - automatically follows for concrete object
- Need a *generic* notion of noninterference that makes sense for all machines
  - Includes a notion of abstracting concrete tags (and associated memory states) into labels

# Some Verification Challenges...

# More uses for tags

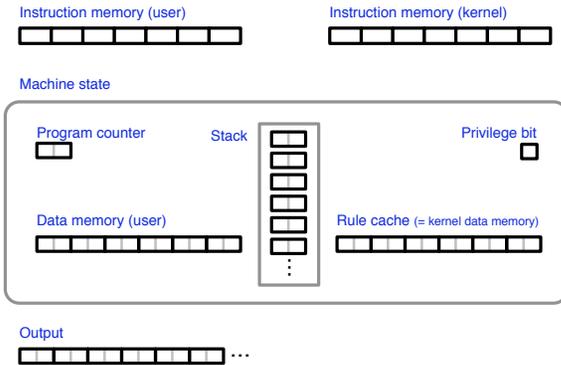
- **SAFE architecture is quite generic**
  - Can be used to implement a range of IFC label models just by varying the rule table [Montagu CSF '13]
- **Other potential uses**
  - access control (clearance)
  - memory protection
  - linearity
  - dynamic typing

# More Security Issues

- Downgrading
- “Least Privilege”
- Concurrency

# Real SAFE Machine

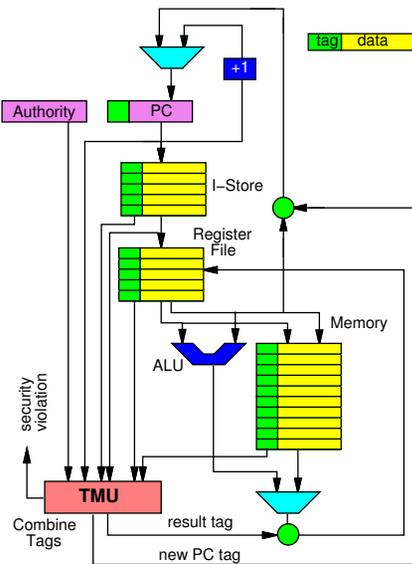
- Scaling methodology to full SAFE hardware and ConcreteWare
  - random testing vs. verification
- Breeze compiler correctness
  - for defense in depth



<i>opcode</i>	<i>allow</i>	$e_{rpc}$	$e_r$
sub	TRUE	$LAB_{pc}$	$LAB_1 \sqcup LAB_2$
output	TRUE	$LAB_{pc}$	$LAB_1 \sqcup LAB_{pc}$
push	TRUE	$LAB_{pc}$	BOT
load	TRUE	$LAB_{pc}$	$LAB_1 \sqcup LAB_2$
store	$LAB_1 \sqcup LAB_{pc} \sqsubseteq LAB_3$	$LAB_{pc}$	$LAB_1 \sqcup LAB_2 \sqcup LAB_{pc}$
jump	TRUE	$LAB_1 \sqcup LAB_{pc}$	--
bnz	TRUE	$LAB_1 \sqcup LAB_{pc}$	--
call	TRUE	$LAB_1 \sqcup LAB_{pc}$	$LAB_{pc}$
ret	TRUE	$LAB_1$	--

# Thank you!

## Questions??



$$\frac{\iota(n) = \text{Sub}}{\mu [n_1 @ L_1, n_2 @ L_2, \sigma] n @ L_{pc} \xrightarrow{\tau} \mu [(n_1 - n_2) @ (L_1 \vee L_2), \sigma] n + 1 @ L_{pc}}$$

$$\frac{\iota(n) = \text{Output}}{\mu [m @ L_1, \sigma] n @ L_{pc} \xrightarrow{m @ L_1 \vee L_{pc}} \mu [\sigma] n + 1 @ L_{pc}}$$

$$\frac{\iota(n) = \text{Push } m}{\mu [\sigma] n @ L_{pc} \xrightarrow{\tau} \mu [m @ \perp, \sigma] n + 1 @ L_{pc}}$$

$$\frac{\iota(n) = \text{Load} \quad \mu(p) = m @ L_2}{\mu [p @ L_1, \sigma] n @ L_{pc} \xrightarrow{\tau} \mu [m @ L_1 \vee L_2, \sigma] n + 1 @ L_{pc}}$$

$$\frac{\iota(n) = \text{Store} \quad \mu(p) = k @ L_3 \quad L_1 \vee L_{pc} \leq L_3}{\mu(p) \leftarrow (m @ L_1 \vee L_2 \vee L_{pc}) = \mu'}{\mu [p @ L_1, m @ L_2, \sigma] n @ L_{pc} \xrightarrow{\tau} \mu' [\sigma] n + 1 @ L_{pc}}$$

$$\frac{\iota(n) = \text{Jump}}{\mu [n' @ L_1, \sigma] n @ L_{pc} \xrightarrow{\tau} \mu [\sigma] n' @ (L_1 \vee L_{pc})}$$